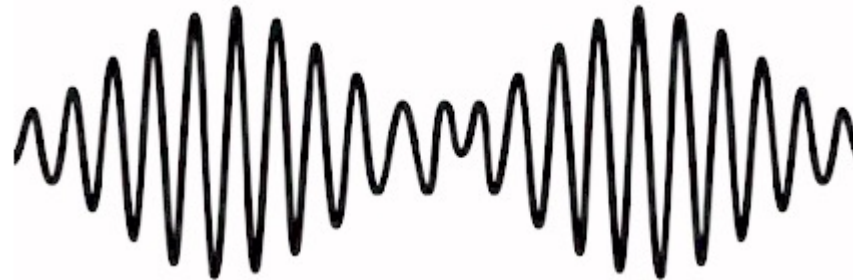


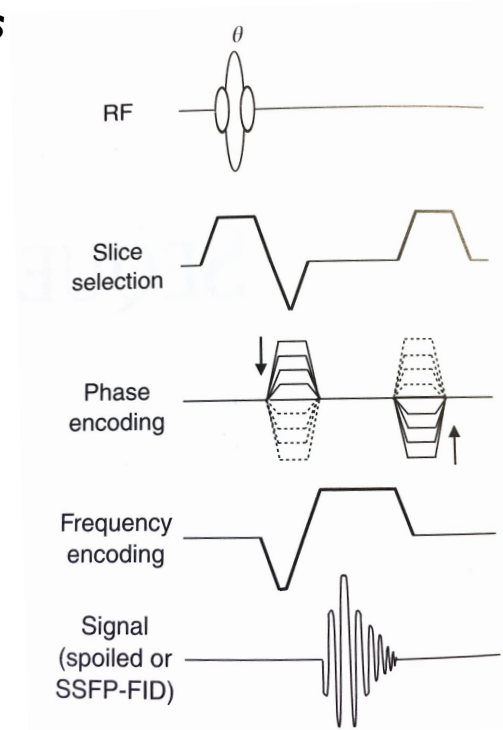
Basic Pulse Sequences

Saturation and Inversion Recovery



Basic Sequences - Gradient Echo (GE or GRE)

- **Class of sequences primarily used for fast scanning** (Frahm et al., *Magn Reson Med*, 1986)
- **GRE used widely for 3D volumetric imaging**
 - **Brain imaging, cardiac/vascular imaging requiring breath-hold, etc.**
- **Also referred to as Gradient Echoes, Gradient Recalled Echoes, Gradient Refocused Echoes, and Field Echoes**



GRE Advantages

Fast Imaging Applications

Why? *Can use a shorter TE/TR than spin echo.*

When? Breath-held, realtime, & 3D volume imaging

Bright blood signal

Why? Inflowing spins haven't "seen" numerous RF pulses.

When? Cardiovascular & angiographic applications.

Low SAR

Why? Imaging flip angles are small.

When? When heating risks are a concern (devices, high field)



GRE Advantages

Quantitative

Why? Multi-echo acquisition are practical.

When? Flow quantification & Fat/Water mapping

Susceptibility Weighted Imaging

Why? No refocusing pulse.

When? T_2^* -weighted & imaging hemorrhage

Reduced Cross-talk

Why? SE hard to match slice profile of 90° & 180°

When? Little or no slice gap for 2D multi-slice



GRE Disadvantages

Off-resonance sensitivity

Why? Field inhomogeneity, Susceptibility, & Chemical shift

T₂*-weighted rather than T₂-weighted

Why? No re-focusing pulse

Larger metal artifacts than SE

Why? No refocusing pulse.



GRE Applications

Primarily used for fast scanning

Flip angle typically $<90^\circ$

Only short time needed for T_1 recovery

Short TRs (2-50ms)

Short TEs (2-10ms)

Therefore, weights T_1 differences

Varying TE can provide T_2^* contrast

Combines field heterogeneity and susceptibility weighting

3D volume imaging

Cardiac/Cardiovascular imaging

Time-of-flight and phase contrast MRA

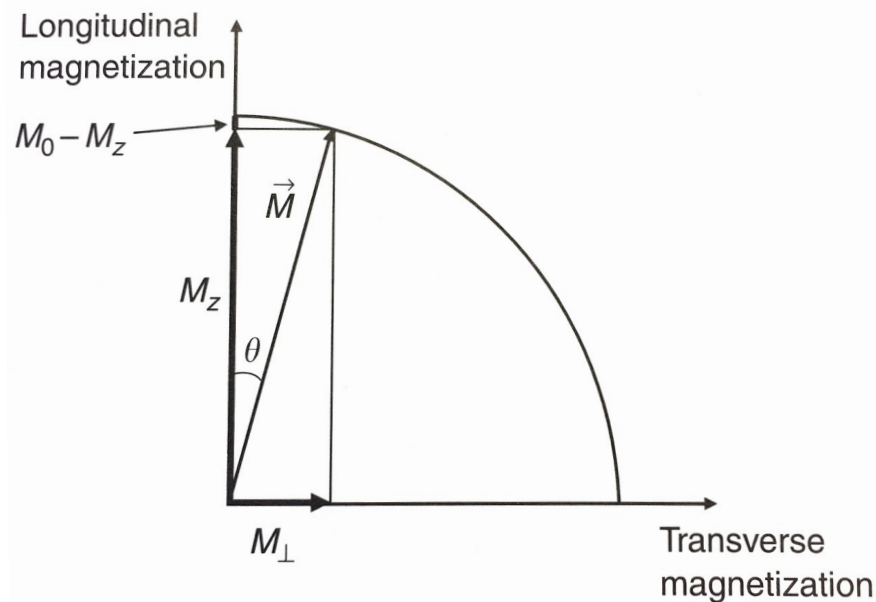
Sequence names

FLASH, FISP/true-FISP, GRASS

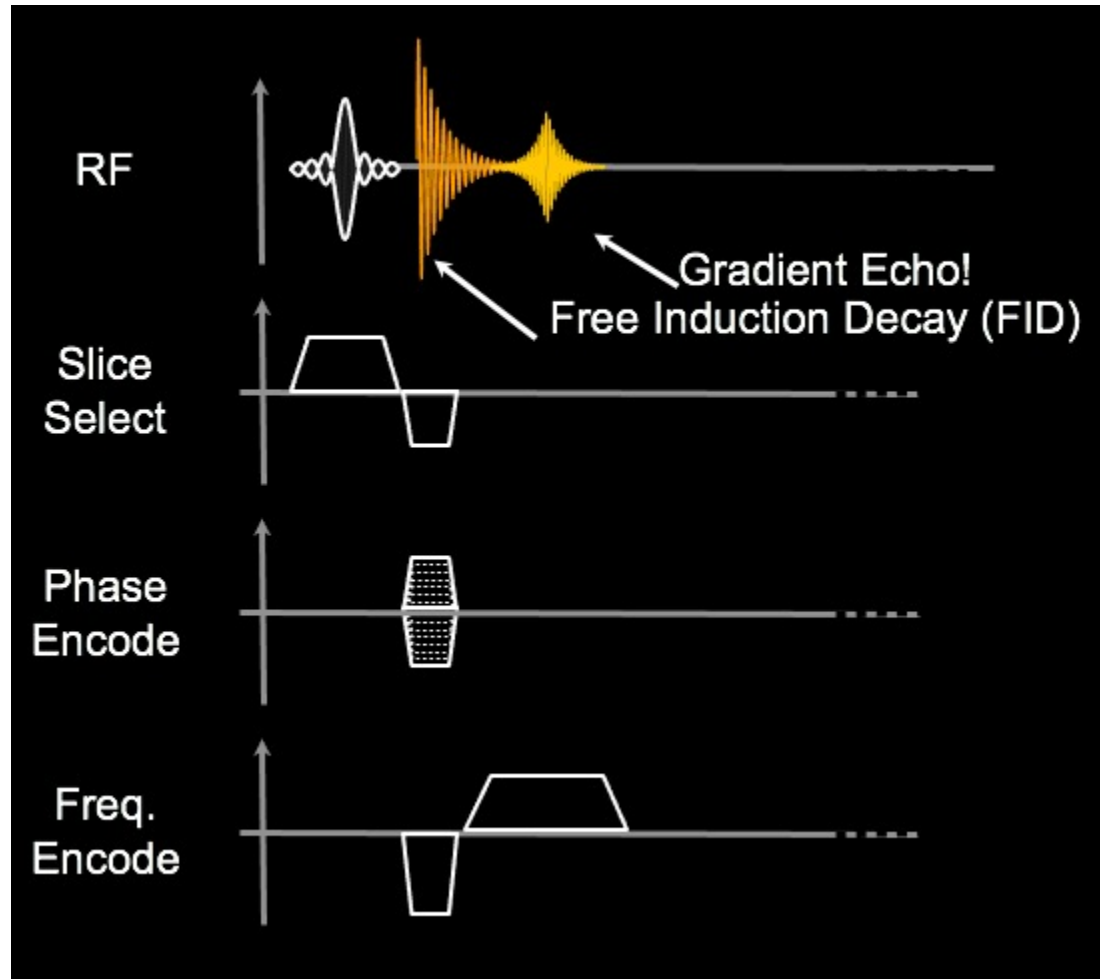


Basic Sequences - Gradient Echo (GE or GRE)

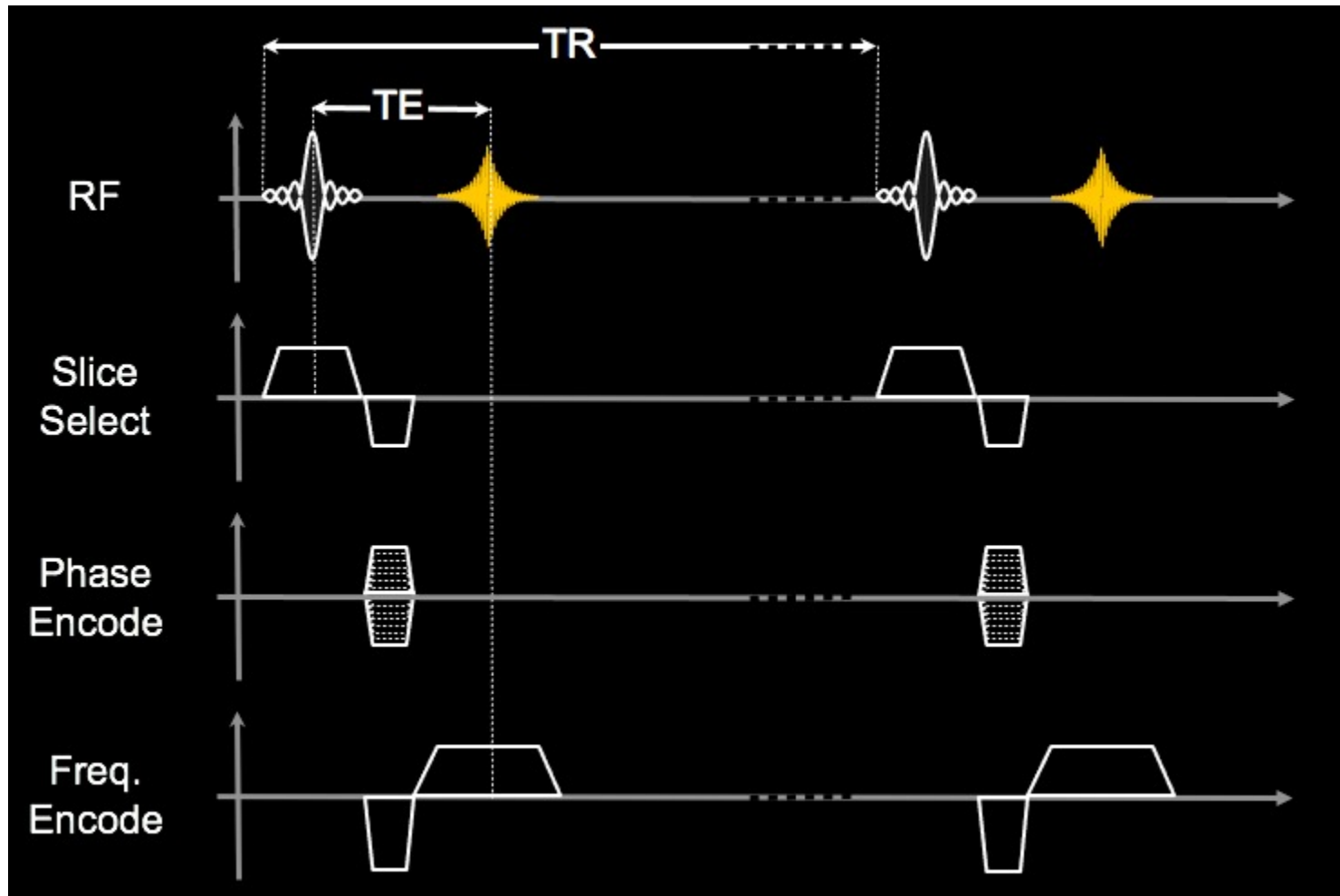
- **GRE acquisitions can be very fast, partially due to using a low flip angle (θ) and short TR**
- **Useful for fast imaging, 3D imaging, time-of-flight (TOF) and phase-contrast angiography, and susceptibility-weighting.**
- **Note that the amount of transverse magnetization created by an RF excitation pulse is much greater than the loss of longitudinal magnetization, resulting in faster acquisition via shorter TR... ($M_{\perp} \gg (M_0 - M_z)$)**
- **For values of $\theta \ll 1$ radian, $\sin\theta \approx \theta \gg 1 - \cos\theta \approx \theta^2/2$**



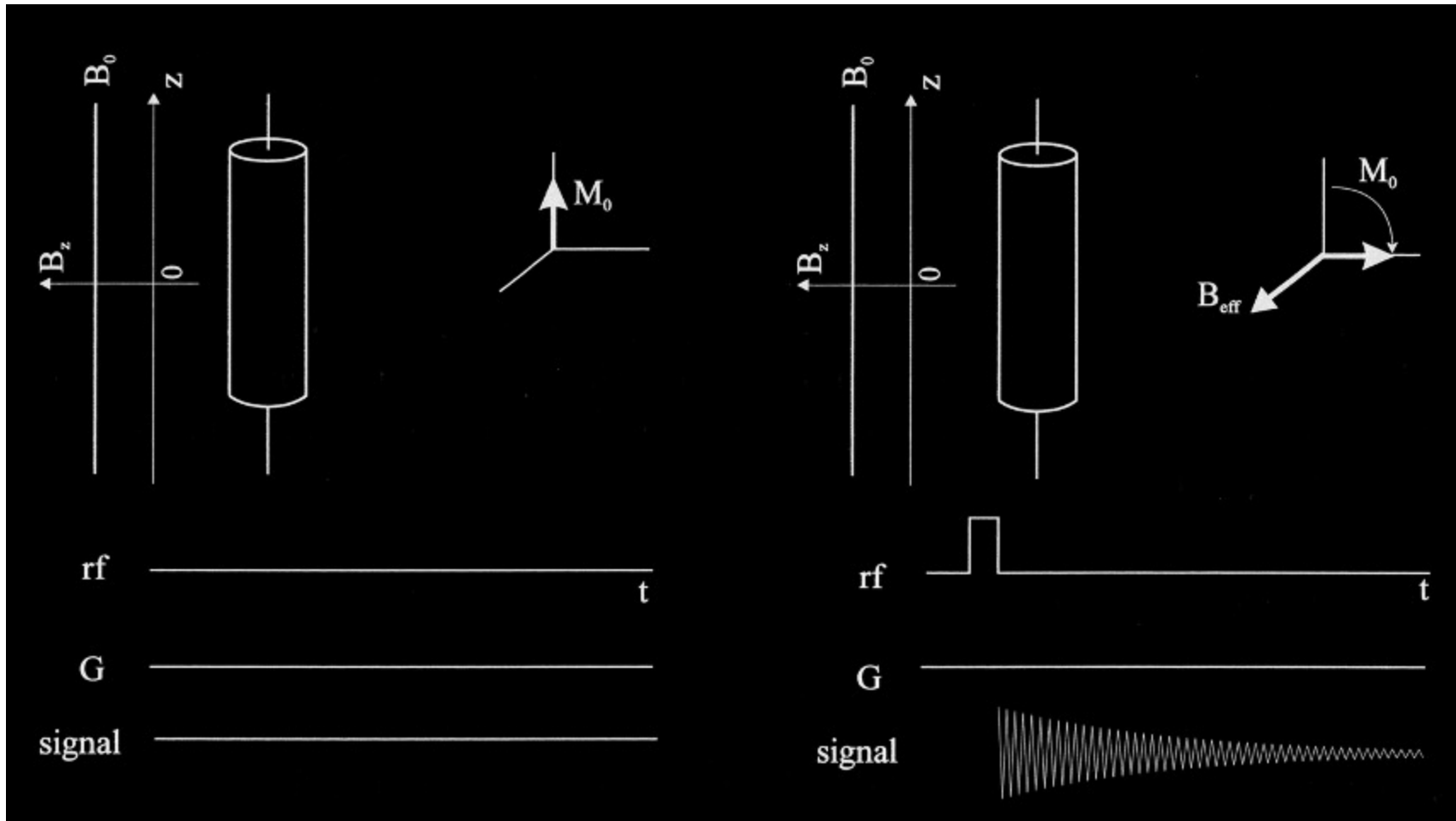
Basic Gradient Echo Pulse Sequence



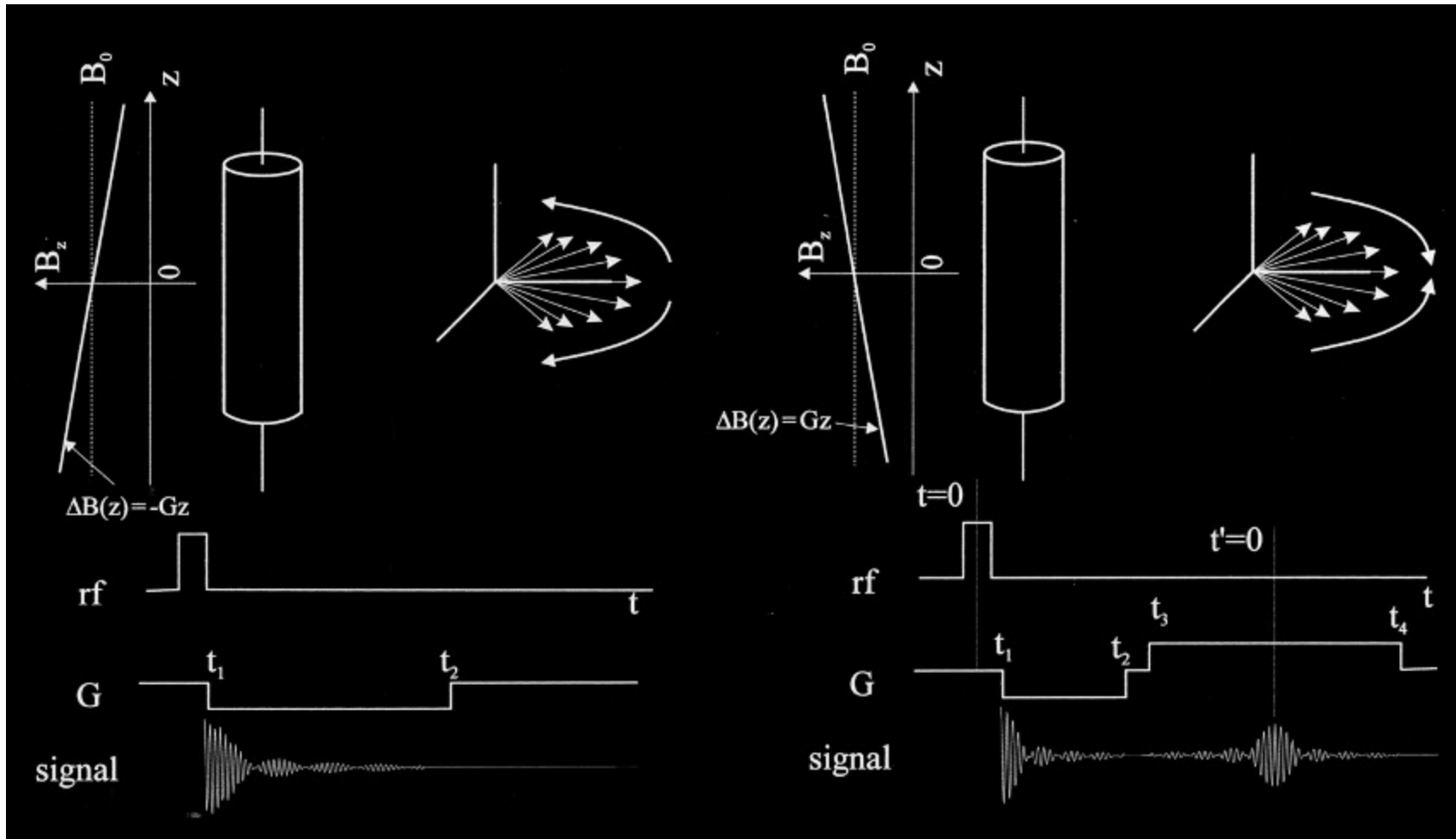
Basic Gradient Echo Pulse Sequence



Basic Gradient Echo Pulse Sequence

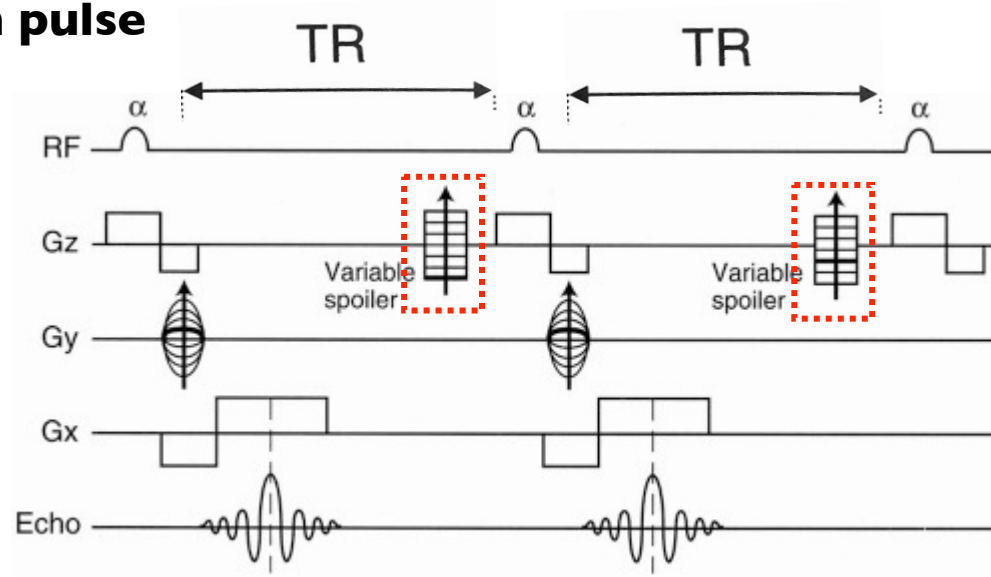


Basic Gradient Echo Pulse Sequence



Basic Sequences - Gradient Echo (GE or GRE)

- ***Spoiled GRE*** - When transverse magnetization is zero before each excitation pulse

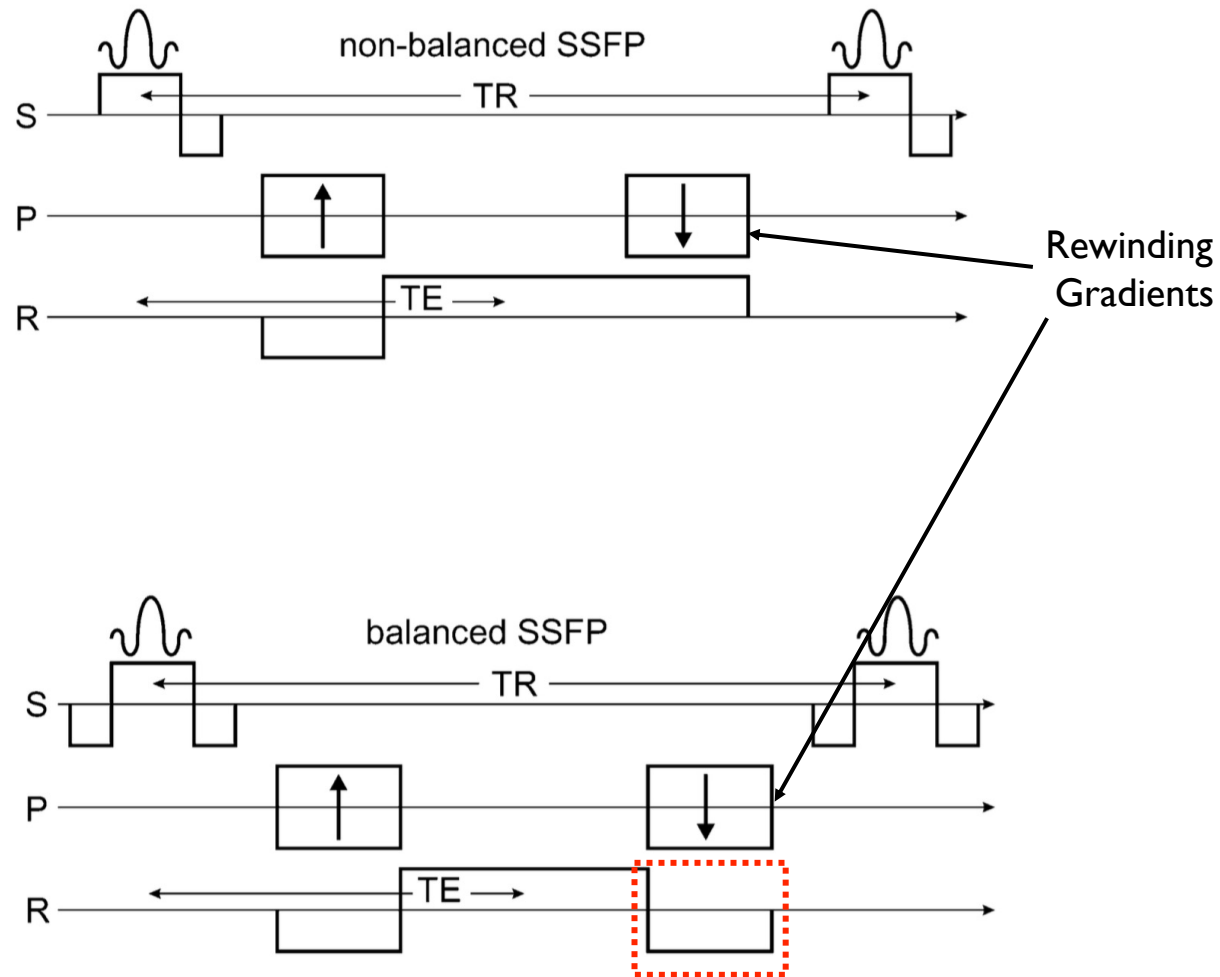


- ***Steady-State Free Precession (SSFP)*** - When transverse magnetization reaches a non-zero steady state just before application of each excitation pulse



Basic Sequences - Gradient Echo (GE or GRE)

- **Balanced SSFP - Special type of SSFP sequence where gradient-induced dephasing within each TR is exactly zero.**



Basic Sequences - Gradient Echo (GE or GRE)

- **Comparison across vendors**

Gradient Echo Pulse Sequences					
Academic Classification	Spoiled Gradient Echo		Steady-State Free Precession (SSFP)		Balanced Steady-State Free Precession (bSSFP)
	Ordinary type	Turbo type (Magnetization preparation, extremely low angle shot, short TR)	FID-like	Echo-like	
Siemens	FLASH Fast Imaging using Low Angle Shot	TurboFLASH Turbo FLASH	FISP Fast Imaging with Steady-state Precession	PSIF Reversed FISP	TrueFISP True FISP
GE	SPGR Spoiled GRASS	FastSPGR Fast SPGR	GRASS Gradient Recall Acquisition using Steady States	SSFP Steady State Free Precession	FIESTA Fast Imaging Employing Steady-state Acquisition
Philips	T₁ FFE T ₁ -weighted Fast Field Echo	TFE Turbo Field Echo	FFE Fast Field Echo	T₂-FFE T ₂ -weighted Fast Field Echo	b-FFE Balanced Fast Field Echo



Basic Sequences - Gradient Echo (GE or GRE)

- **Comparison across vendors**

TABLE 14.1
Commercial Names of Common GRE Pulse Sequences Used by a Few MR Equipment Vendors^a

Vendor	Spoiled Gradient Echo	SSFP-FID or Gradient Echo	SSFP-Echo, or CE-FAST	Balanced SSFP or True FISP	Multiacquisition SSFP or CISS	Dual-Echo SSFP or DESS
General Electric	SPGR	Gradient echo or GRASS	SSFP ^b	FIESTA	FIESTA-C	—
Philips	CE-FFE-T1 or T1-FFE	FFE	CE-FFE-T2 T2-FFE	Balanced FFE	—	—
Siemens	FLASH	FISP	PSIF	TrueFISP	CISS	DESS

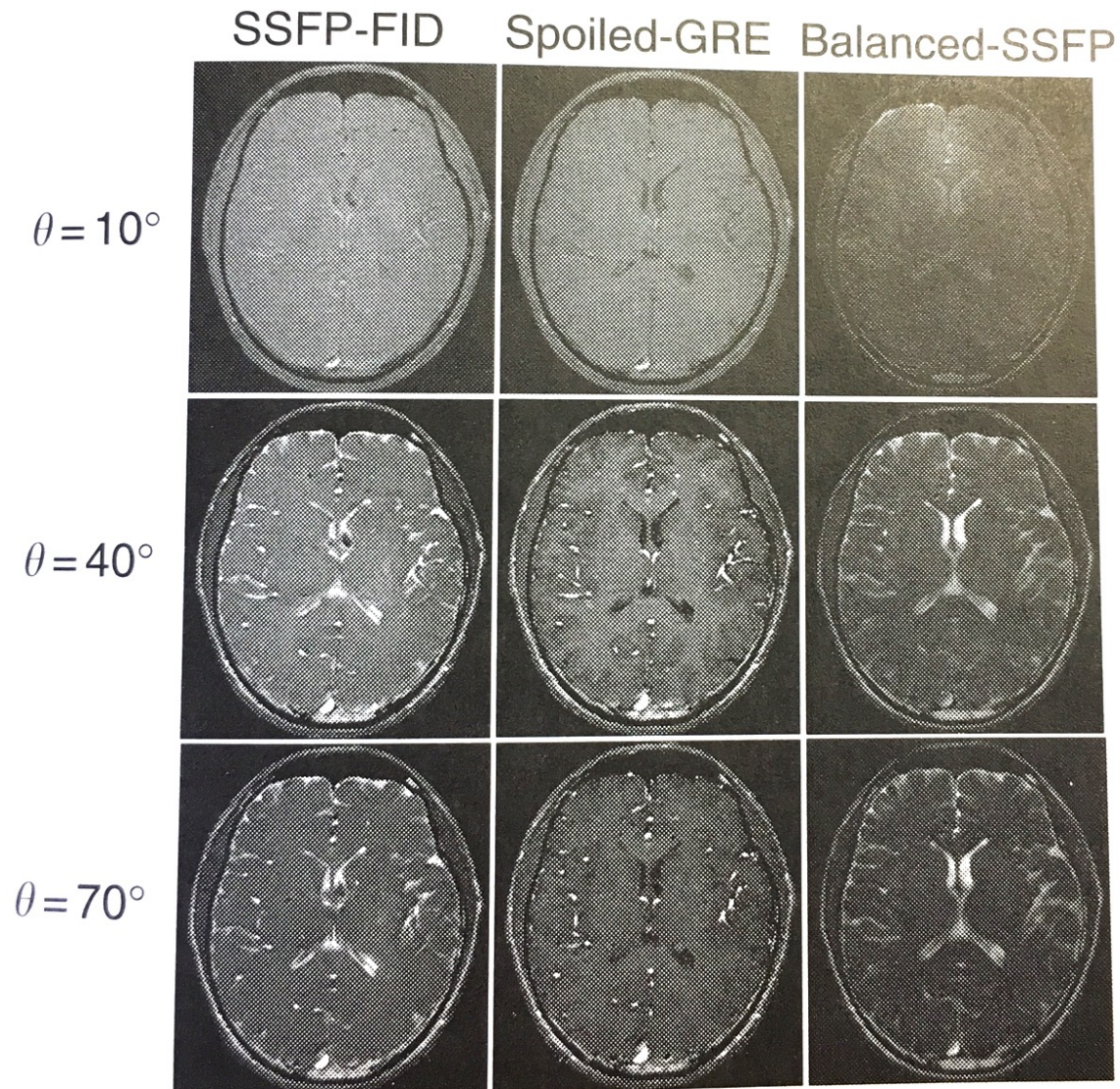
^aCE-FAST, contrast-enhanced Fourier-acquired steady state; CE-FFE, contrast-enhanced fast field echo; CISS, constructive interference in the steady state; DESS, dual-echo steady state; FFE, fast field echo; FID, free-induction decay; FIESTA, fast imaging employing steady-state acquisition; FIESTA-C, fast imaging employing steady-state acquisition with phase cycling; FISP, fast imaging with steady (-state free) precession; FLASH, fast low-angle shot; GRASS, gradient recalled acquisition in the steady state; PSIF, reversed fast imaging with steady (-state free) precession; SPGR, spoiled gradient echo; SSFP, steady-state free precession.

^bSSFP-Echo pulse sequence not currently offered by General Electric.



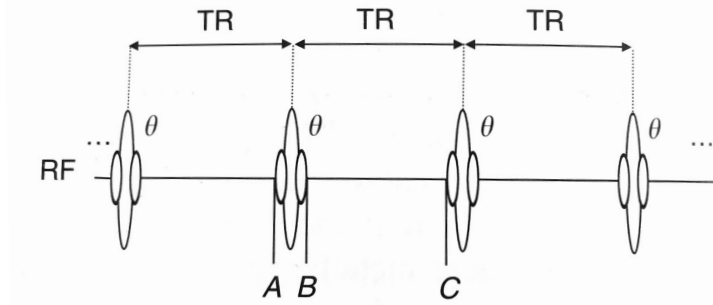
Basic Sequences - Gradient Echo (GE or GRE)

- **Useful for fast imaging, 3D imaging, time-of-flight (TOF) and phase-contrast angiography, susceptibility-weighting, DCE-MRI, and T2* mapping**



Basic Sequences - Gradient Echo (GE or GRE)

- **Steady State of the Longitudinal Magnetization for the Spoiled GRE Sequence:**



$$M_{zC} = M_{zB} e^{-TR/T_1} + M_0 \left(1 - e^{-TR/T_1} \right) = M_{zA} \cos \theta \cdot E_1 + M_0 (1 - E_1)$$

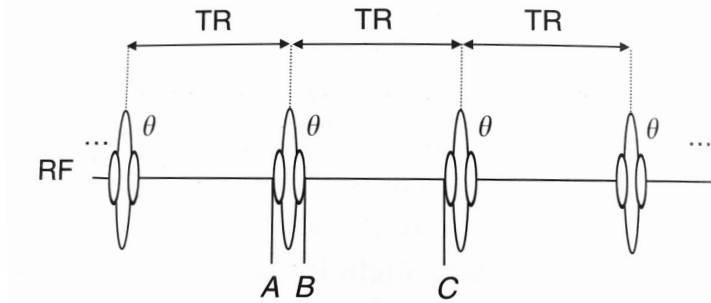
$$E_1 = e^{-TR/T_1}$$

- **At steady state, $M_{zA} = M_{zC}$**



Basic Sequences - Gradient Echo (GE or GRE)

- **Steady State of the Longitudinal Magnetization for the Spoiled GRE Sequence:**



$$M_{zC} = M_{zB} e^{-TR/T_1} + M_0 \left(1 - e^{-TR/T_1} \right) = M_{zA} \cos \theta \cdot E_1 + M_0 (1 - E_1)$$

$$E_1 = e^{-TR/T_1}$$

- **At steady state, $M_{zA} = M_{zC}$**

$$M_{zA} = M_{zA} \cos \theta \cdot E_1 + M_0 (1 - E_1)$$

$$\frac{M_{zA}}{M_0} = \frac{M_{zA}}{M_0} \cos \theta \cdot E_1 + 1 - E_1$$

$$\frac{M_{zA}}{M_0} - \frac{M_{zA}}{M_0} \cos \theta \cdot E_1 = 1 - E_1$$

$$\frac{M_{zA}}{M_0} (1 - \cos \theta \cdot E_1) = 1 - E_1$$

$$\frac{M_{zA}}{M_0} = \frac{1 - E_1}{1 - \cos \theta \cdot E_1} \equiv f_{z,ss}$$



Basic Sequences - Gradient Echo (GE or GRE)

- **Signal Intensity of the the Spoiled GRE Sequence:**

$$S_{\text{spoil}} = M_{zA} \sin \theta \cdot e^{-TE/T_2^*}$$



Basic Sequences - Gradient Echo (GE or GRE)

- **Signal Intensity of the the Spoiled GRE Sequence:**

$$S_{\text{spoil}} = M_{zA} \sin \theta \cdot e^{-TE/T_2^*}$$

$$\frac{M_{zA}}{M_0} = \frac{1 - E_1}{1 - \cos \theta \cdot E_1}$$

$$\frac{S_{\text{spoil}}}{M_0 \cdot \sin \theta \cdot e^{-TE/T_2^*}} = \frac{1 - E_1}{1 - \cos \theta \cdot E_1}$$

$$S_{\text{spoil}} = \frac{M_0 \cdot \sin \theta \cdot E_2^* (1 - E_1)}{1 - \cos \theta \cdot E_1}$$

**Contrast adjusted by changing
flip angle, TE and TR.**



Gradient Echo Contrast

Gradient Echo Parameters

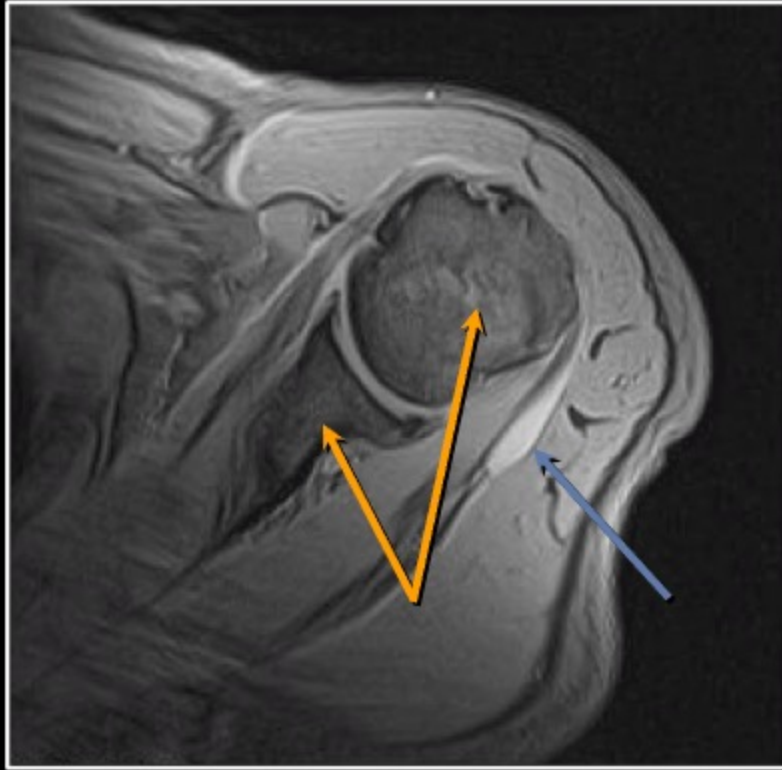
Type of Contrast	TE	TR	Flip Angle
Spin Density	Short	Long	Small
T ₁ -Weighted	Short	Intermediate	Large
T ₂ [*] -Weighted	Intermediate	Long	Small

Gradient Echo Parameters

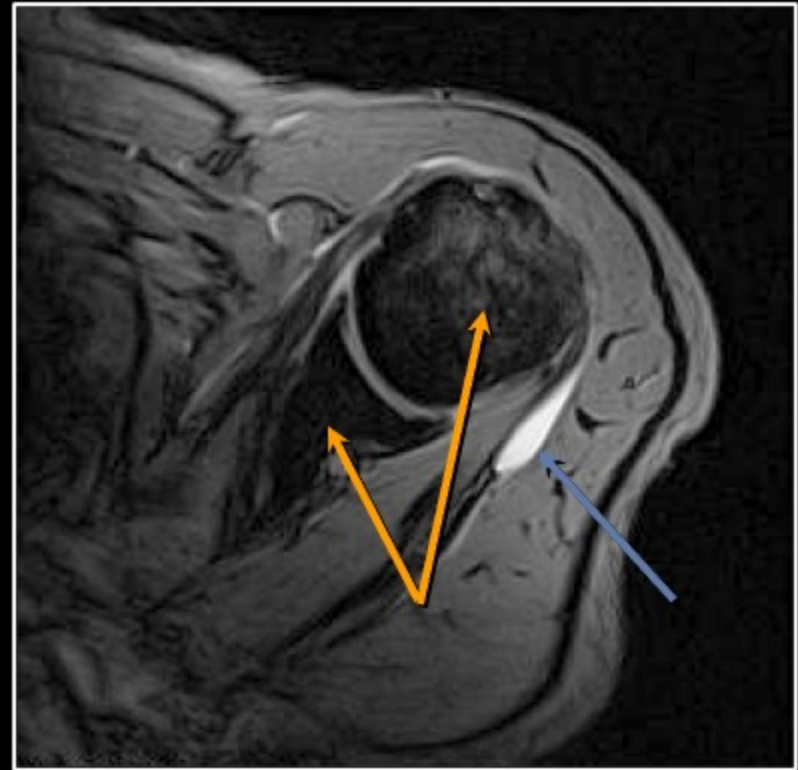
Type of Contrast	TE	TR	Flip Angle
Spin Density	<5ms	>100ms	<10°
T ₁ -Weighted	<5ms	<50ms	>30°
T ₂ [*] -Weighted	>20ms	>100ms	<10°



T2*-Weighted GRE



TE=9ms



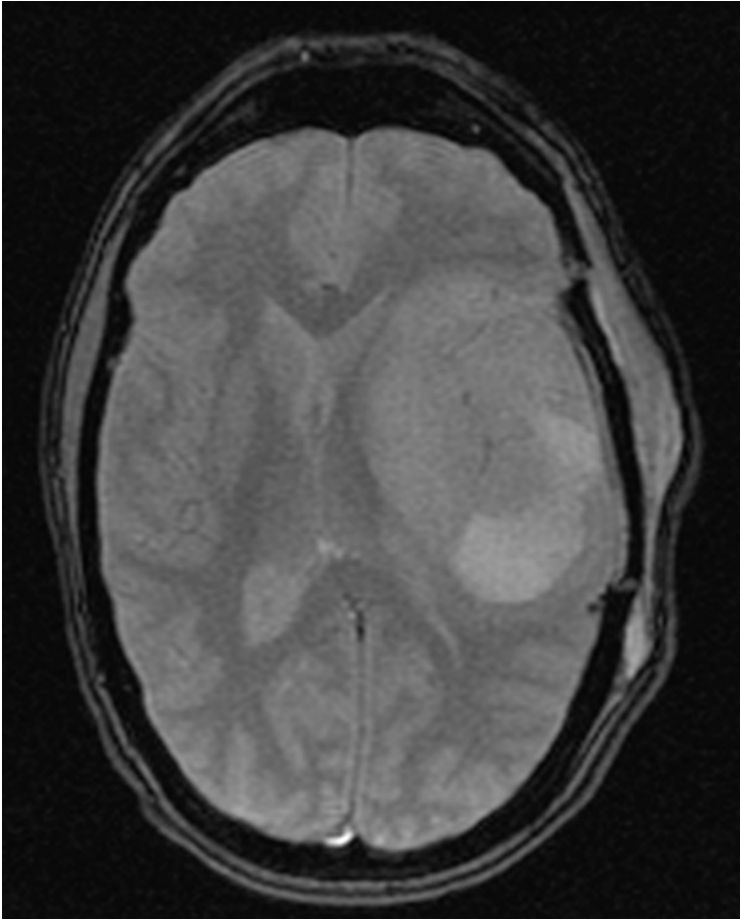
TE=30ms

Susceptibility Weighting (darker with longer TE)
Bright fluid signal (long T₂* is brighter with longer TE)

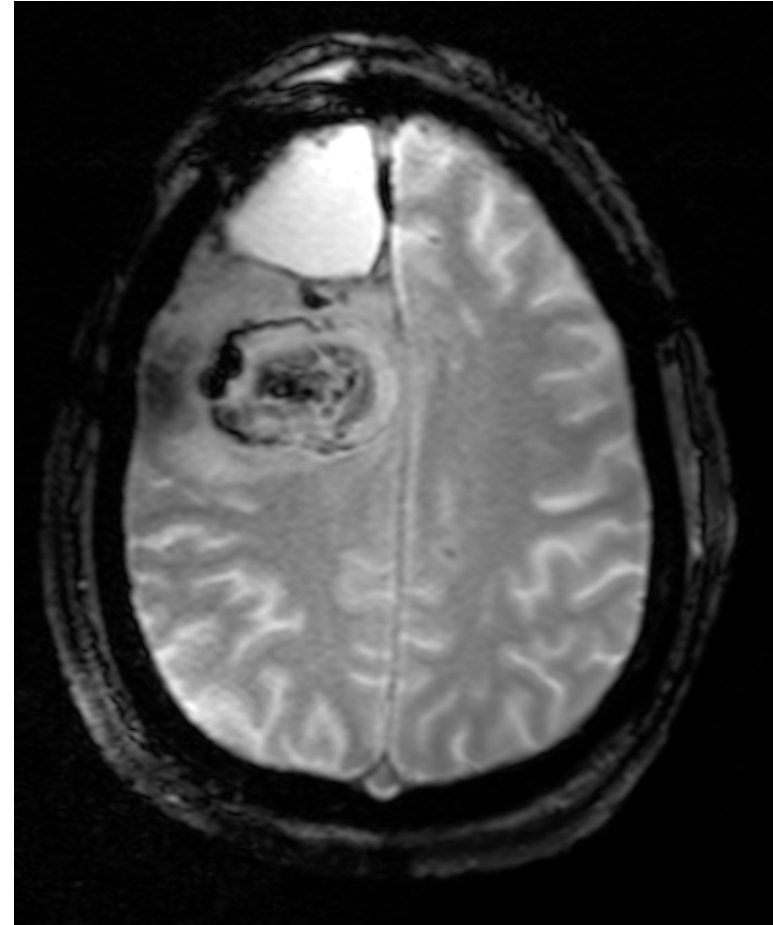


T2*-Weighted GRE

TE=15ms



TE=26ms



Basic Sequences - Gradient Echo (GE or GRE)

- **Ernst Angle - Flip angle that maximizes the spoiled GRE signal**
 - **Setting the first derivative to zero and verifying the 2nd derivative is negative (local maxima) yields:**



Basic Sequences - Gradient Echo (GE or GRE)

- **Ernst Angle - Flip angle that maximizes the spoiled GRE signal**
 - **Setting the first derivative to zero and verifying the 2nd derivative is negative (local maxima) yields:**

$$S_{\text{spoil}} = \frac{M_0 \cdot \sin \theta \cdot E_2^* (1 - E_1)}{1 - \cos \theta \cdot E_1}$$

$$\frac{d}{d\theta}(S_{\text{spoil}}) = \frac{d}{d\theta} \left(\frac{M_0 \cdot \sin \theta \cdot E_2^* (1 - E_1)}{1 - \cos \theta \cdot E_1} \right) = 0$$

$$\frac{d}{d\theta}(S_{\text{spoil}}) = 0 = \frac{M_0 \cdot \cos \theta \cdot E_2^* (1 - E_1)}{1 - \cos \theta \cdot E_1} - \frac{M_0 \cdot \cos \theta \cdot E_2^* (1 - E_1) E_1 \sin^2 \theta}{(1 - \cos \theta \cdot E_1)^2}$$

$$\frac{d}{d\theta}(S_{\text{spoil}}) = 0 = \frac{M_0 \cdot E_2^* (1 - E_1)}{1 - \cos \theta \cdot E_1} \left(\cos \theta - \frac{E_1 \sin^2 \theta}{1 - \cos \theta \cdot E_1} \right)$$

$$\cos \theta = \frac{E_1 \sin^2 \theta}{1 - \cos \theta \cdot E_1}$$

$$\cos \theta - \cos^2 \theta \cdot E_1 = E_1 \sin^2 \theta$$

$$\cos \theta = E_1 (\sin^2 \theta + \cos^2 \theta)$$

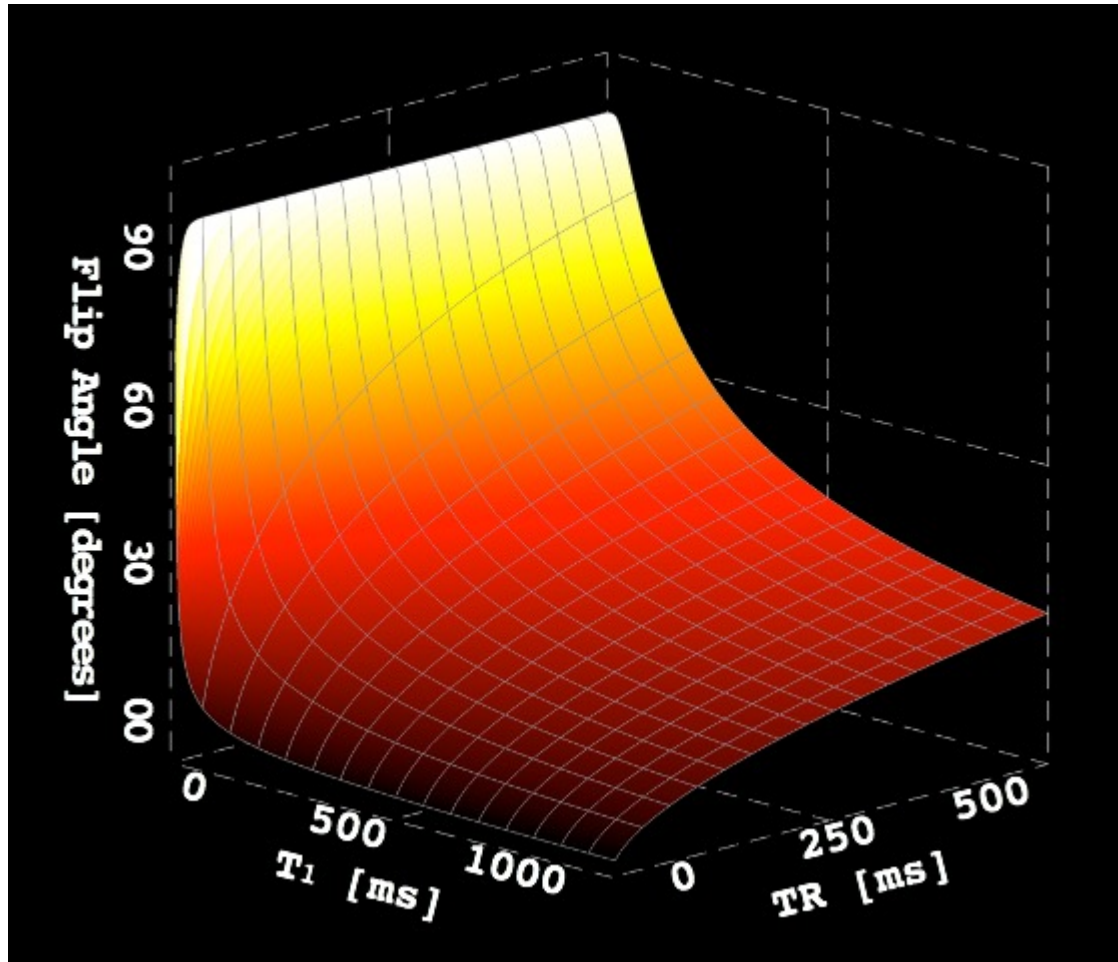
$$\theta = \arccos E_1$$



Basic Sequences - Gradient Echo (GE or GRE)

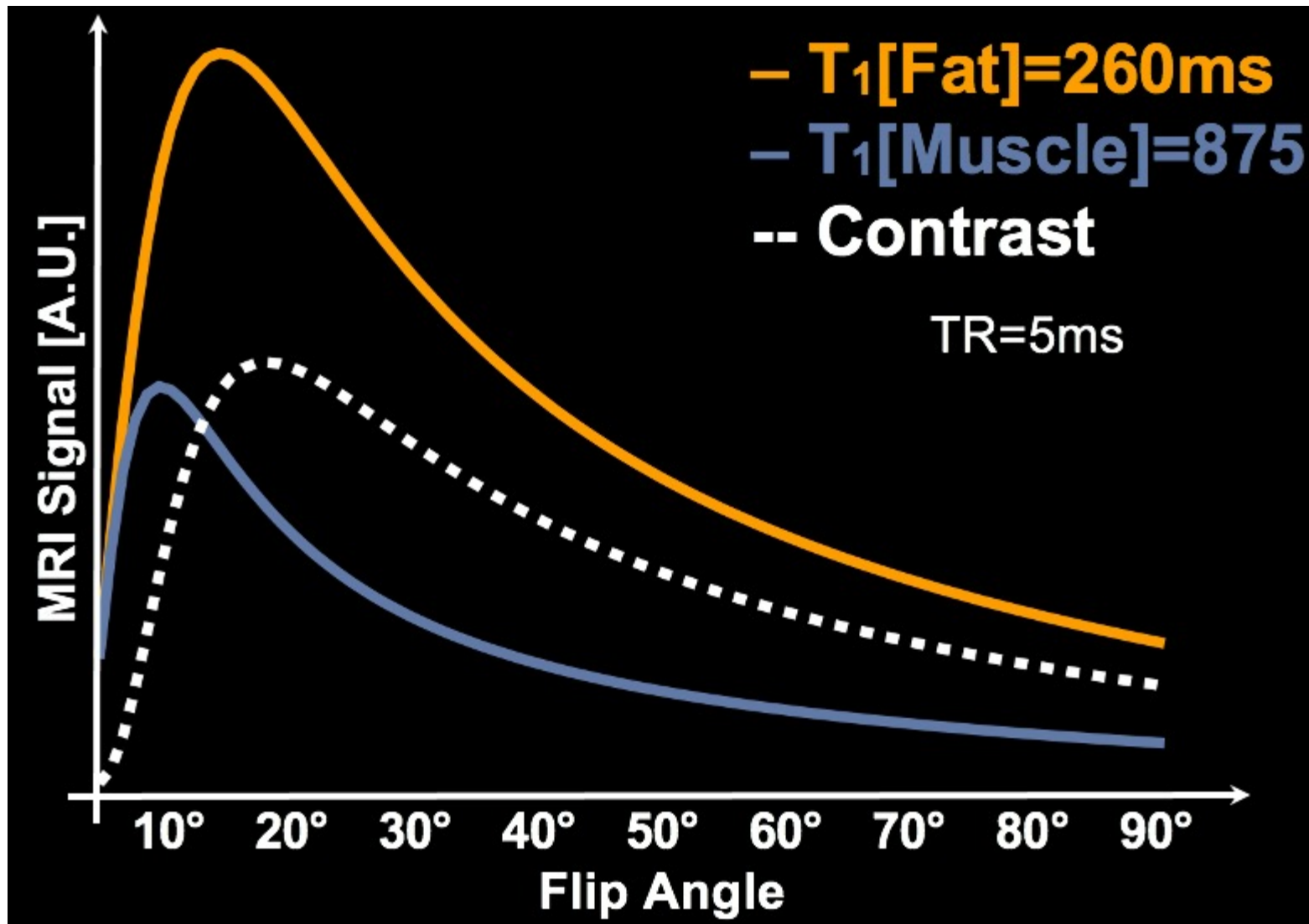
- **Ernst Angle - Flip angle that maximizes the spoiled GRE signal**

$$\theta = \arccos E_1$$



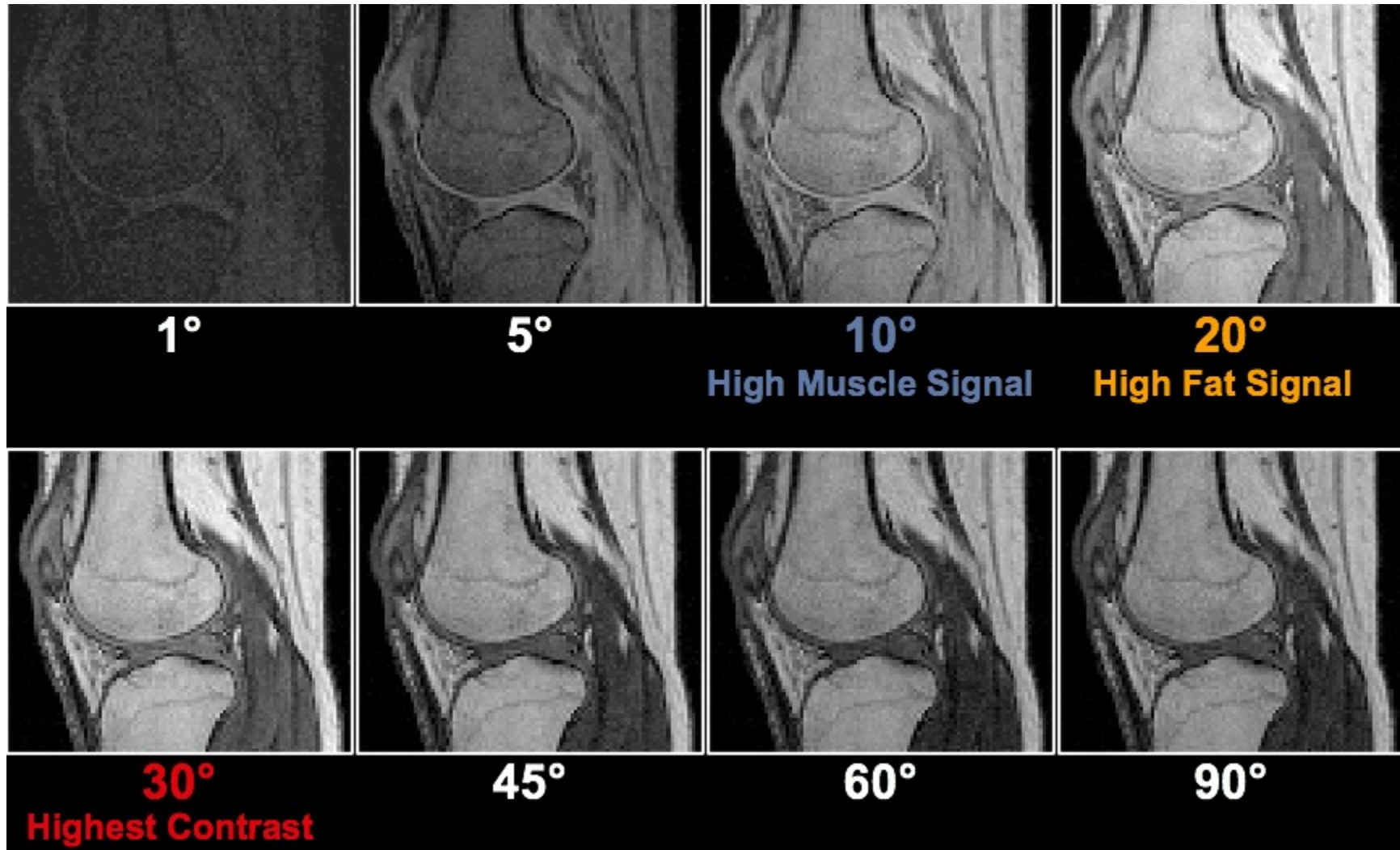
Basic Sequences - Gradient Echo (GE or GRE)

- **Ernst Angle - Flip angle that maximizes the spoiled GRE signal**



Basic Sequences - Gradient Echo (GE or GRE)

- **Ernst Angle - Flip angle that maximizes the spoiled GRE signal**



Why Spoiling?

Eliminates M_{xy} at end of each TR

Prevents cumulative errors/artifacts

Shortens the TR

Faster imaging

Enhances T_1 contrast

T_2 -dependent signal (M_{xy}) is eliminated

Long TR

Choose TR 4-5x T_2^*

Can work for interleaved multi-slice

Gradient spoiling

Applied at end of TR

Dephases spins within voxel

Variable gradient area from TR to TR

Spatially non-uniform

RF spoiling

Cycle the phase of the RF pulse

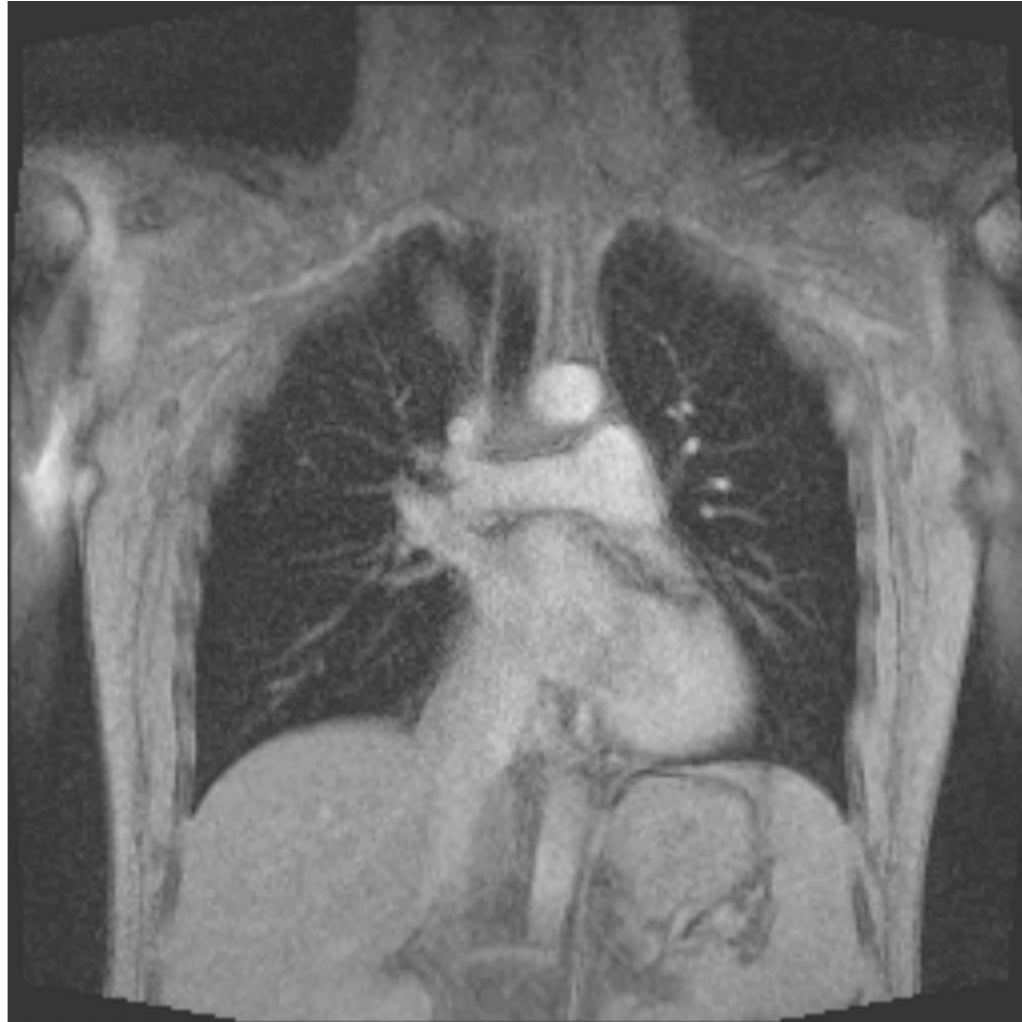
Minimizes coherent signal pathways

Requires a phase encode rewinder

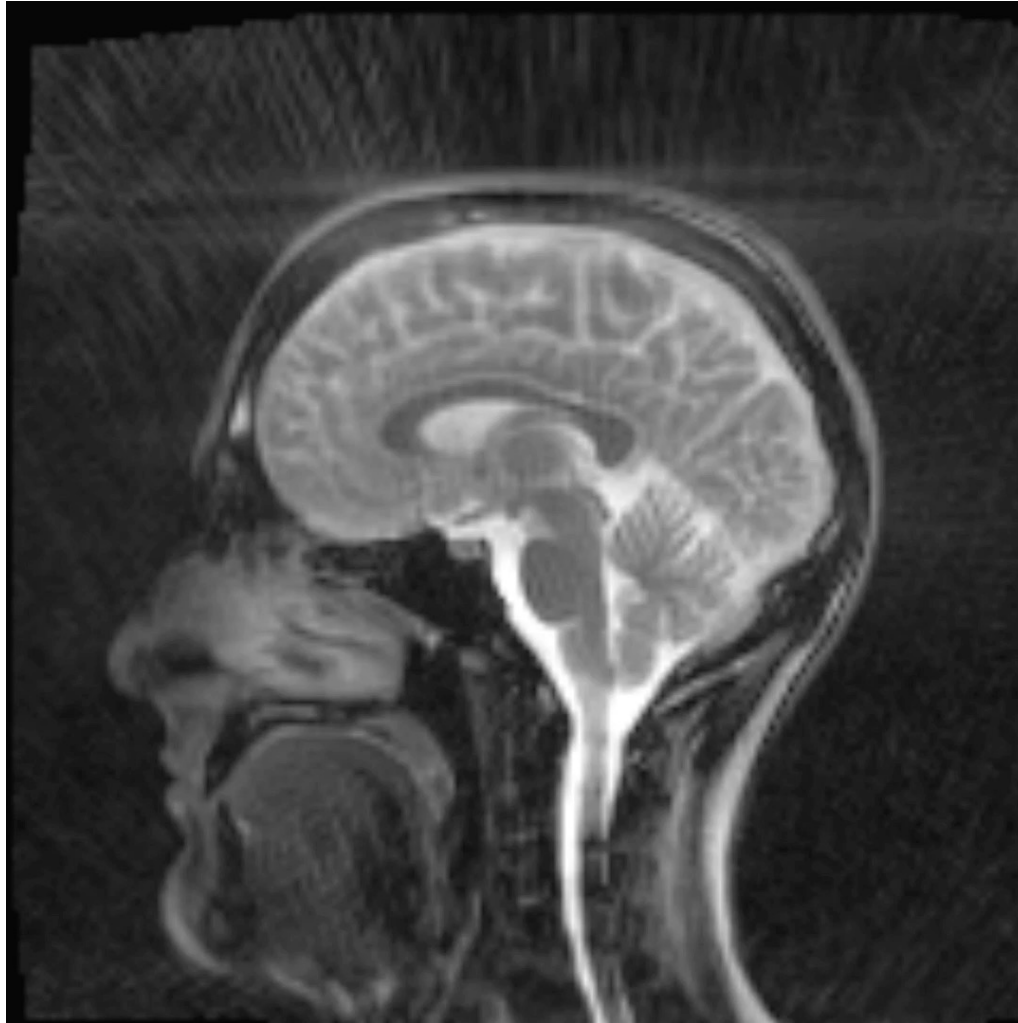
How to Spoil?



Real-Time Imaging with Gradient Echoes



Real-Time Imaging with Gradient Echoes



Basic Sequences - Gradient Echo (GE or GRE)

- **Balanced SSFP Magnetization at Steady State:**

$$M_{ss} = M_0 \frac{\sqrt{E_2(1-E_1)} \sin \theta}{1 - (E_1 - E_2) \cos \theta - E_1 E_2}$$

- **If $TR \ll T_1, T_2$ (reasonable for biological tissues with $TR \sim 3-5ms$)**

$$M_{ss} = M_0 \frac{\sin \theta}{1 + \cos \theta + (1 - \cos \theta) \left(\frac{T_1}{T_2} \right)}$$

- **Ernst Angle is:**

$$\theta = \arccos \left(\frac{\frac{T_1}{T_2} - 1}{\frac{T_1}{T_2} + 1} \right)$$

- **With Maximum Signal Intensity of:**

$$M_{ss} = \frac{1}{2} M_0 \sqrt{\frac{T_1}{T_2}}$$



GRE & Fat/Water Phase

- **Balanced SSFP Magnetization at Steady State:**

$$M_{ss} = M_0 \frac{\sqrt{E_2(1-E_1)} \sin \theta}{1 - (E_1 - E_2) \cos \theta - E_1 E_2}$$

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- **Ernst Angle is:**

$$\theta = \arccos \left(\frac{\frac{T_1}{T_2} - 1}{\frac{T_1}{T_2} + 1} \right)$$

- **With Maximum Signal Intensity of:**

$$M_{ss} = \frac{1}{2} M_0 \sqrt{\frac{T_1}{T_2}}$$



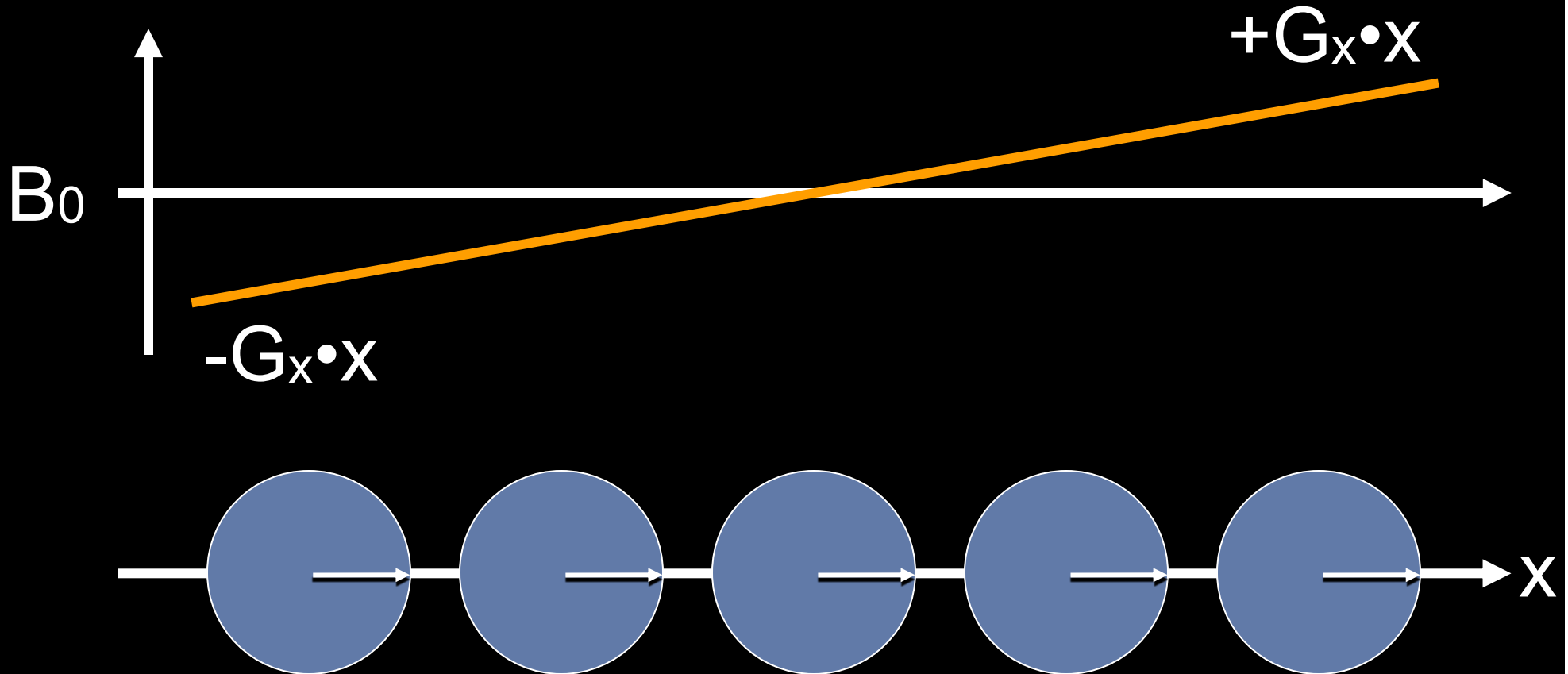
Gradient Echoes & Fat

GRE & Fat/Water Frequency



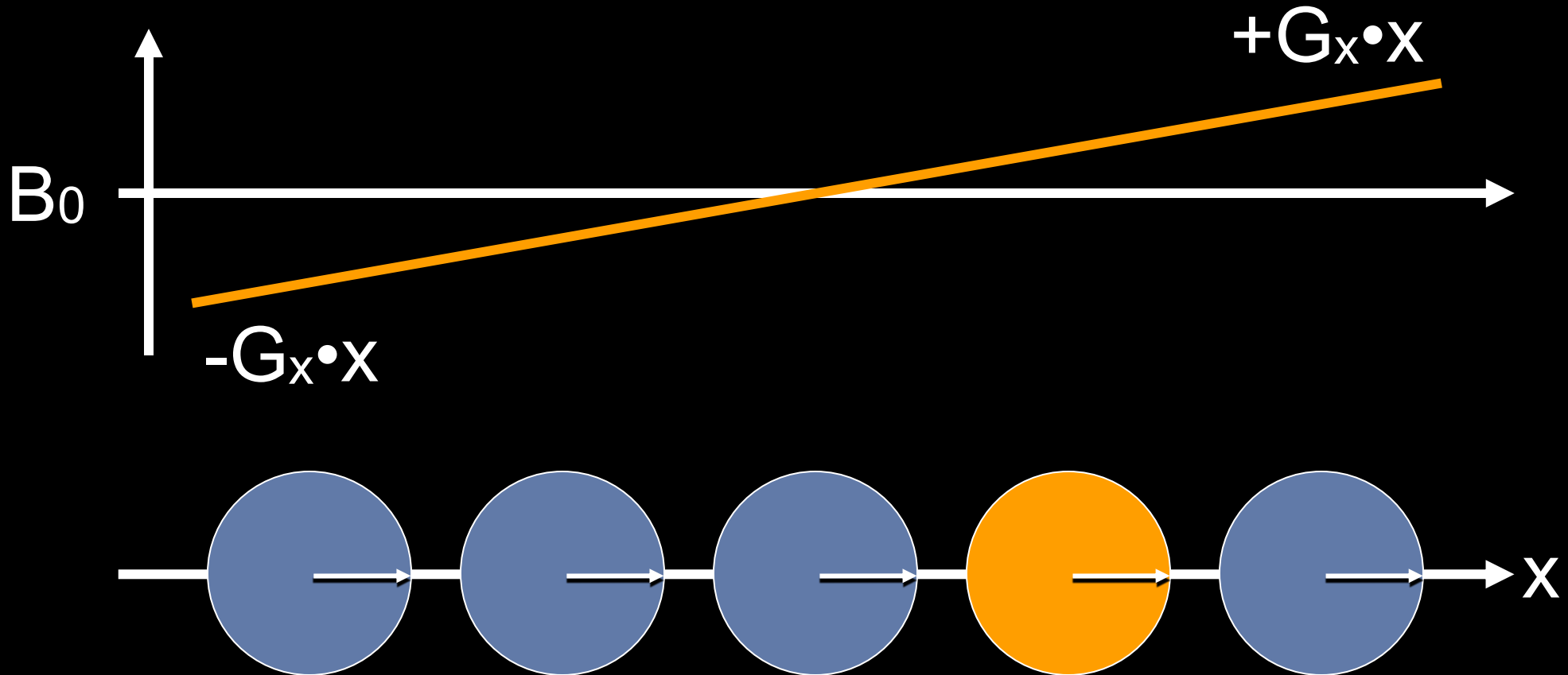
Water Spins in a Uniform Field

GRE & Fat/Water Frequency



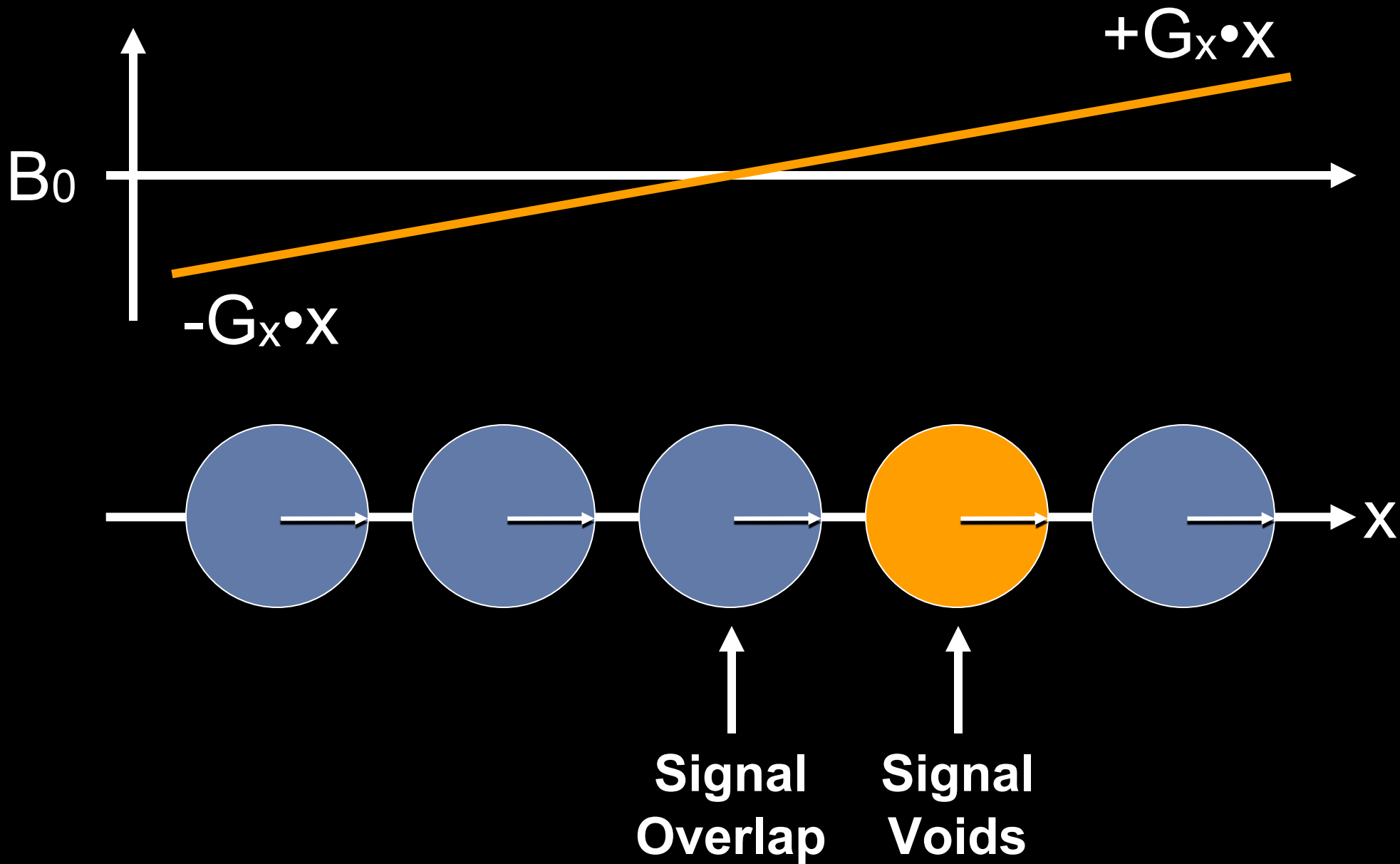
Water Spins in a Gradient Field

GRE & Fat/Water Frequency



Water & Fat Spins in a Gradient Field

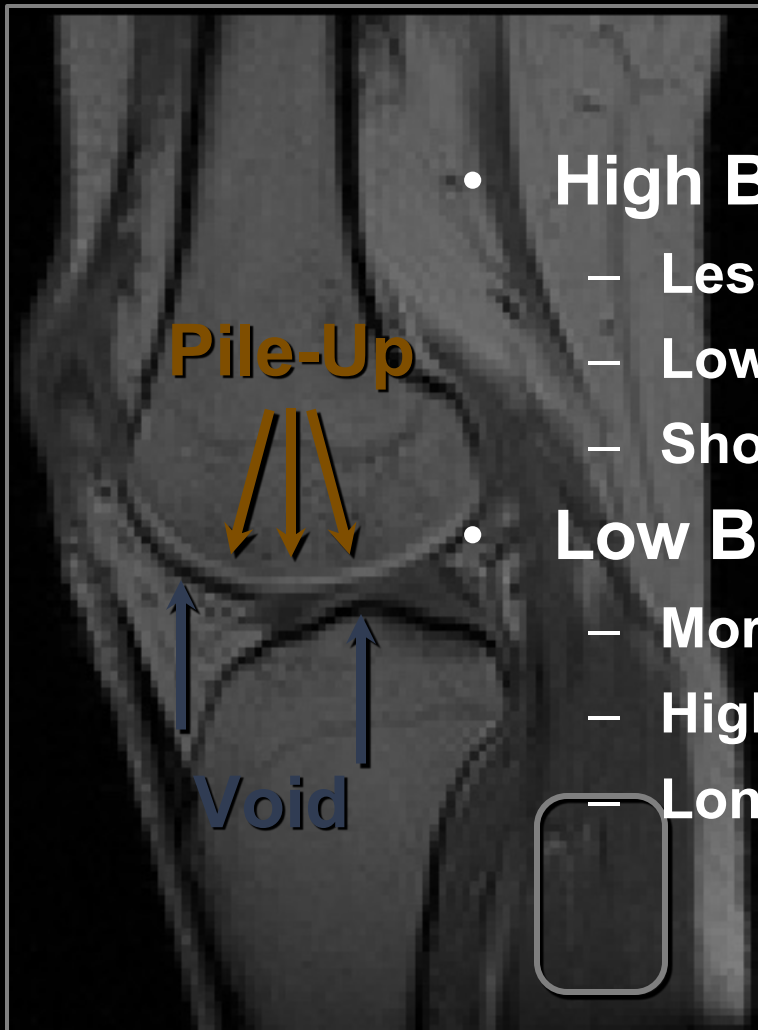
GRE & Fat/Water Frequency



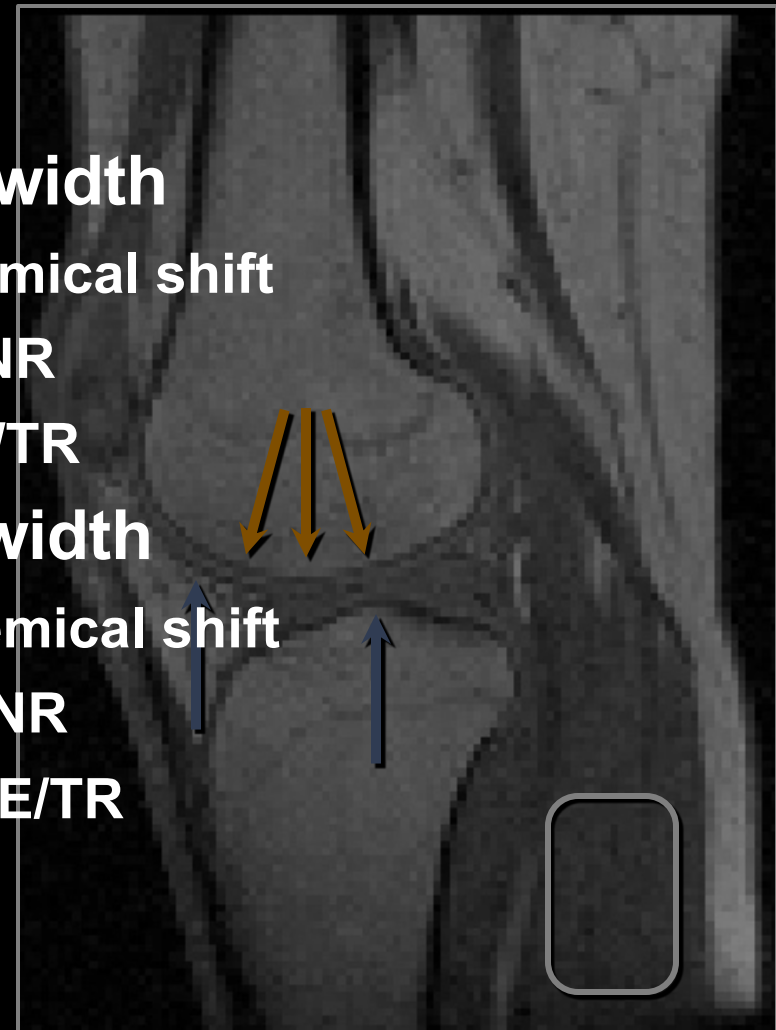
GRE & Fat/Water Frequency

Low Bandwidth

High Bandwidth

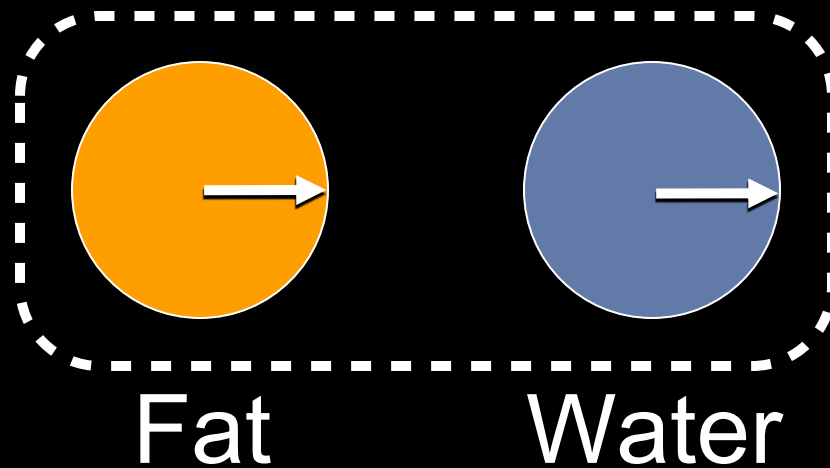


- High Bandwidth
 - Less chemical shift
 - Lower SNR
 - Short TE/TR
- Low Bandwidth
 - More chemical shift
 - Higher SNR
 - Longer TE/TR



GRE and Fat/Water Phase

- Pixels are frequently a mixture of fat and water
- Pixel intensity is the vector sum of fat and water



In-Phase

$$\rightarrow + \rightarrow > 0$$

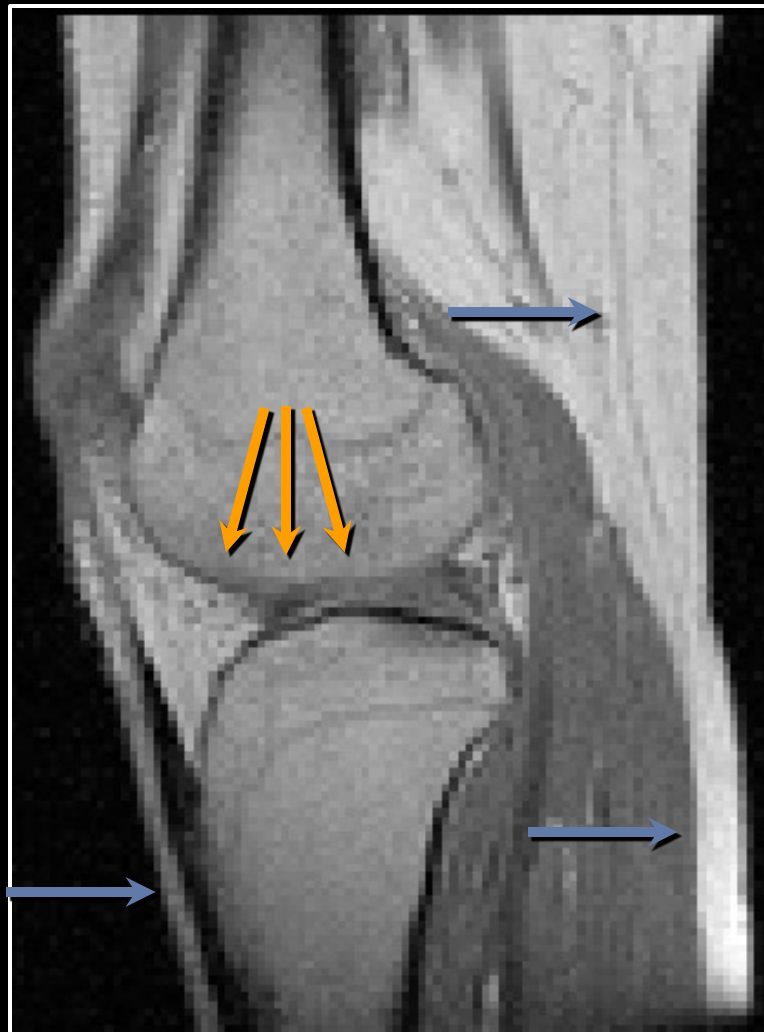
Opposed-Phase

$$\leftarrow + \rightarrow = 0$$

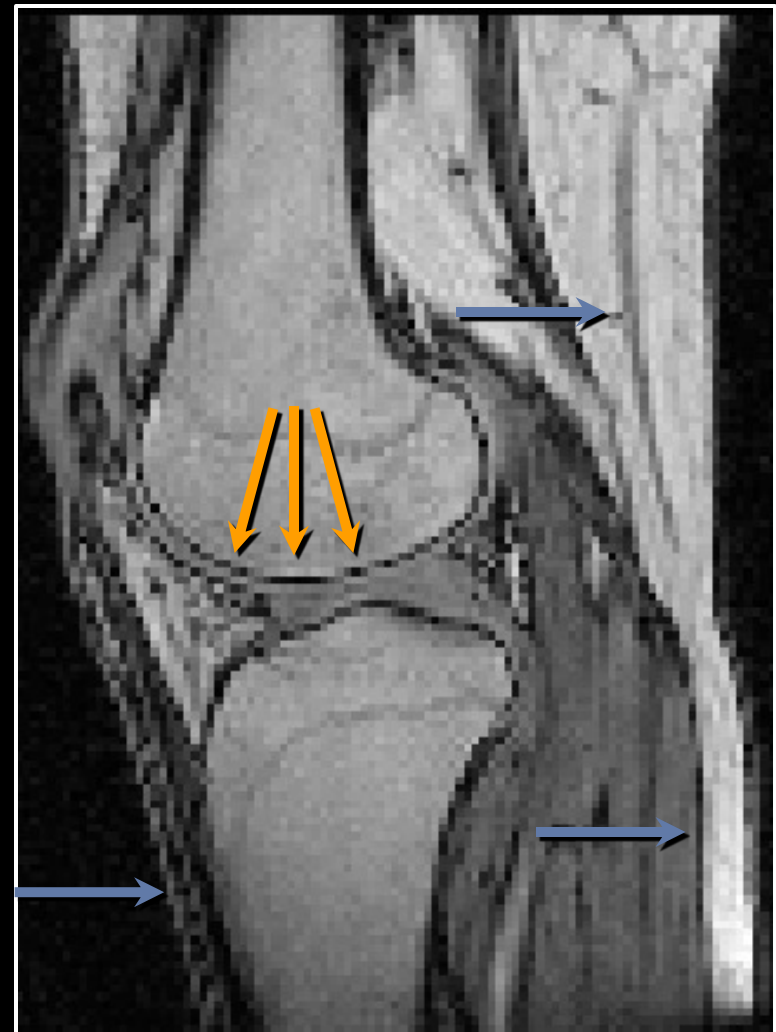
The TE controls the phase between fat and water.

GRE and Fat/Water Phase

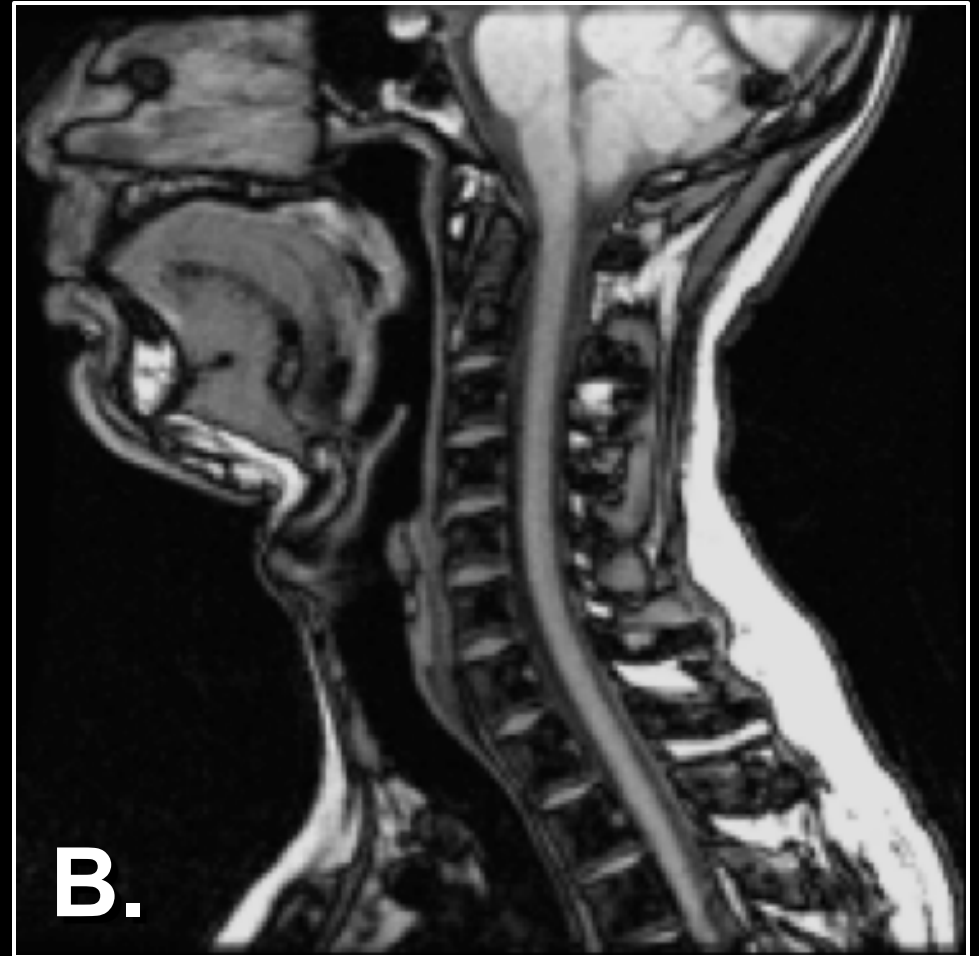
In-Phase



Opposed-Phase

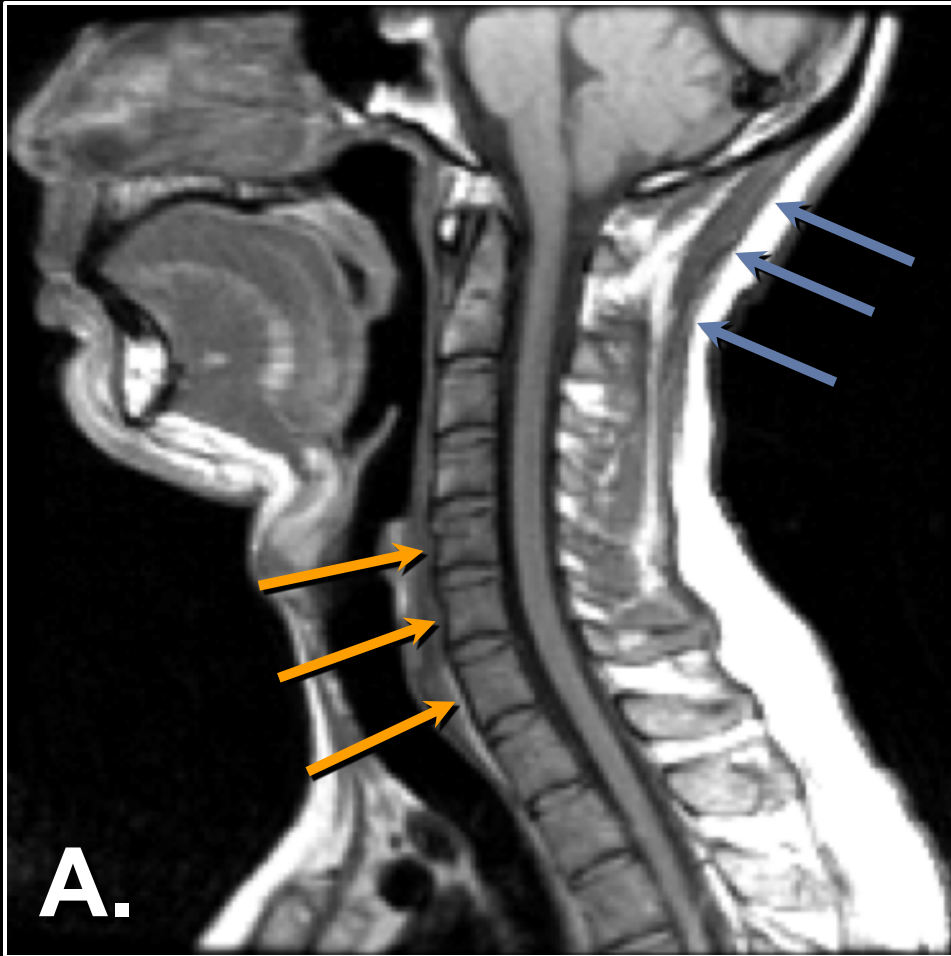


Which image is the in-phase image?

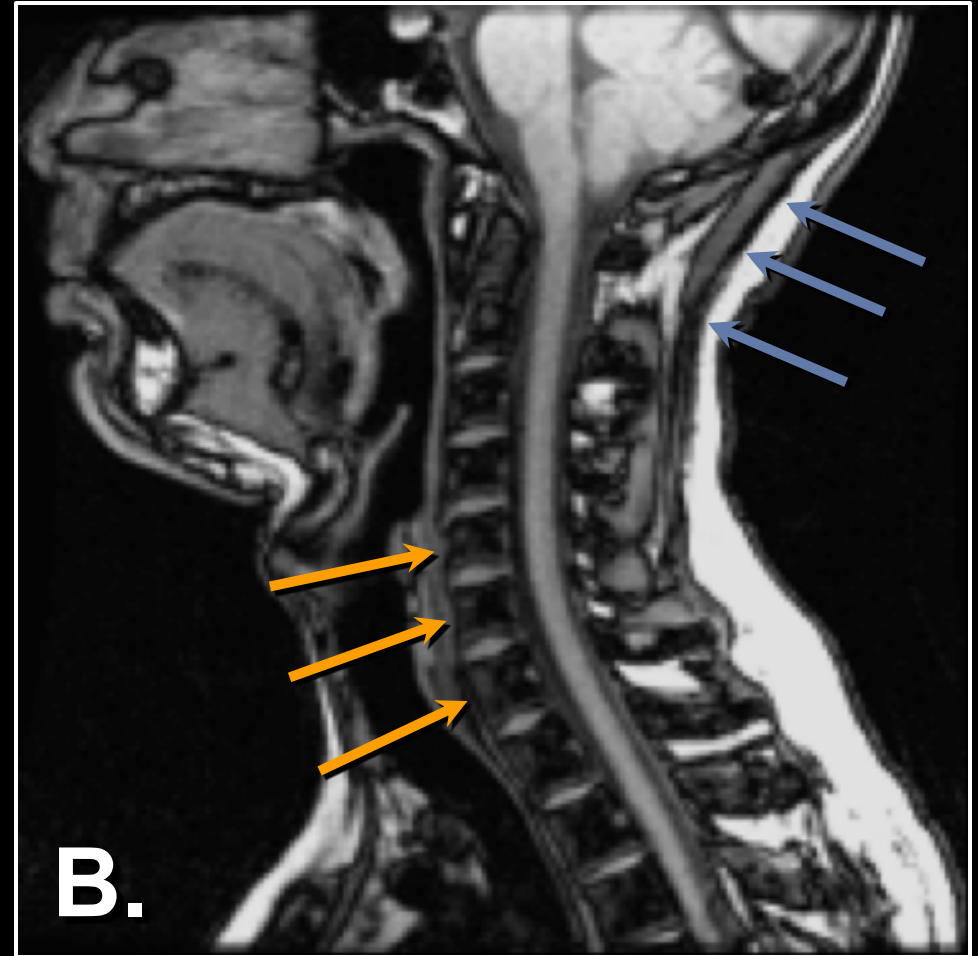


Images Courtesy of Scott Reeder

Which image is the in-phase image?



In-Phase

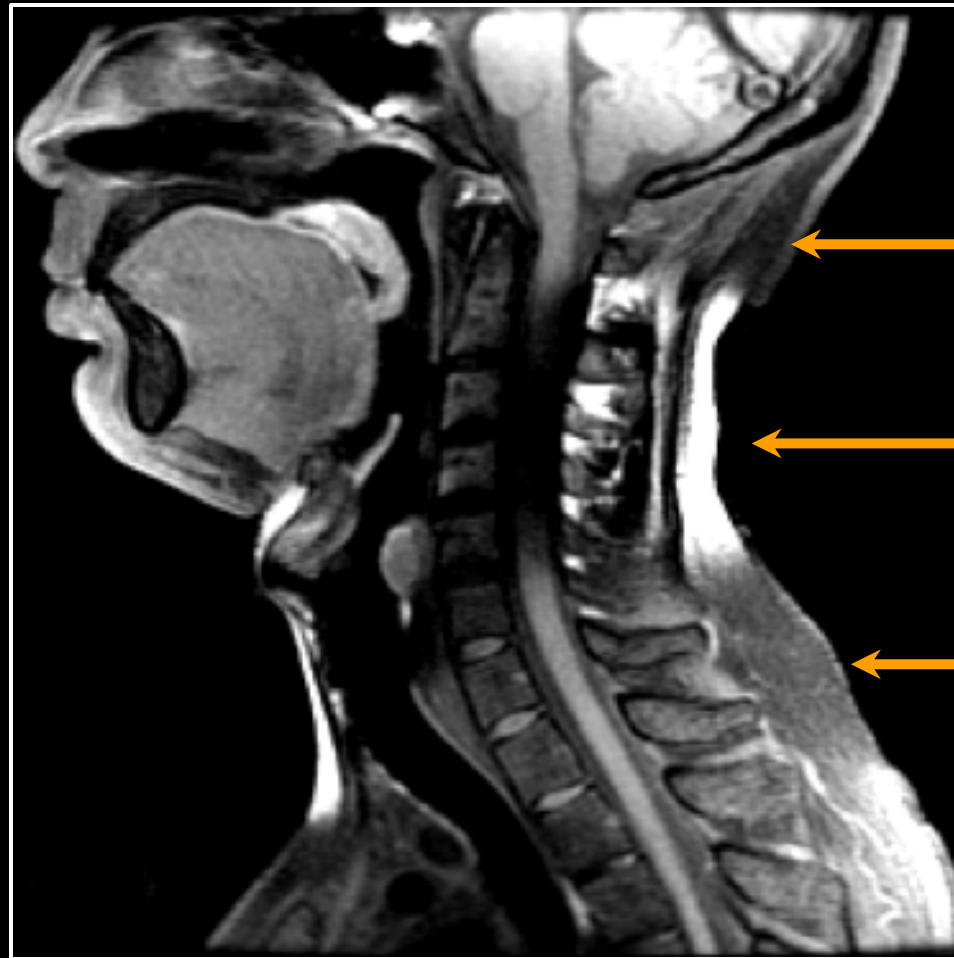


Opposed-Phase

Gradient Echoes & Fat Suppression

- **Why is fat suppression/separation important?**
 - Fat is bright on most pulse sequences.
 - But so are many other things...
 - CSF & edema
 - Flowing blood
 - Contrast enhanced tissues
- **Fat obscures underlying pathology**
 - Edema, neoplasm, inflammation
- **How can fat be eliminated in GRE images?**
 - Fat saturation pulses
 - Multi-echo acquisitions
 - Dixon/IDEAL

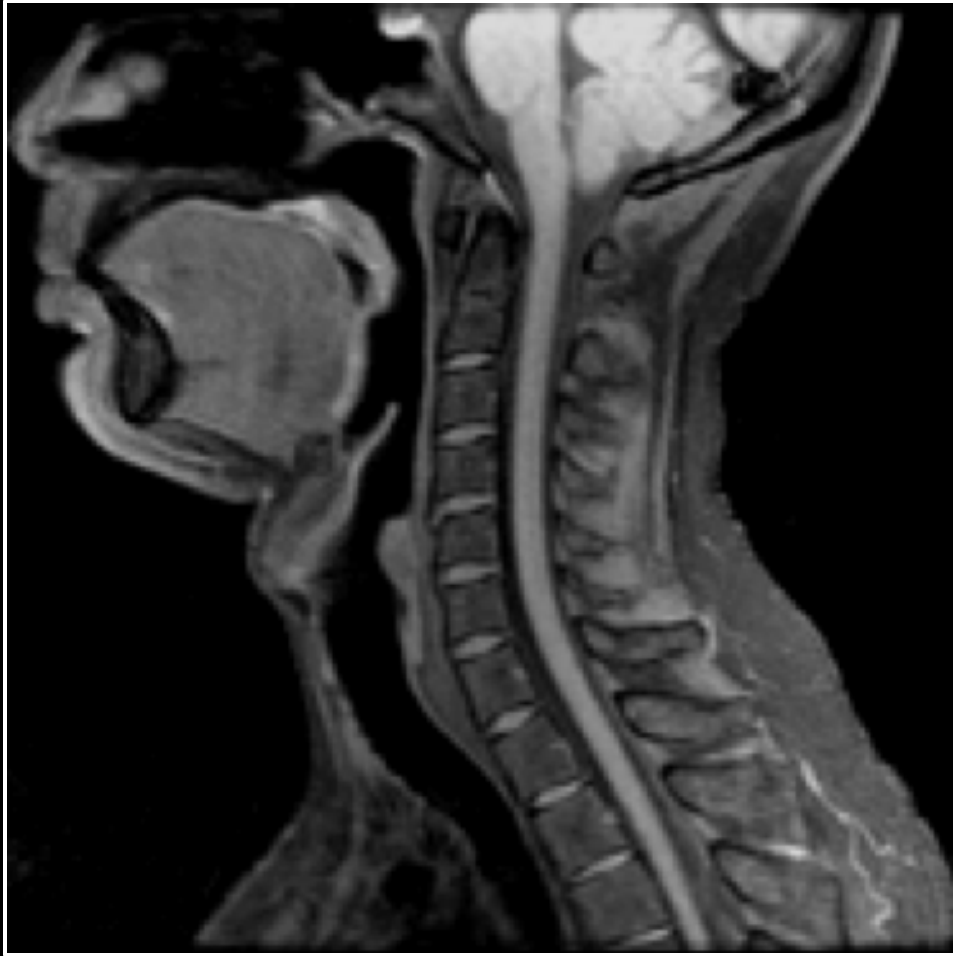
Gradient Echoes & Fat/Water Separation



**Fat-Sat Can
Be Spatially
Non-Uniform**

Fat-Sat Image

Gradient Echoes & Fat/Water Separation



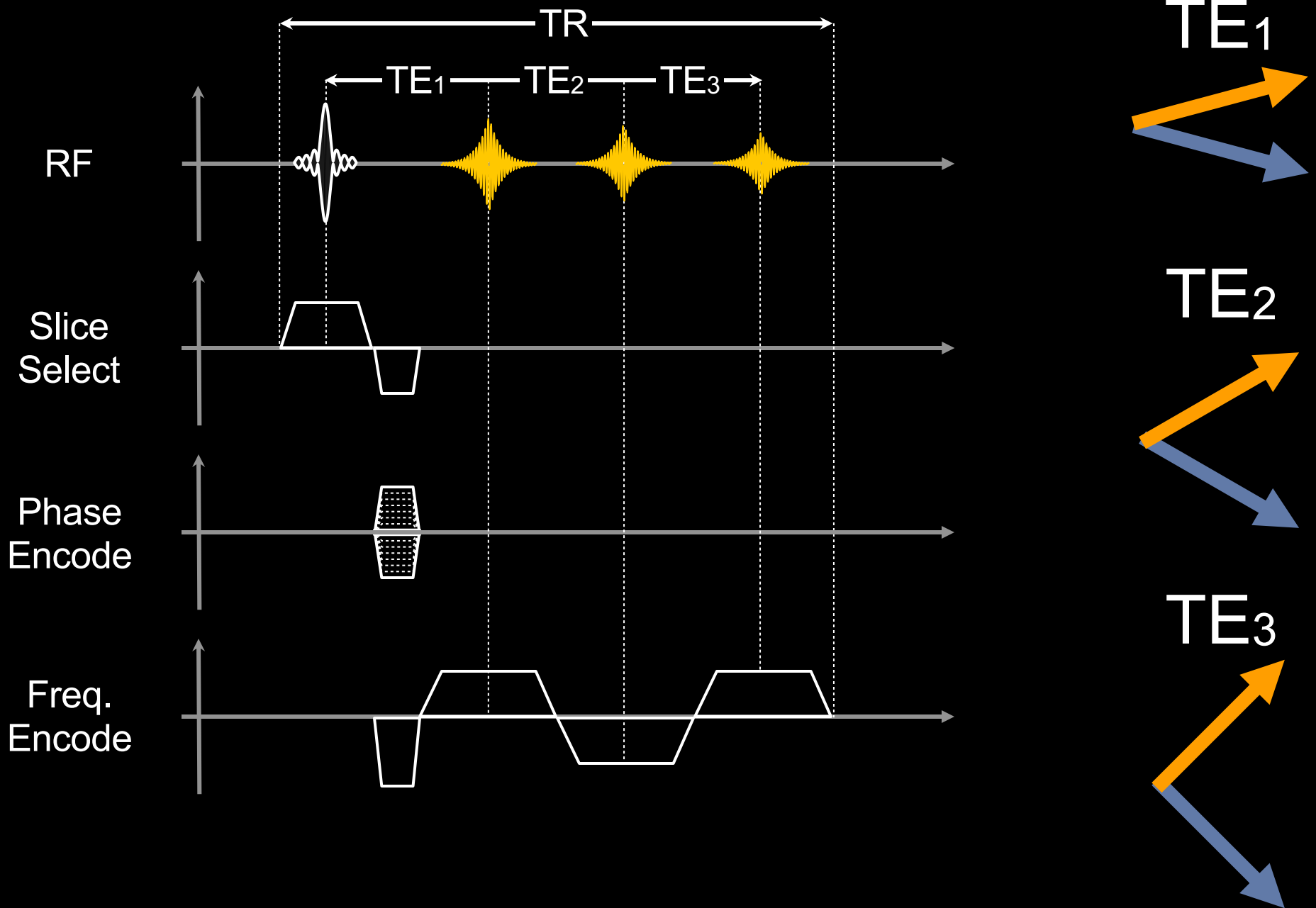
IDEAL Water Image



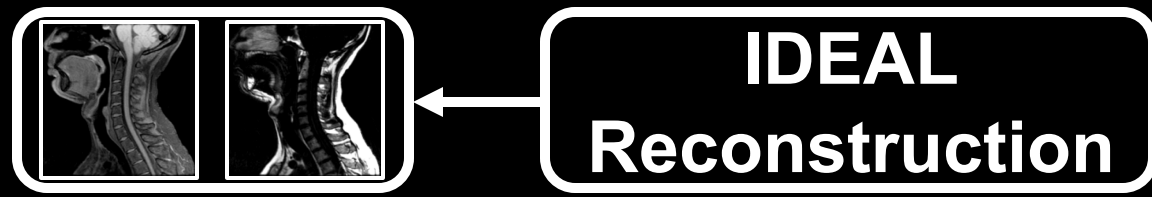
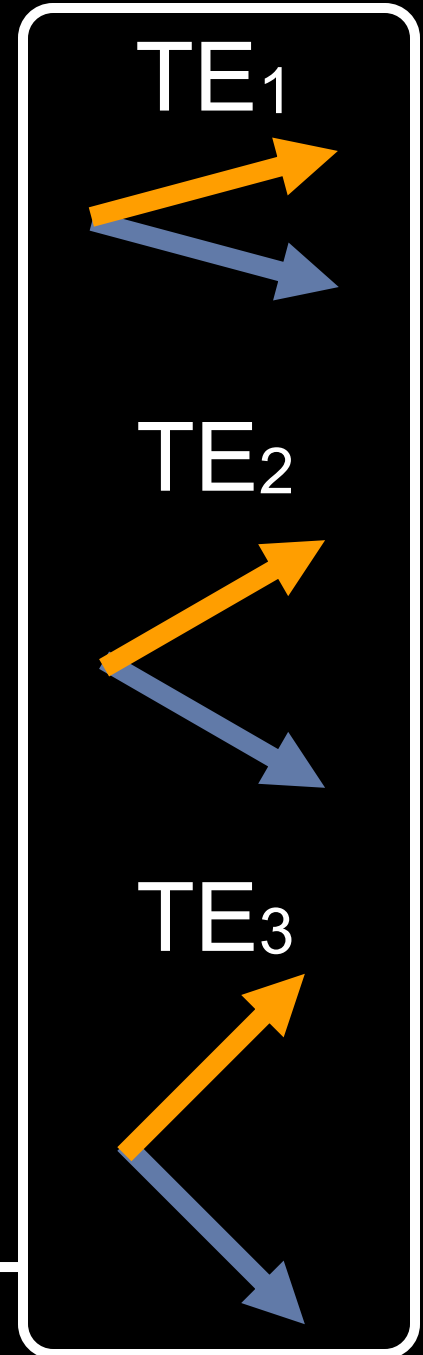
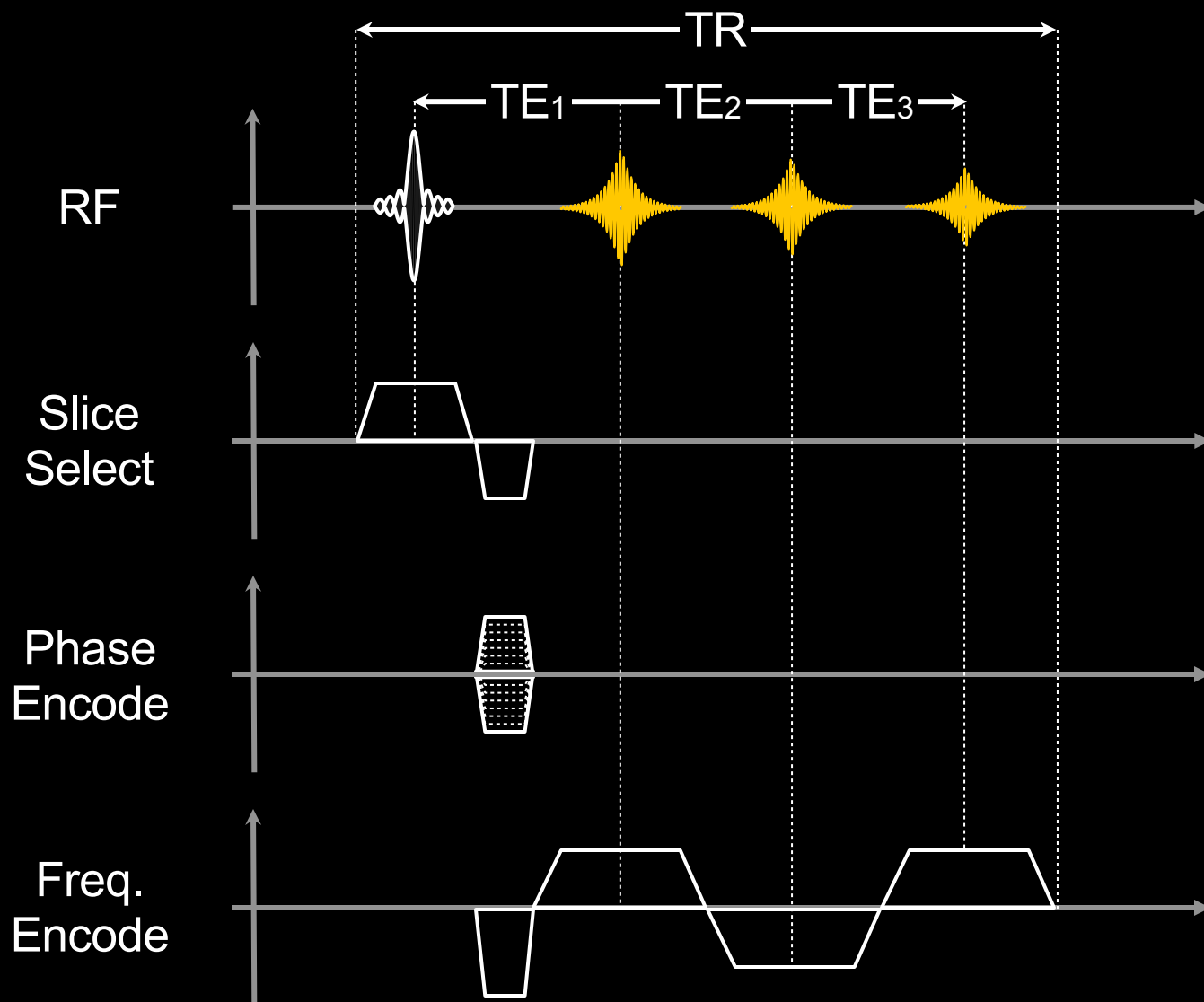
IDEAL Fat Image

Images Courtesy of Scott Reeder

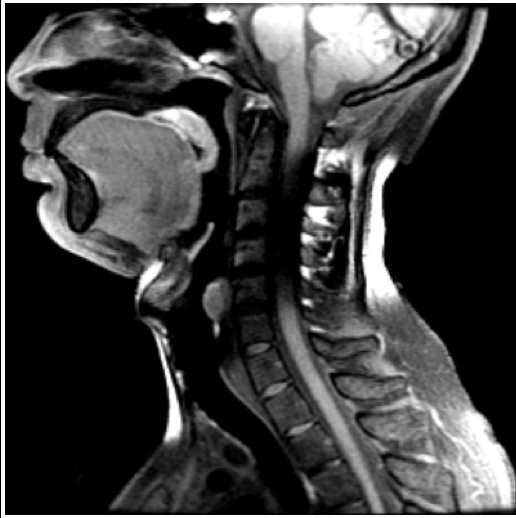
GRE & Fat/Water Separation - How?



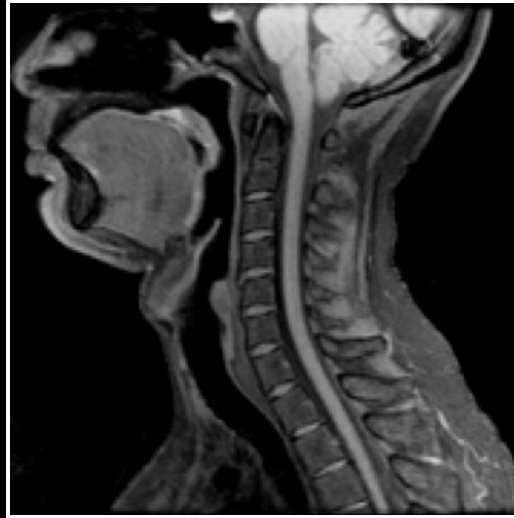
GRE & Fat/Water Separation - How?



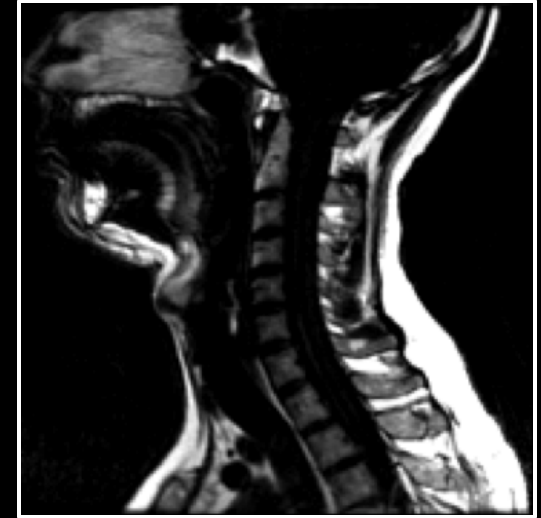
Gradient Echoes & Fat/Water Separation



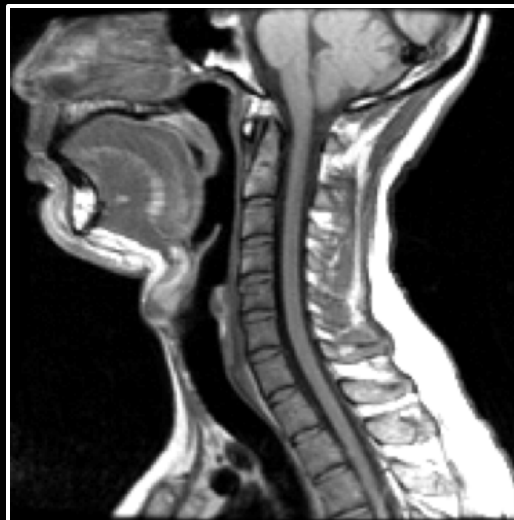
Imperfect Fat Sat



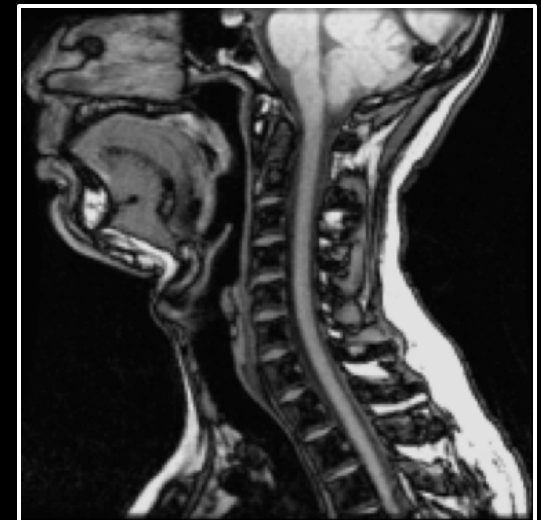
IDEAL water image



IDEAL fat image



in-phase



opposed-phase

Images Courtesy of Dr. Scott Reeder