

Imaging Principles

M219 - Principles and Applications of MRI

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1/31/2024

Course Overview

- 2024 course schedule
 - https://mrrl.ucla.edu/pages/m219_2024
- Assignments
 - Homework #2 is due on 2/14
- TA office hours, Weds 4-6pm
- Office hours, Fridays 10-12pm

Combined B_0 and Gradient Fields

- Gradients contribute to the net B-field, but only along the z-direction

$$(\vec{G} \cdot \vec{r}) \hat{k} = (G_x \cdot x + G_y \cdot y + G_z \cdot z) \hat{k}$$

$$\vec{B}(\vec{r}, t) = (B_0 + \vec{G}(t) \cdot \vec{r}) \hat{k}$$

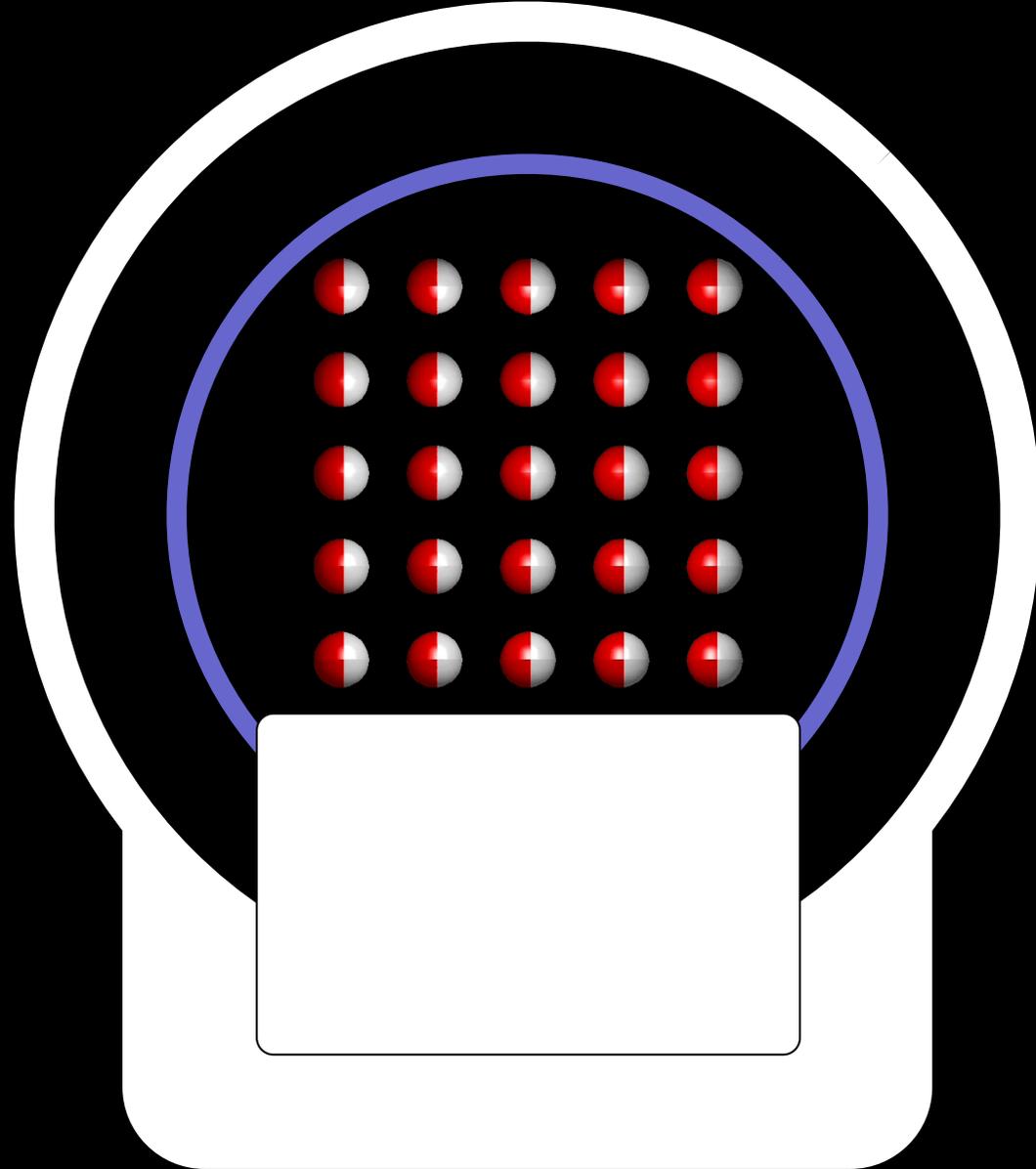
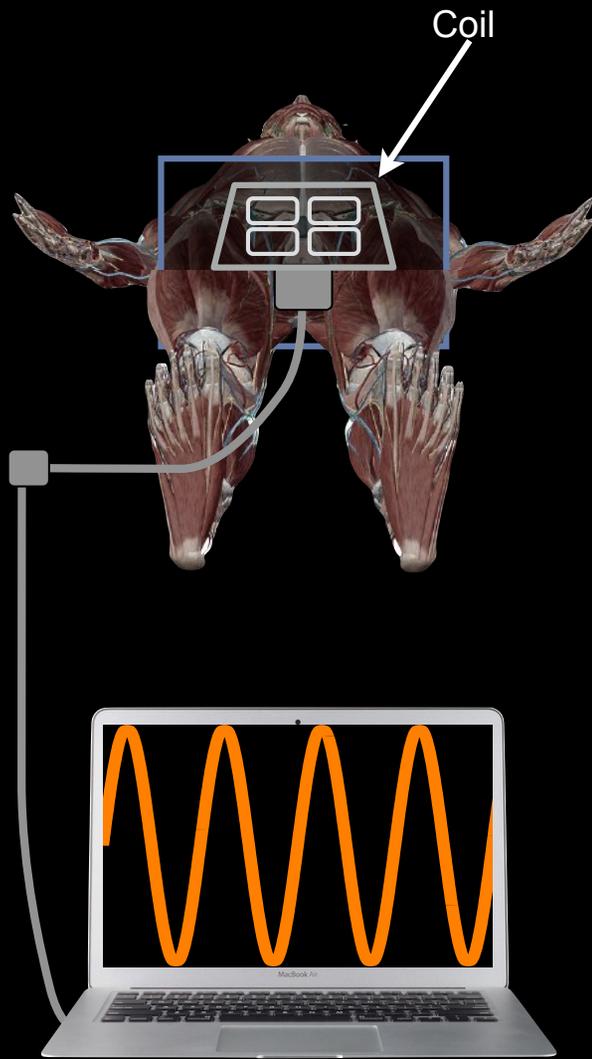
- Each gradient coil can be activated independently and simultaneously

B-Field Assumptions in MRI

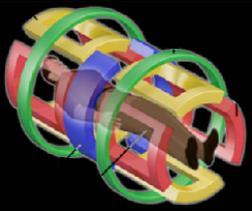
- **B_0 -field is:**
 - Perfectly uniform over space.
 - “ B_0 homogeneity”
 - Perfectly stable with time.
- **B_1 -field is:**
 - Perfectly uniform over space.
 - “ B_1 homogeneity”
 - Temporally modulated exactly as specified.
- **Gradient Fields are:**
 - Perfectly linear over space.
 - “Gradient linearity”
 - Temporally modulated exactly as specified

How do we measure M_{xy} ?

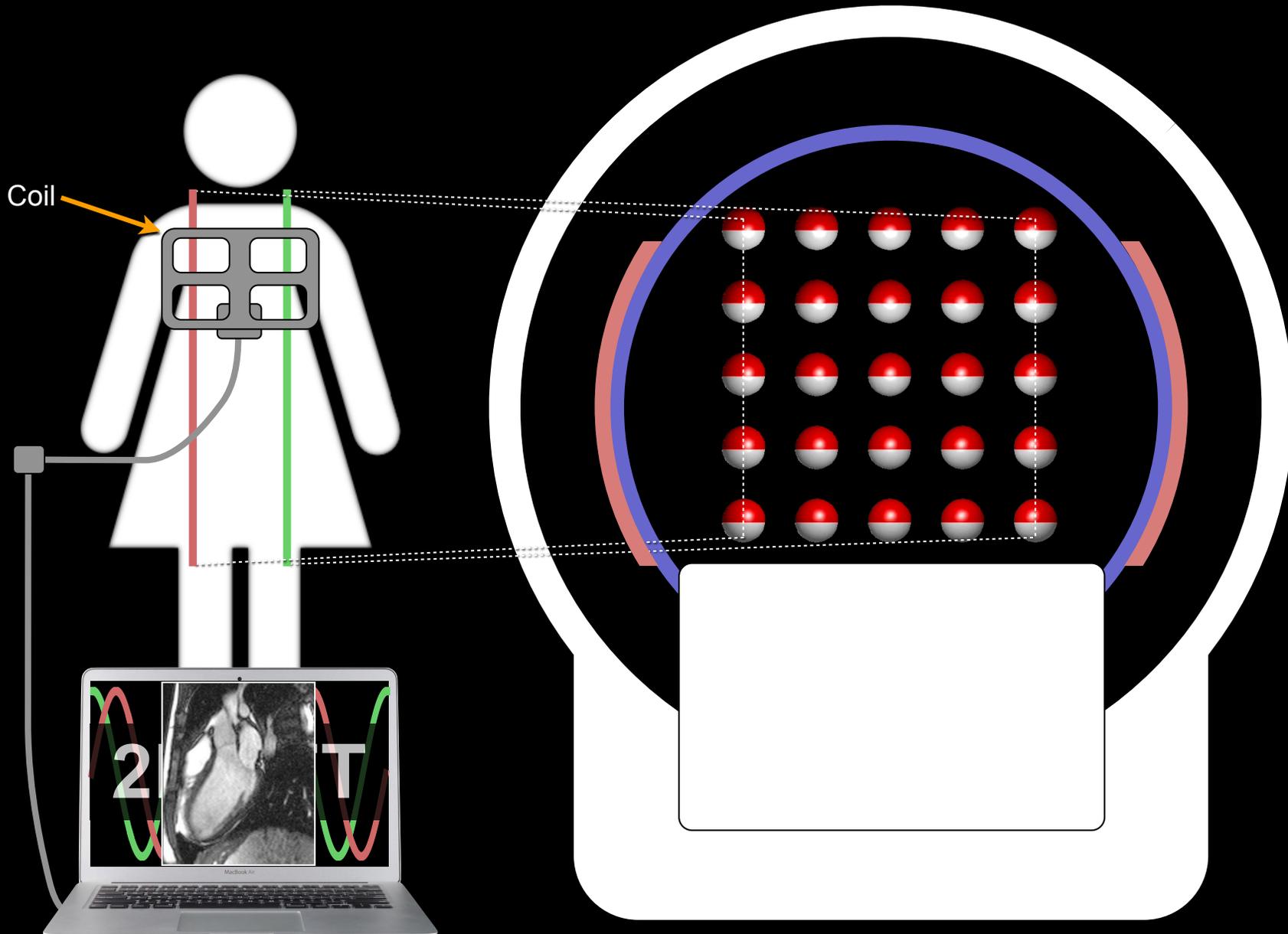
Faraday's Law of Induction



Precessing spins *induce* a current in a nearby coil.



Faraday's Law of Induction



The trick is to encode spatial information and image contrast in the echo.

Basic Detection Principles

Magnetic Flux Through The Coil – *Reciprocity*

$$\Phi(t) = \int_{object} \vec{B}_r(\vec{r}) \cdot \vec{M}(\vec{r}, t) d\vec{r}$$

↑
Magnetic
Flux

↑
Coil
Sensitivity

↑
Bulk
Magnetization

Eqn. 5.38

What happens if the coil has poor sensitivity?

What happens if the coil's sensitivity is perpendicular to the bulk magnetization? How would that happen?

Basic Detection Principles

We get here

$$S(t) = \int_{\text{object}} M_{xy}(\mathbf{r}, 0) e^{-i\gamma \Delta B(\mathbf{r})t} d\mathbf{r}$$

From Here

$$V(t) = -\frac{\partial \Phi(t)}{\partial t} = -\frac{\partial}{\partial t} \int_{\text{object}} \vec{B}(\vec{r}) \cdot \vec{M}(\vec{r}, t) d\vec{r}$$

with 25 pages of Math!

Basic Detection Principles

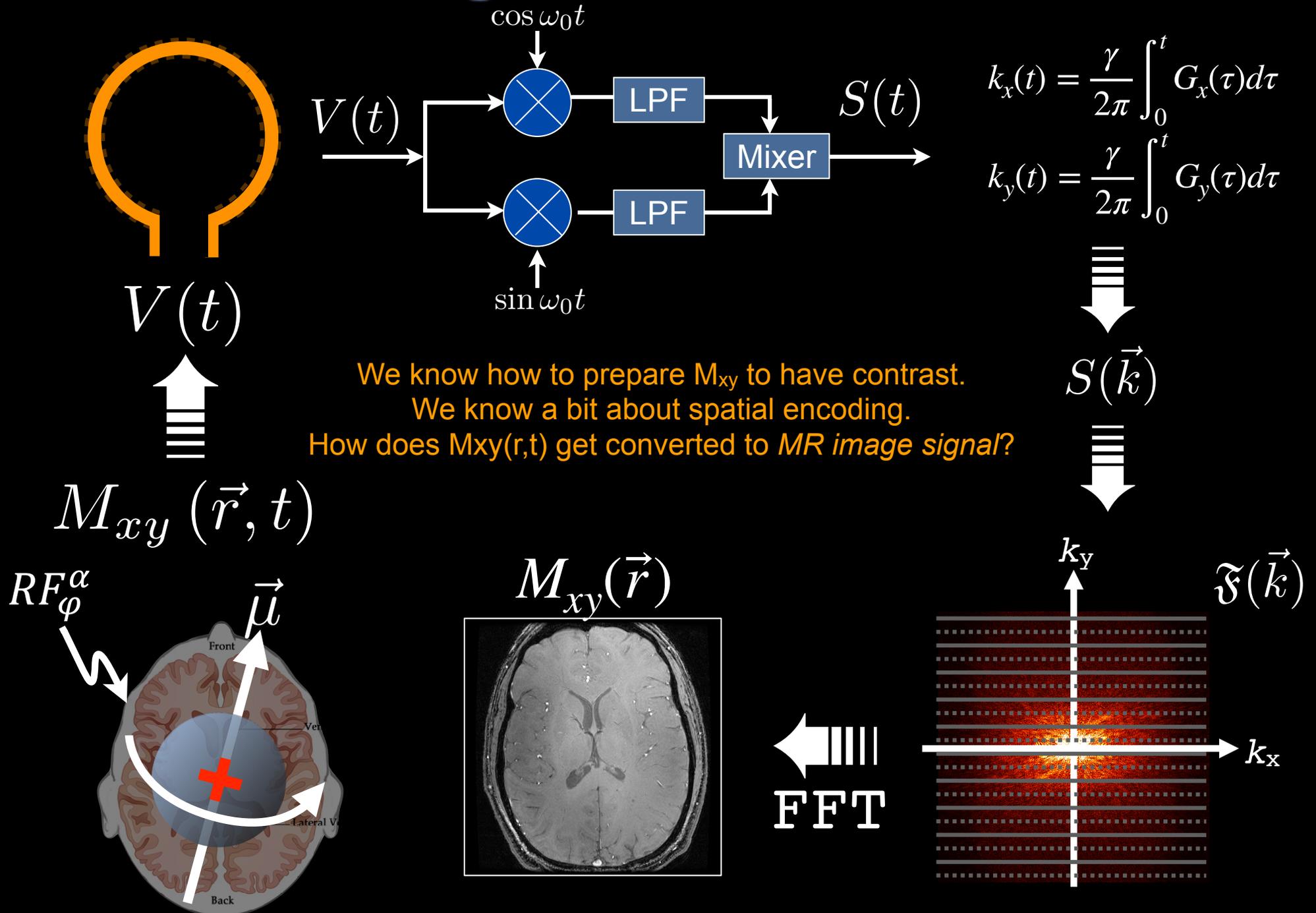
$$S(t) = \int_{\text{object}} M_{xy}(\mathbf{r}, 0) e^{-i\gamma\Delta B(\mathbf{r})t} d\mathbf{r}$$

Observations

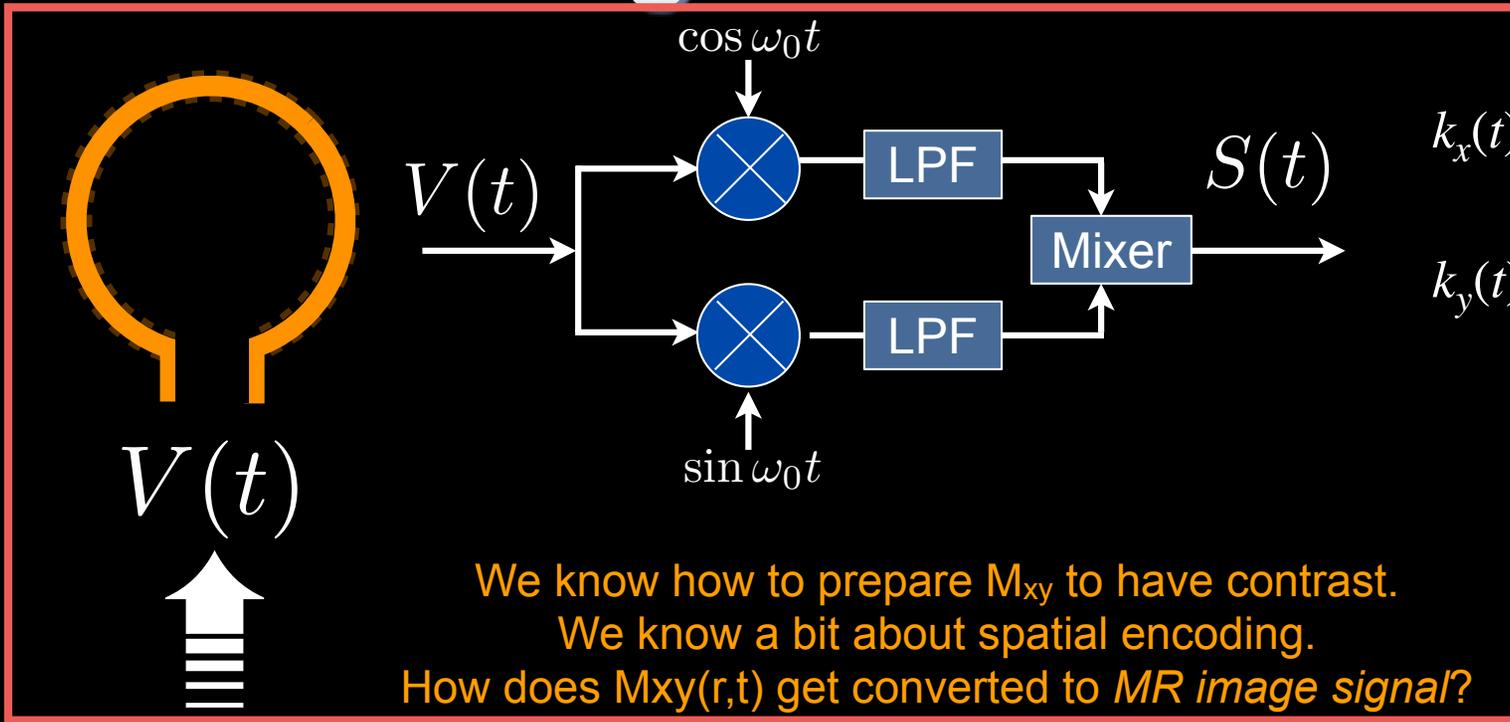
Detected signal is the vector sum of all transverse magnetizations in the “rotating frame” within the imaging volume.

The Larmor frequency precession (Lab frame rotation) is necessary for detection, although only the baseband signal matters for imaging

Signals in MRI

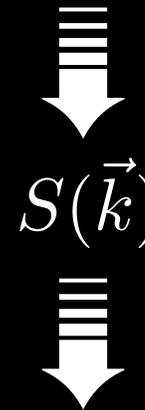


Signals in MRI



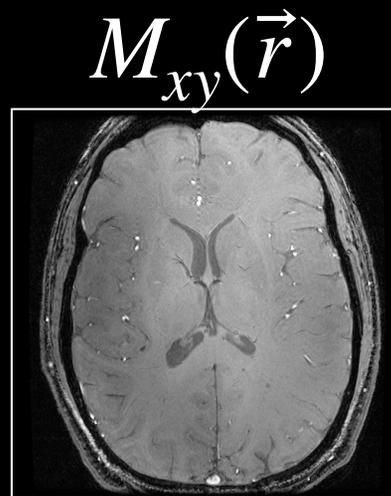
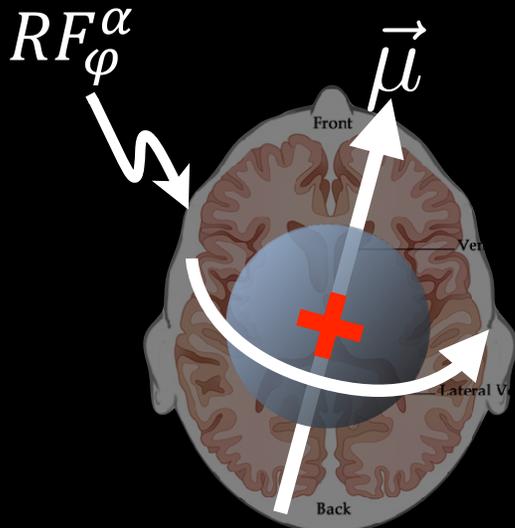
$$k_x(t) = \frac{\gamma}{2\pi} \int_0^t G_x(\tau) d\tau$$

$$k_y(t) = \frac{\gamma}{2\pi} \int_0^t G_y(\tau) d\tau$$

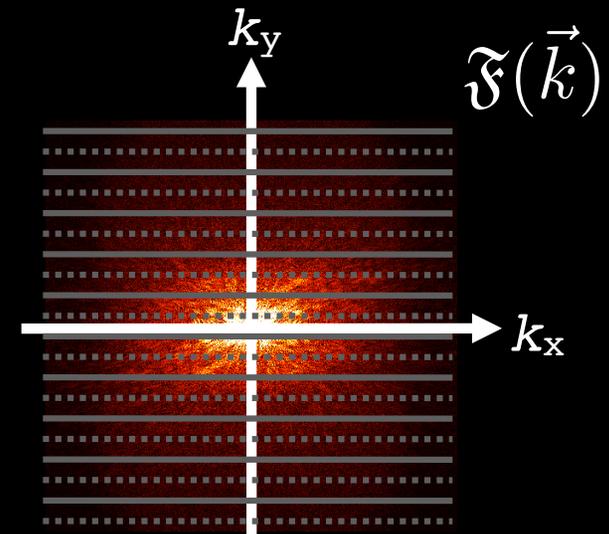


$$S(\vec{k})$$

$$M_{xy}(\vec{r}, t)$$



FFT



To the Board

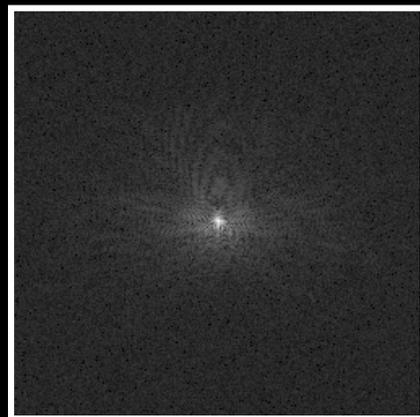
MR Signal Equation

$$s(t) = \int_x \int_y M(x, y) e^{-i2\pi(k_x(t) \cdot x + k_y(t) \cdot y)} dx dy$$

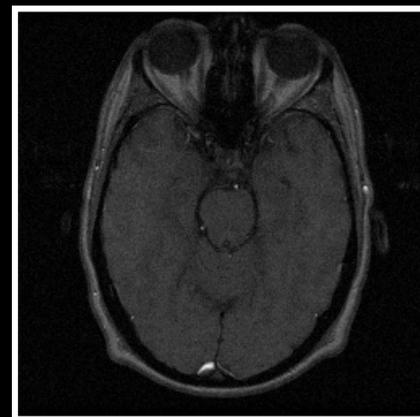
$$k_x(t) = \frac{\gamma}{2\pi} \int_0^t G_x(\tau) d\tau \quad k_y(t) = \frac{\gamma}{2\pi} \int_0^t G_y(\tau) d\tau$$

$$s(t) = m(k_x(t), k_y(t))$$

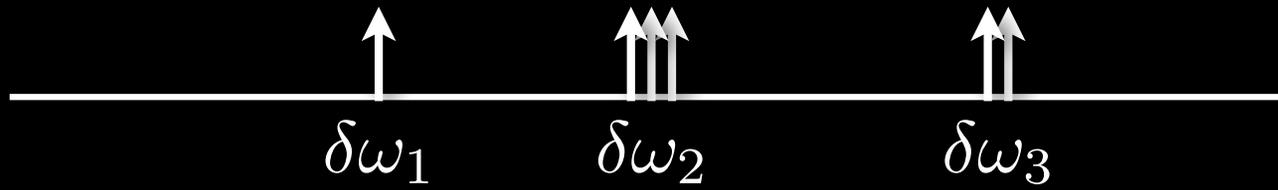
$$m = \mathcal{FT}(M(x, y))$$



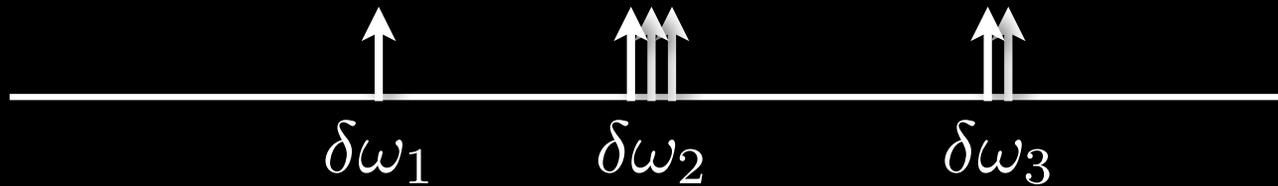
FT
↔



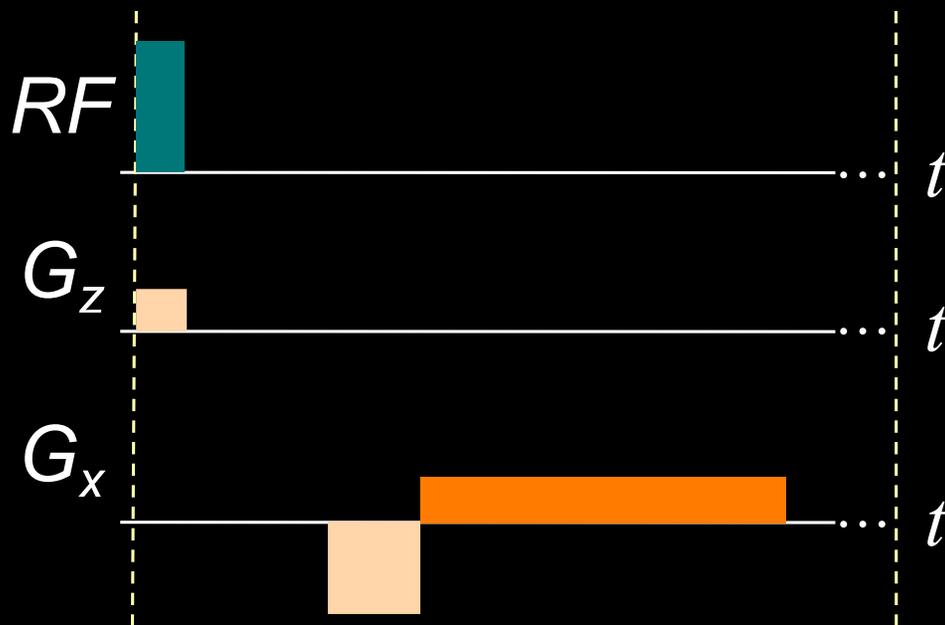
1D Imaging



1D Imaging



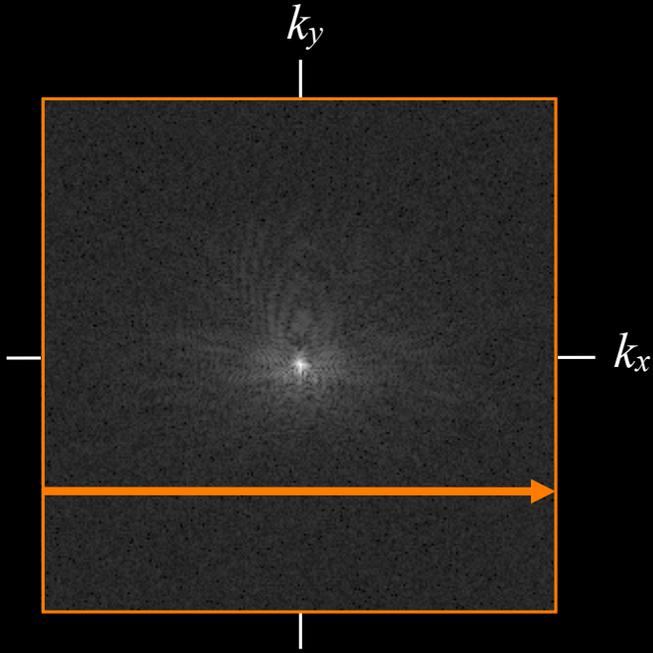
Pulse Sequence Diagram



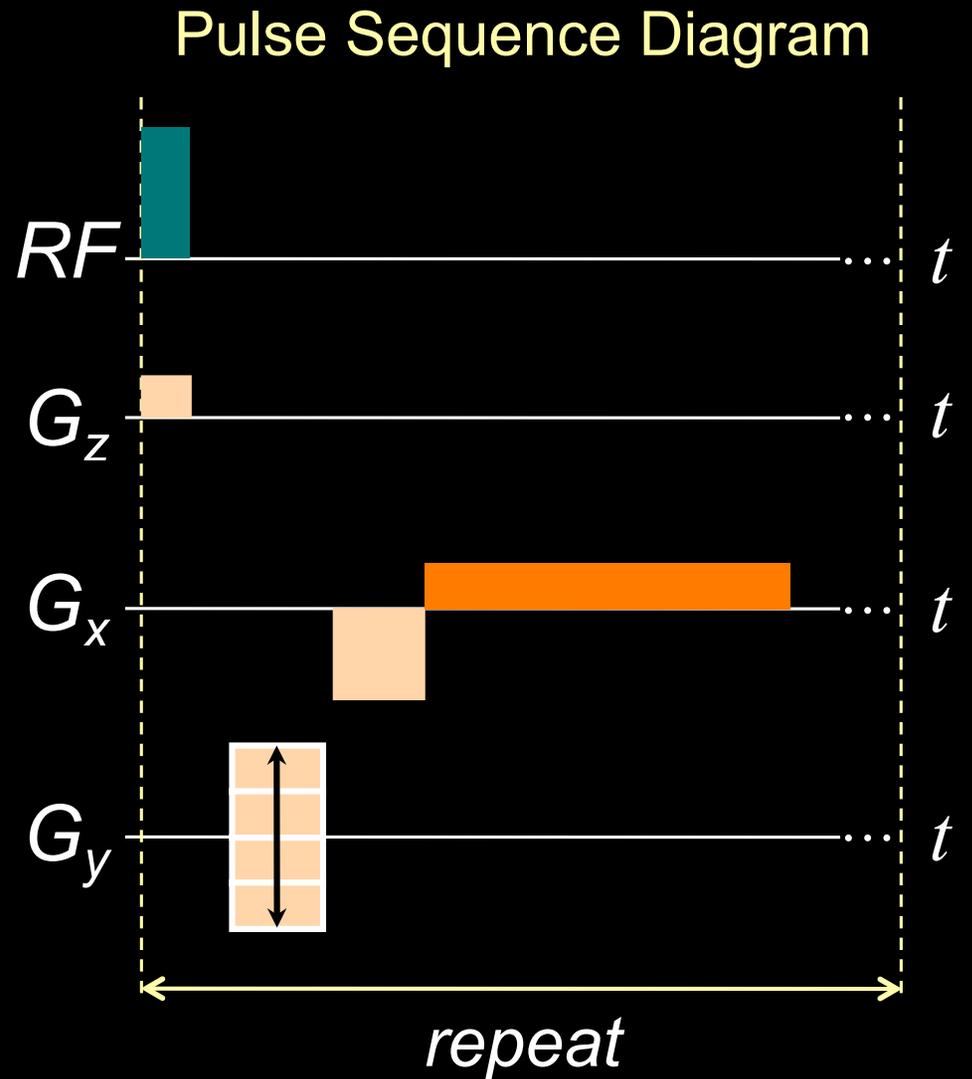
$$s(t) = m(k_x(t))$$



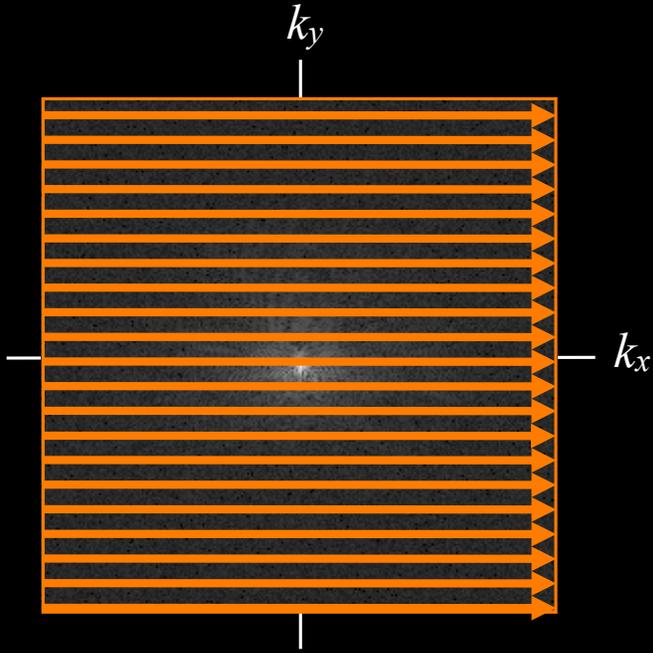
2D Imaging



$$s(t) = m(k_x(t), k_y(t))$$

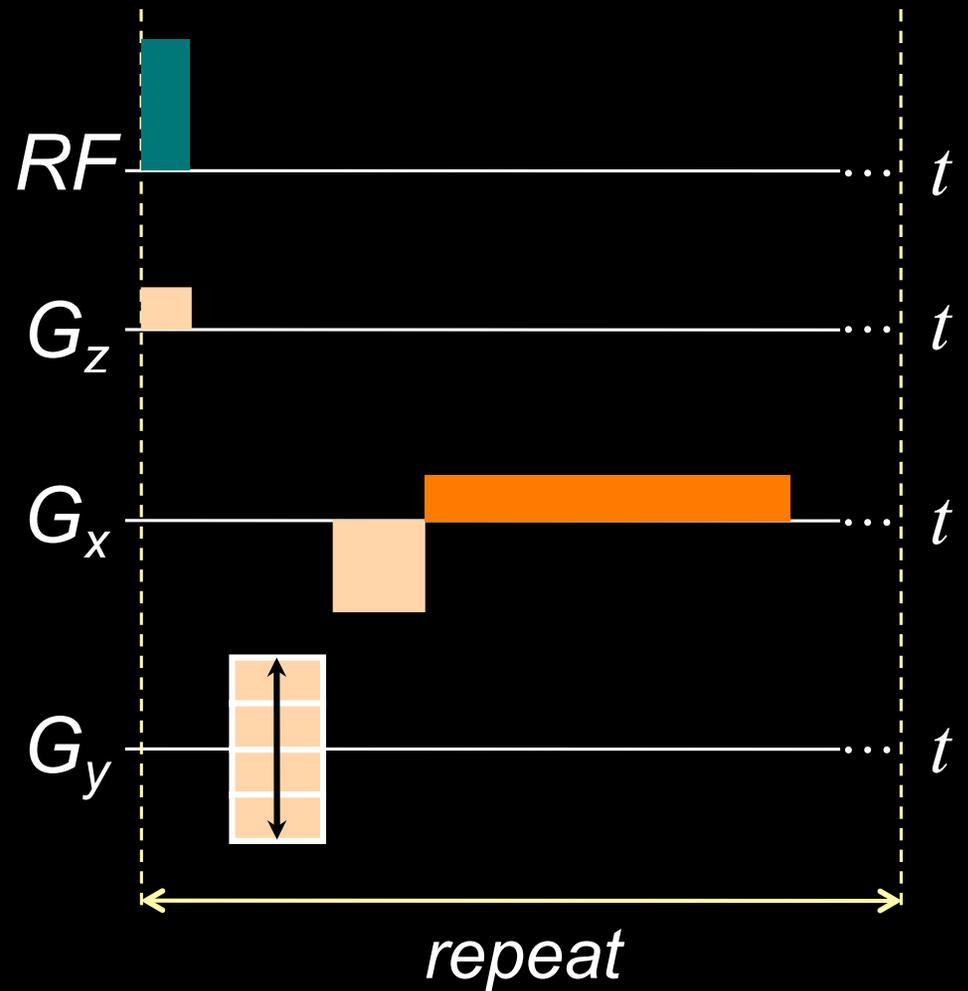


2D Imaging

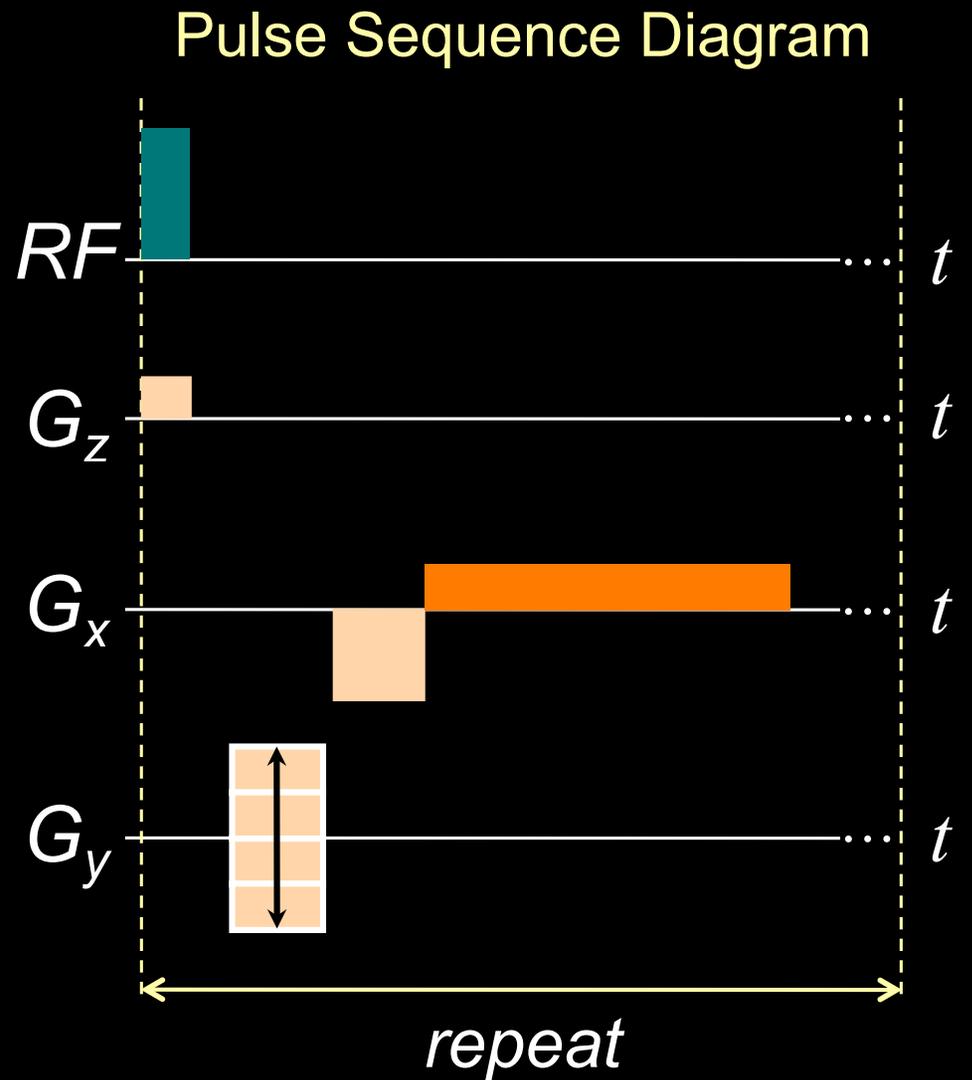
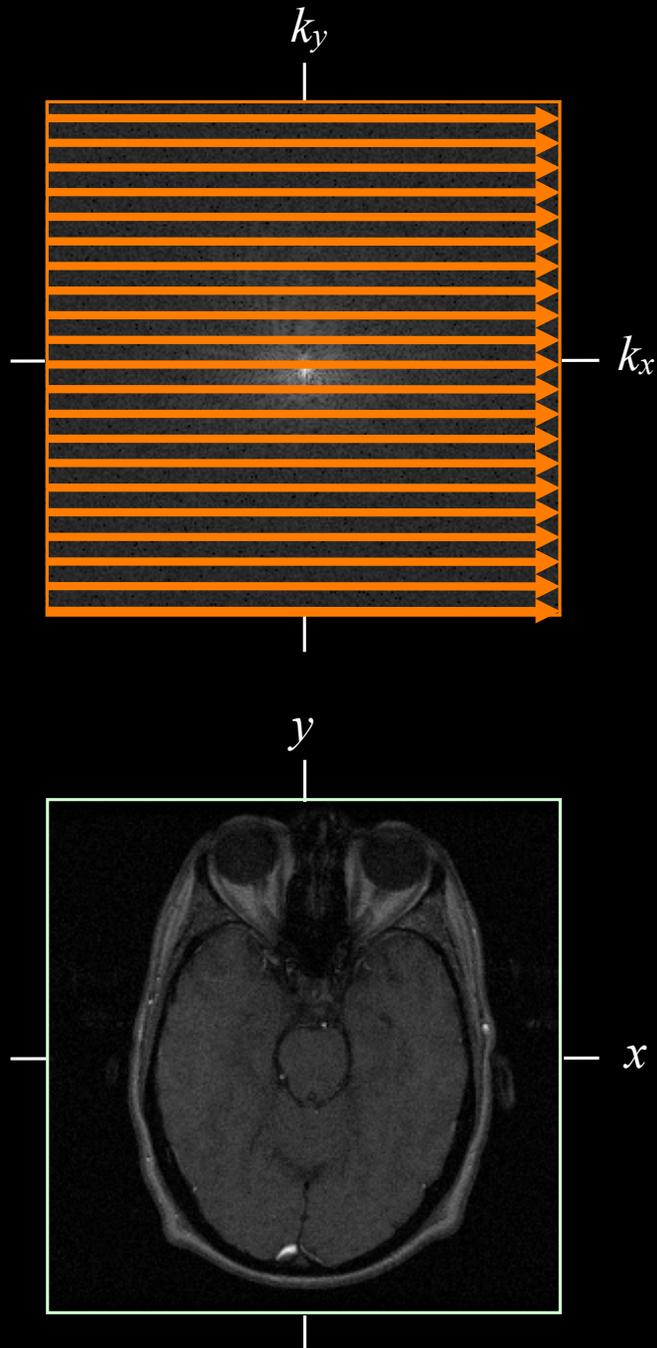


$$s(t) = m(k_x(t), k_y(t))$$

Pulse Sequence Diagram

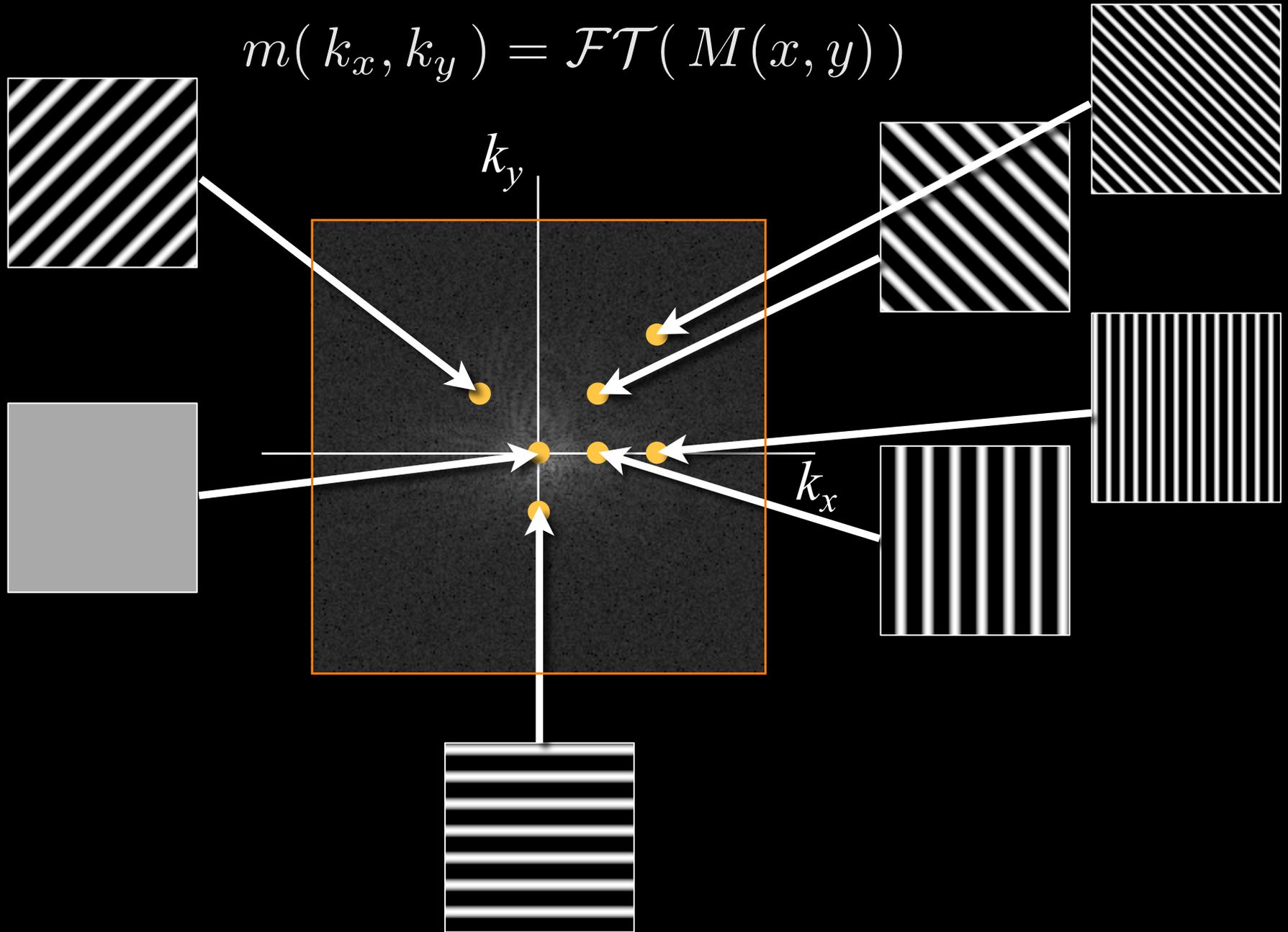


2D Imaging



2D k-Space: MRI Data

$$m(k_x, k_y) = \mathcal{FT}(M(x, y))$$

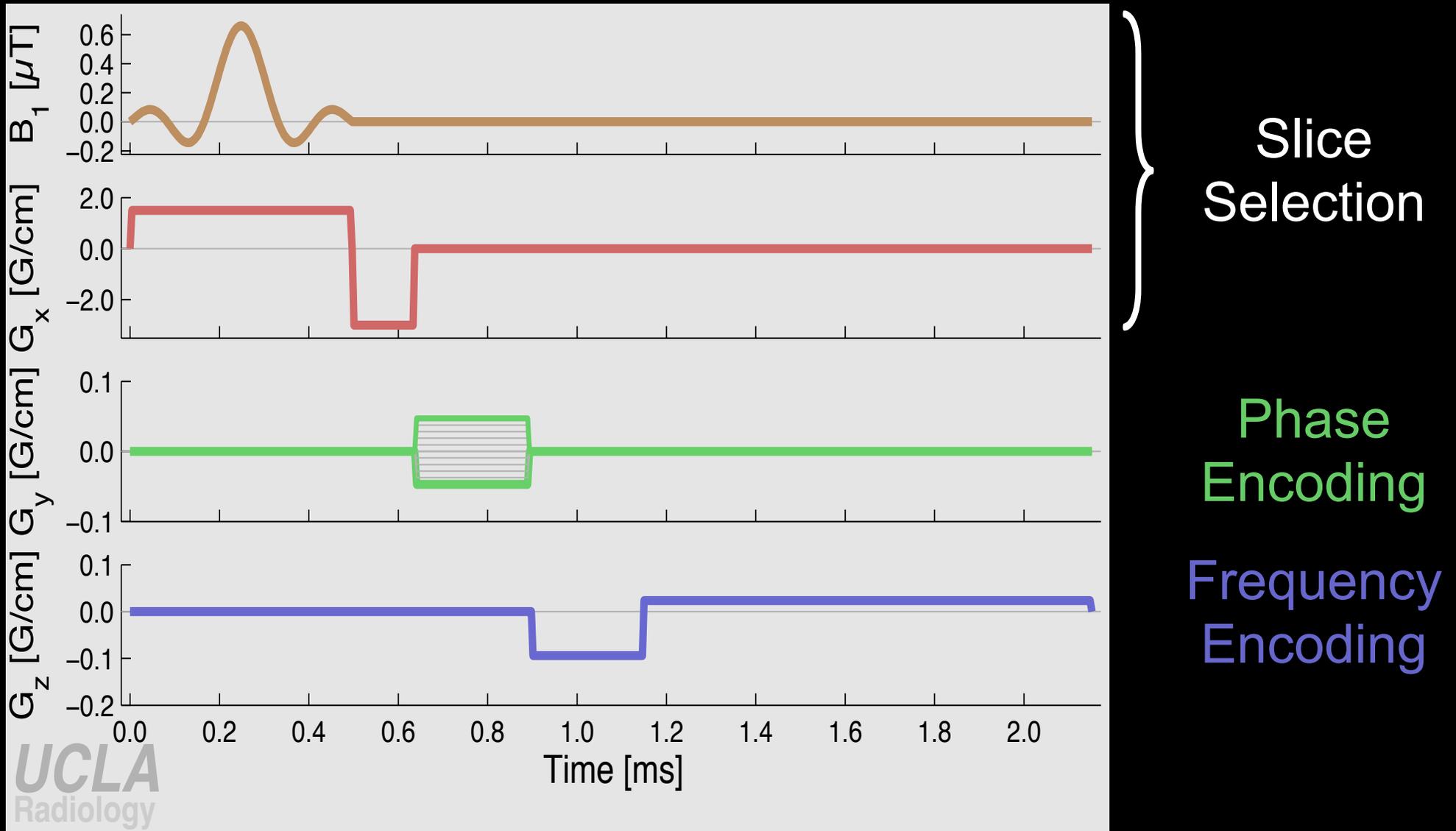


Spatial Encoding

- Three key steps:
 - **Slice selection**
 - You have to pick slice!
 - **Phase Encoding**
 - You have to encode 1 of 2 dimensions within the slice.
 - **Frequency Encoding (aka *readout*)**
 - You have to encode the other dimension within the slice.



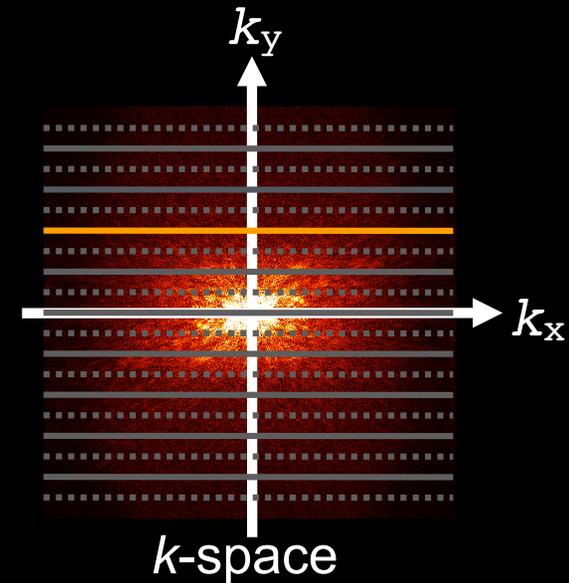
3 Steps for Spatial Localization



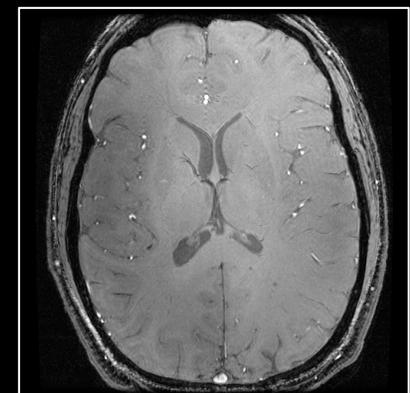
Pulse Sequence Diagram - Timing diagram of the RF and gradient events that comprise an MRI pulse sequence.

Phase Encoding

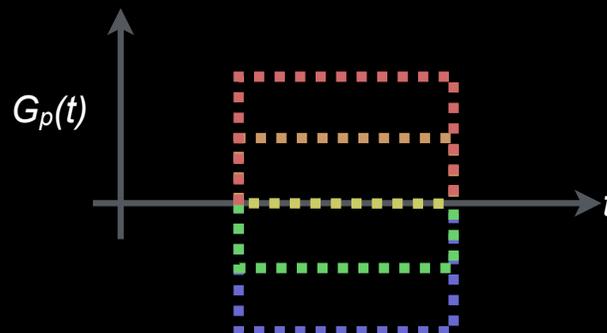
- **Consists of:**
 - Phase encoding gradient
 - Magnitude changes with each TR
 - Can be played with other gradients
 - Crushers, Slice-selection rephaser, readout dephasing
- **Used with Cartesian imaging**
- **After excitation, before readout**
- **Adds linear spatial variation of phase**
- **Phase encode in**
 - one direction for 2D imaging
 - two directions for 3D imaging
- **Only one PE step per echo**



↓ iFFT

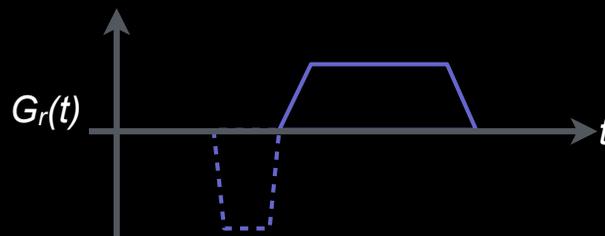


Image

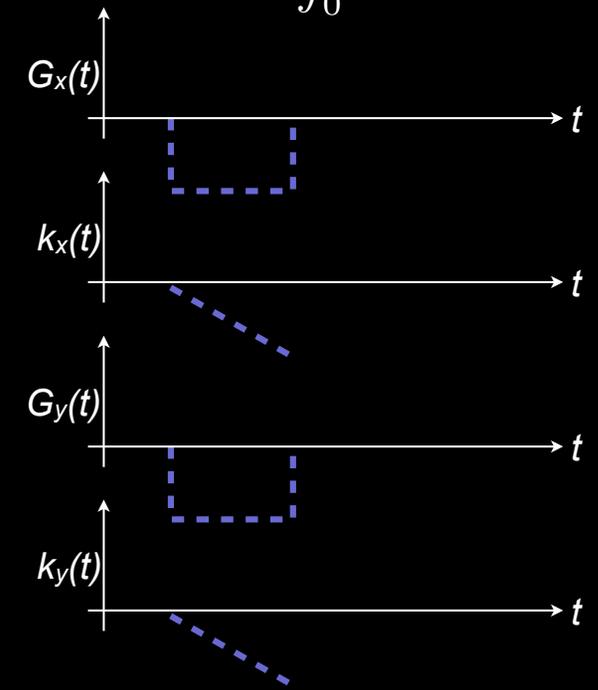
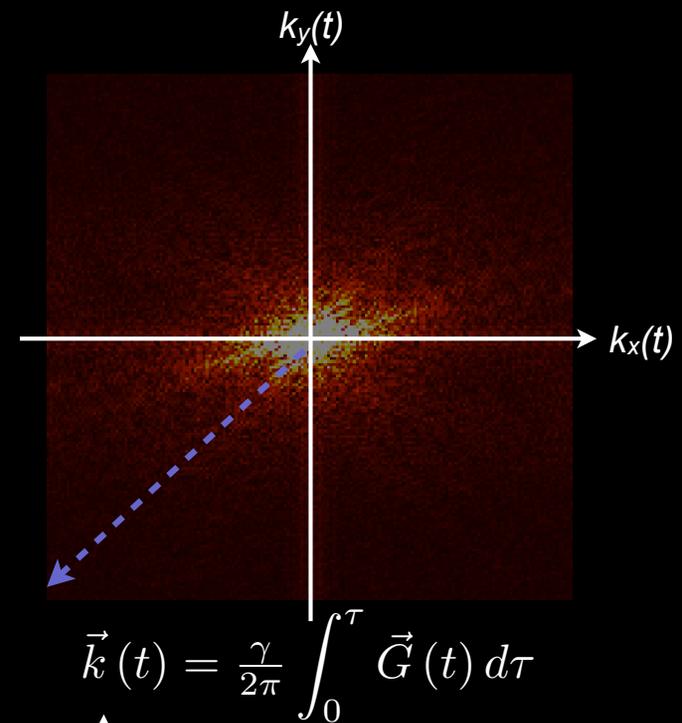
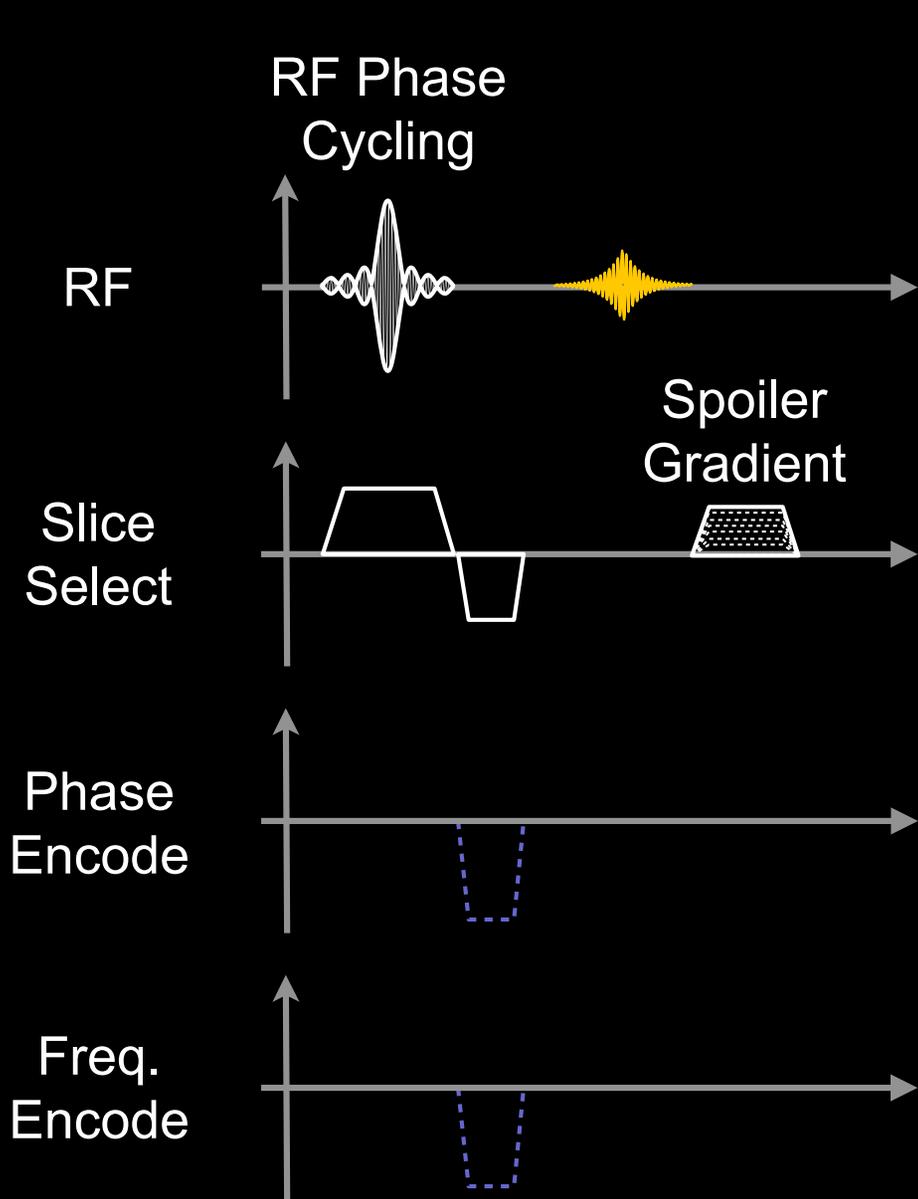


Frequency Encoding

- **Consists of:**
 - **Frequency encoding gradient**
 - **Constant magnitude for Cartesian imaging**
 - **No simultaneous**
 - **RF (B_1)**
 - **Other gradients**
 - phase encoding, slice encoding, crushers
 - **Readout pre-phasing gradient**
 - **Prepares spin phase so peak echo amplitude occurs at middle of readout (TE)**
 - **AKA “readout de-phasing gradient”**
- **Adds linear spatial variation of frequency**
- **Helps form an echo**

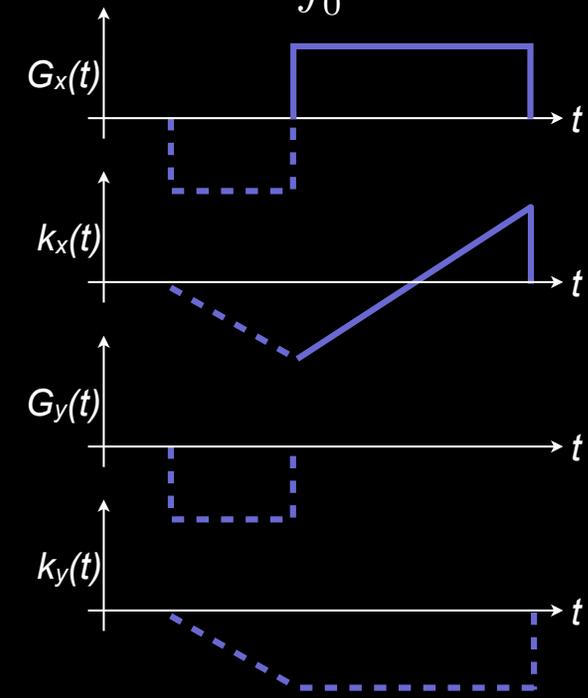
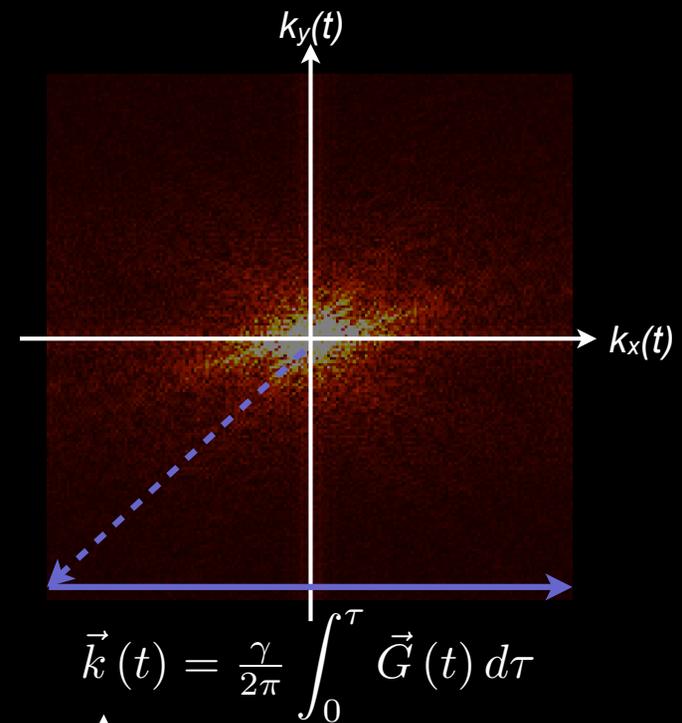
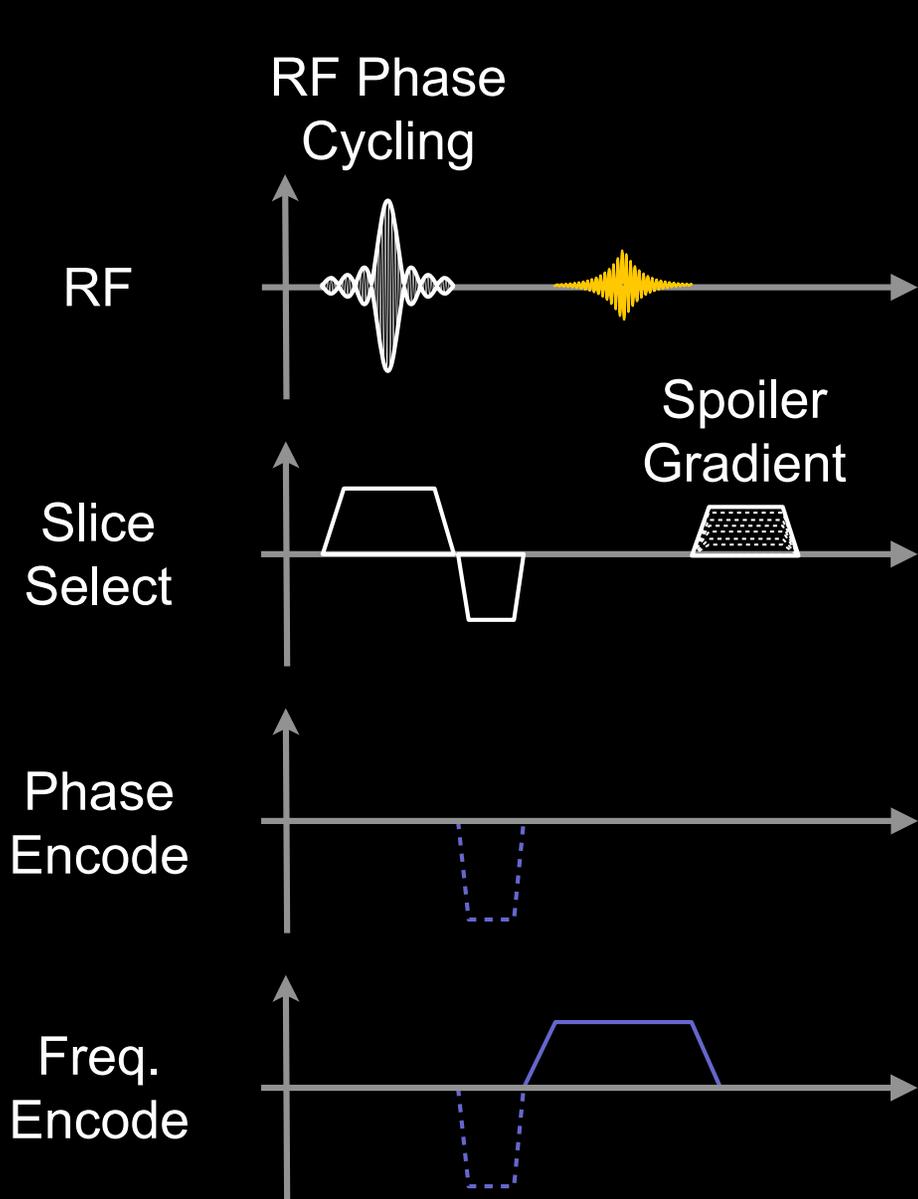


Where am I in k -space?



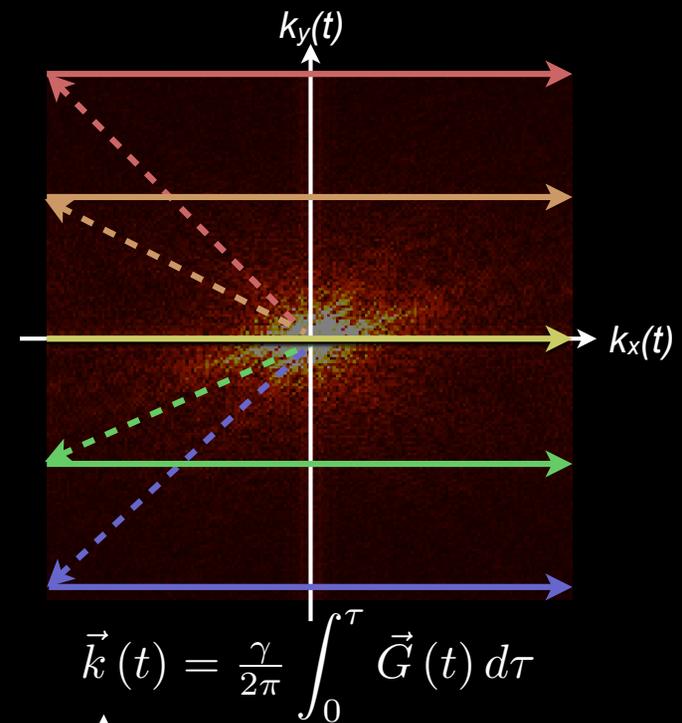
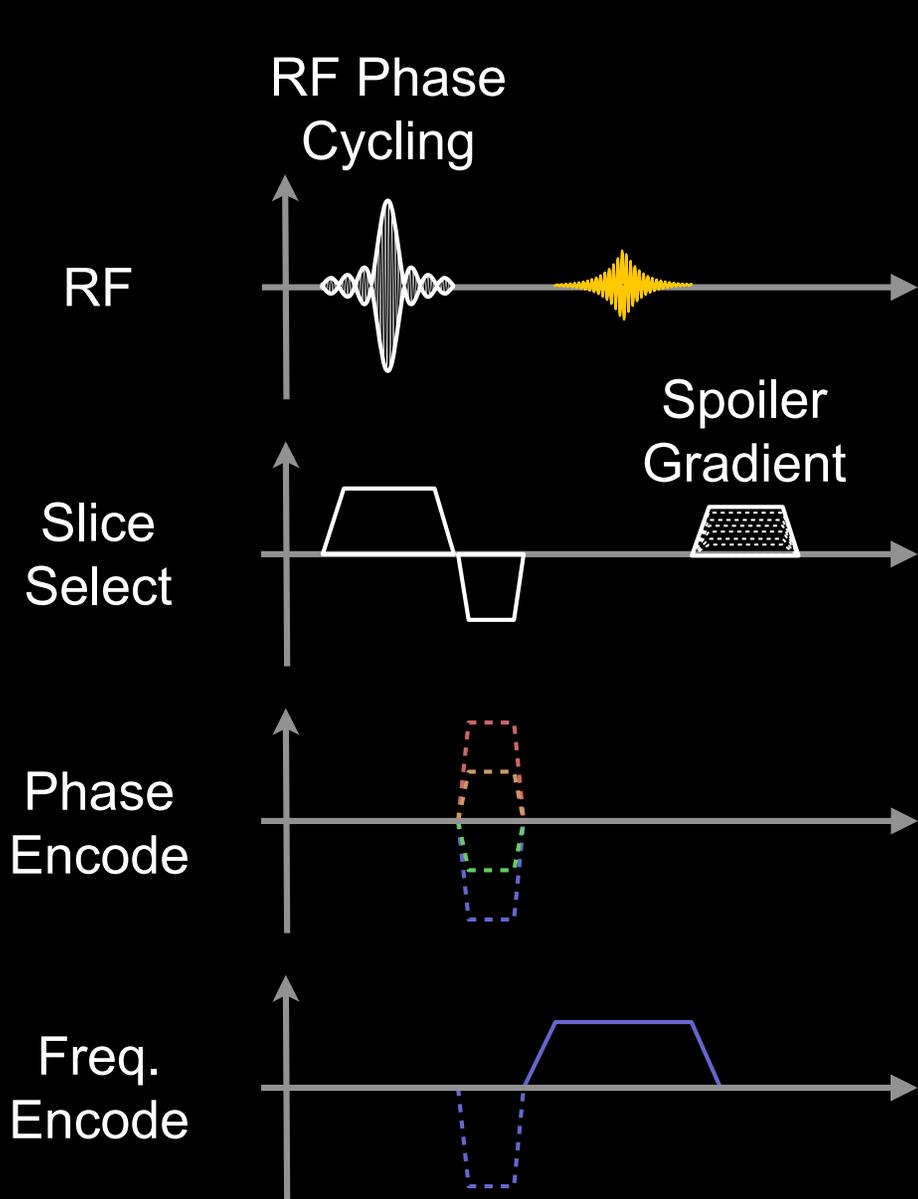
One phase encoded echo is acquired per TR.

Where am I in k -space?

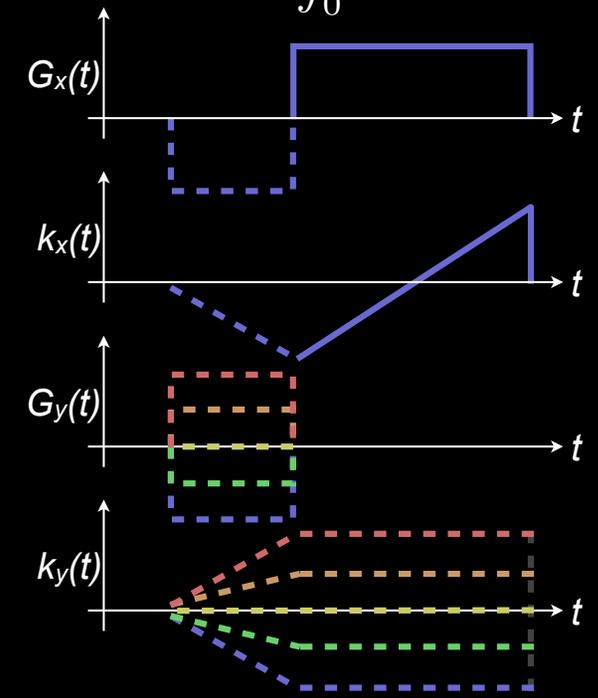


One phase encoded echo is acquired per TR.

Where am I in k -space?



$$\vec{k}(t) = \frac{\gamma}{2\pi} \int_0^t \vec{G}(\tau) d\tau$$



One phase encoded echo is acquired per TR.

Questions?

- Related reading materials
 - Nishimura - Chap 5

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<http://mrri.ucla.edu/sunglab>