### **MRI Systems III: Gradients**

### M219 - Principles and Applications of MRI Kyung Sung, Ph.D. 1/27/2025

## **Course Overview**

- 2025 course schedule
  - https://mrrl.ucla.edu/pages/m219\_2025
- Assignments
  - Homework #1 due on 1/29

- TA office hours, Mon 4-6pm
- Office hours, Fri 10-11am

### **Bloch Equations - Lab Frame**



- Precession
  - Magnitude of M unchanged
  - Phase (rotation) of M changes due to B
- Relaxation
  - T<sub>1</sub> changes are slow O(100ms)
  - T<sub>2</sub> changes are fast O(10ms)
  - Magnitude of M can be ZERO





### Free Precession in the Rotating Frame



- No precession
- T<sub>1</sub> and T<sub>2</sub> Relaxation
- Drop the diffusion term
- System or first order, linear, separable ODEs!



The precessional term drops out in the rotating frame.



### Free? Forced? Relaxation?

- We've considered all combinations of:
  - Free and forced precession
  - With and without relaxation
  - Laboratory and rotating frames
- Which one's concern M219 the most?
  - Free precession in the rotating frame with relaxation
  - Forced precession in the rotating frame without relaxation.
- We can, in fact, simulate all of them...









 $T_2^*$  is signal loss from spin dephasing and  $T_2$ 

T2\*<T2 (always!)



### Forced Precession in the Rot. Frame with Relaxation

$$\frac{\partial \vec{M}_{rot}}{\partial t} = \gamma \vec{M}_{rot} \times \vec{B}_{eff} - \frac{M_{x'}\vec{i'} + M_{y'}\vec{j'}}{T_2} - \frac{(M_{z'} - M_0)\vec{k'}}{T_1}$$
$$\vec{B}_{eff} = B_1^e(t)\hat{i'}$$

- B1 induced nutation
- T<sub>1</sub> and T<sub>2</sub> Relaxation

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- Drop the diffusion term
- System or first order, linear, coupled PDEs!
- When does this equation apply?



# Types of RF Pulses

- Excitation Pulses
- Inversion Pulses
- Refocusing Pulses
- Saturation Pulses
- Spectrally Selective Pulses
- Spectral-spatial Pulses
- Adiabatic Pulses

## **Excitation Pulses**

- Tip M<sub>z</sub> into the transverse plane
- Typically 200µs to 5ms
- Non-uniform across slice thickness
  - Imperfect slice profile
- Non-uniform within slice
  - Termed B<sub>1</sub> inhomogeneity
  - Non-uniform signal intensity across FOV

## 90° Excitation Pulse



# **Small Flip Angle Excitation**



## **Inversion Pulses**

- Typically, 180° RF Pulse
  - non-180° that still results in -M<sub>Z</sub>
- Invert M<sub>Z</sub> to -M<sub>Z</sub>
  - Ideally produces no M<sub>XY</sub>
- Hard Pulse
  - Constant RF amplitude
  - Typically non-selective
- Soft (Amplitude Modulated) Pulse
  - Frequency selective
  - Spatially Selective

### **Inversion Pulses**



# **Refocusing Pulses**

- Typically, 180° RF Pulse
  - Provides optimally refocused M<sub>XY</sub>
  - Largest spin echo signal
- non-180°
  - Partial refocusing
  - Lower SAR
  - Multiple non-180° produce stimulated echoes
- Refocus spin dephasing due to
  - imaging gradients
  - local magnetic field inhomogeneity
  - magnetic susceptibility variation
  - chemical shift

# **Refocusing Pulses**



### Gradient Fields & Spins

Gradients are a special kind of inhomogeneous field whose *z*-component varies linearly along a specific direction called the gradient direction.

$$(\overrightarrow{G} \cdot \overrightarrow{r}) \ \hat{k} = (G_x \cdot x + G_y \cdot y + G_z \cdot z) \ \hat{k}$$
$$\overrightarrow{B}(\overrightarrow{r}, t) = (B_0 + \overrightarrow{G}(t) \cdot \overrightarrow{r}) \ \hat{k}$$
$$B_G(\overrightarrow{r}, t)$$

• Each gradient coil can be activated independently and simultaneously







The magnetic field at a position depends on the magnitude of the applied gradient.















 $B_0$ 

 $B_0$ 

lici a

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 $B_0 - \delta B_0$ 



What coordinate frame are we in?





















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**Possible Slice** 

### X+Z-Gradients



### Spin Isochromat









Simultaneous gradients create an arbitrary isochromat plane.

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### How do we measure M<sub>xy</sub>?

### Faraday's Law of Induction



Precessing spins induce a current in a nearby coil.



The trick is to encode spatial information and image contrast in the echo.

### **Basic Detection Principles**

Magnetic Flux Through The Coil – Reciprocity

$$\Phi(t) = \int_{object} \vec{B}_r(\vec{r}) \cdot \vec{M}(\vec{r}, t) d\vec{r}$$

$$\uparrow \qquad \uparrow \qquad \uparrow \qquad \uparrow \qquad f_{agnetic} \qquad$$

### What happens if the coil has poor sensitivity?

What happens if the coil's sensitivity is perpendicular to the bulk magnetization? How would that happen?

### **Basic Detection Principles**

We get here

$$S(t) = \int_{\text{object}} M_{xy}(r, 0) e^{-i\gamma \Delta B(r)t} dr$$

From Here

$$V\left(t\right) = -\frac{\partial \Phi\left(t\right)}{\partial t} = -\frac{\partial}{\partial t} \int_{object} \vec{B}\left(\vec{r}\right) \cdot \vec{M}\left(\vec{r},t\right) d\vec{r}$$

### with 25 pages of Math!

# Basic Detection Principles $S(t) = \int_{\text{object}} M_{xy}(r, 0) e^{-i\gamma \Delta B(r)t} dr$

**Observations** 

Detected signal is the vector sum of all transverse magnetizations in the "rotating frame" within the imaging volume.

The Larmor frequency precession (Lab frame rotation) is necessary for detection, although only the baseband signal matters for imaging

To the Board

Y-Gradient





http://www.magnet.fsu.edu







![](_page_36_Picture_3.jpeg)

![](_page_36_Picture_4.jpeg)

![](_page_37_Picture_1.jpeg)

![](_page_37_Picture_2.jpeg)

![](_page_37_Picture_3.jpeg)

![](_page_37_Picture_4.jpeg)

![](_page_37_Picture_5.jpeg)

![](_page_38_Picture_1.jpeg)

![](_page_38_Picture_2.jpeg)

![](_page_38_Picture_3.jpeg)

- Primary function
  - Encode spatial information
    - Slice selection
    - Phase encoding
    - Frequency encoding
- Secondary functions
  - Sensitize/de-sensitize images to motion
  - Minimize artifacts (crushers & spoilers)
  - Magnetization re-phasing in slice selection
  - Magnetization de-phasing during readout

![](_page_39_Picture_11.jpeg)

![](_page_39_Picture_12.jpeg)

- Gradients are a:
  - Small
    - <5G/cm (<0.0075T @ edge of 30cm FOV)</li>
  - Spatially varying
    - Linear gradients
    - Adds to B<sub>0</sub> only in Z-direction
  - Time varying
    - Slewrate Max. ~150-200mT/m/ms
  - Magnetic field
    - Adds/Subtracts to the B<sub>0</sub> field
  - Parallel to B<sub>0</sub>
- Gradients are NOT:
  - Fields perpendicular to B<sub>0</sub>

![](_page_40_Picture_15.jpeg)

![](_page_41_Figure_1.jpeg)

#### Gradients are "linear" over ~40-50cm on each axis.

![](_page_41_Picture_3.jpeg)

![](_page_41_Picture_4.jpeg)

## **B-Field Assumptions in MRI**

- B<sub>0</sub>-field is:
  - Perfectly uniform over space.
    - "B<sub>0</sub> homogeneity"
  - Perfectly stable with time.
- B<sub>1</sub>-field is:
  - Perfectly uniform over space.
    - "B<sub>1</sub> homogeneity"
  - Temporally modulated exactly as specified.
- Gradient Fields are:
  - Perfectly linear over space.
    - "Gradient linearity"
  - Temporally modulated exactly as specified

![](_page_42_Picture_13.jpeg)

### Imperfections of Gradient Fields

- Gradient coils aren't perfect
  - Non-linearity
  - Eddy Currents
  - Maxwell terms (Concomitant fields)
  - But they are small
    - <u>Much</u> smaller than B<sub>0</sub>
    - We will ignore them...but they exist...

![](_page_43_Picture_8.jpeg)

![](_page_43_Picture_9.jpeg)

![](_page_45_Figure_1.jpeg)

Ideally spatial position is linearly related to frequency.

![](_page_45_Picture_3.jpeg)

![](_page_45_Picture_4.jpeg)

- Basic <u>assumption</u> in MRI is that the zcomponent of the B-field created by the gradient coils varies <u>linearly</u> with x, y, or z over the FOV.
- Higher gradient amplitudes and slewrates can be achieved by compromising on spatial linearity.
- Gradient non-linearity causes geometric and intensity distortions.

![](_page_46_Picture_4.jpeg)

![](_page_46_Picture_5.jpeg)

![](_page_47_Picture_1.jpeg)

![](_page_47_Picture_2.jpeg)

![](_page_47_Figure_3.jpeg)

![](_page_47_Picture_4.jpeg)

Image Courtesy of M.T. Alley & B.A. Hargeaves

![](_page_47_Picture_6.jpeg)

## Solution

- Improve hardware and linearity!
- Pay attention to FOV!
- Image warping parameters that are system specific and applied to all images.
  - Works well qualitatively.
  - Can be problematic quantitatively.

![](_page_48_Picture_6.jpeg)

**Gradient Safety** 

## **Gradient Safety**

- Noise
- **Peripheral nerve** stimulation (PNS)

![](_page_50_Picture_3.jpeg)

![](_page_50_Figure_4.jpeg)

Solution: De-rate gradient slew rates, but this increases scan time.

Solution:

![](_page_50_Picture_7.jpeg)

Ear plugs

Head phones

### Time-varying gradients induce mechanical vibrations and PNS.

![](_page_50_Picture_11.jpeg)

![](_page_50_Picture_12.jpeg)

![](_page_50_Picture_13.jpeg)

### **MRI Gradient Noise**

![](_page_51_Picture_1.jpeg)

![](_page_51_Picture_2.jpeg)

Switching the gradients on ms time scales (kHz) generates acoustic noise.

![](_page_51_Picture_4.jpeg)

## **Gradient Noise**

- Jet take-off @ 25m
- Car horn @ 1m
- Live rock band
- MRI gradients full load
- Garbage disposal
- MRI gradients basic load ≤75 dB
- Radio or TV Audio

~150 dB (eardrum rupture) ~110 dB (borderline painful) ~100 dB

<mark>≤99 dB</mark> ~80 dB

~70dB

![](_page_52_Picture_10.jpeg)

![](_page_52_Picture_12.jpeg)

### Gradient Safety – GMax

- G<sub>max</sub> limitations:
  - Concern: None known.
    - B<sub>0</sub> is already pretty big.
  - Conventional Gradients
    - G<sub>Max</sub> = 4 to 5G/cm (=50mT/m)
  - Cutting Edge Gradients
    - G<sub>Max</sub> = 8G/cm (=80mT/m)
  - Connectome Gradients
    - G<sub>Max</sub> = 30G/cm (=300mT/m)
  - Consider the  $\Delta B$  contributed by a gradient...

![](_page_53_Figure_11.jpeg)

### **Gradient Slewrate**

- Gradient slew rate
  - T/m/s (or G/cm/s)
  - dG/dt Rate of change of gradient amplitude
- Slew rate limited by dB/dt:
  - Concern: Peripheral Nerve Stimulation
  - Regulated by FDA
  - Normal Mode: dB/dt=16 T/s•(1+0.36/ß)
  - First Level Mode: dB/dt=20 T/s•(1+0.36/ß)
  - ß=stimulus duration [ms]

![](_page_54_Figure_10.jpeg)

Δt

![](_page_54_Picture_11.jpeg)

![](_page_55_Picture_0.jpeg)

- Related reading materials
  - Nishimura Chap 5

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