

# *Compressed Sensing & Artificial Intelligence*

M229 Advanced Topics in MRI

*Kyung Sung, Ph.D.*

2021.05.27

# Class Business

- Final project abstract / presentation
  - Abstract due on 6/4 by 5pm
  - Recorded presentation file (5-6min) due on 6/7 by 5pm
  - Final project presentation and Q&A (<5min) session on 6/8 (10-12pm)
- Office hours
  - Instructors: Fri 10-12 noon
- Online course evaluation

# Today's Topics

- Compressed sensing
  - Compressibility or sparsity
  - Incoherent measurement
  - Reconstruction
- Machine learning / artificial intelligence
  - Model evaluation
  - Model selection

# Fast MRI Techniques

- Many reconstruction methods minimize aliasing artifacts by exploiting information redundancy (or prior knowledge)
  - Parallel imaging
  - Compressed sensing



Donoho, *IEEE TIT*, 2006  
Candes et al., *Inverse Problems*, 2007

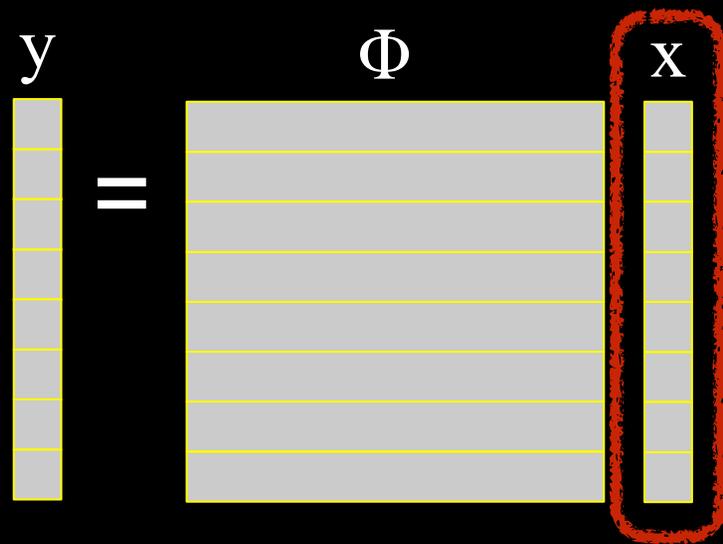
# What is Compressed Sensing?

- CS is about acquiring a **sparse** signal in a most efficient way (subsampling) with the help of an **incoherent** projecting basis

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8 Equations  
8 Unknowns

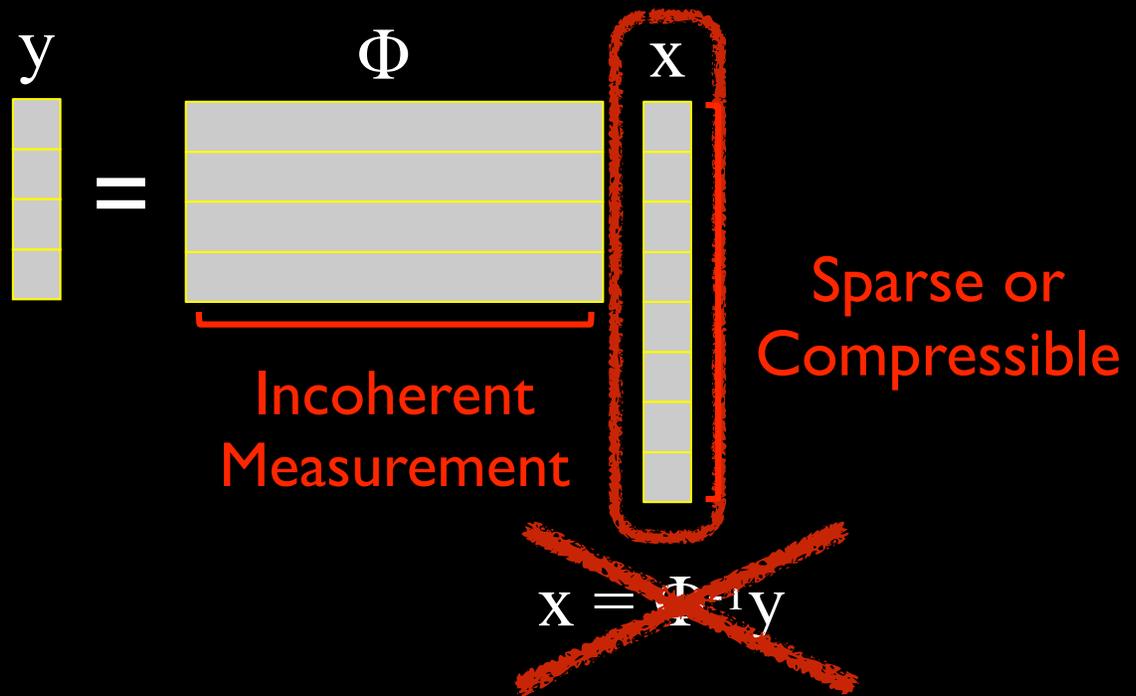


$$x = \Phi^{-1}y$$

# What is Compressed Sensing?

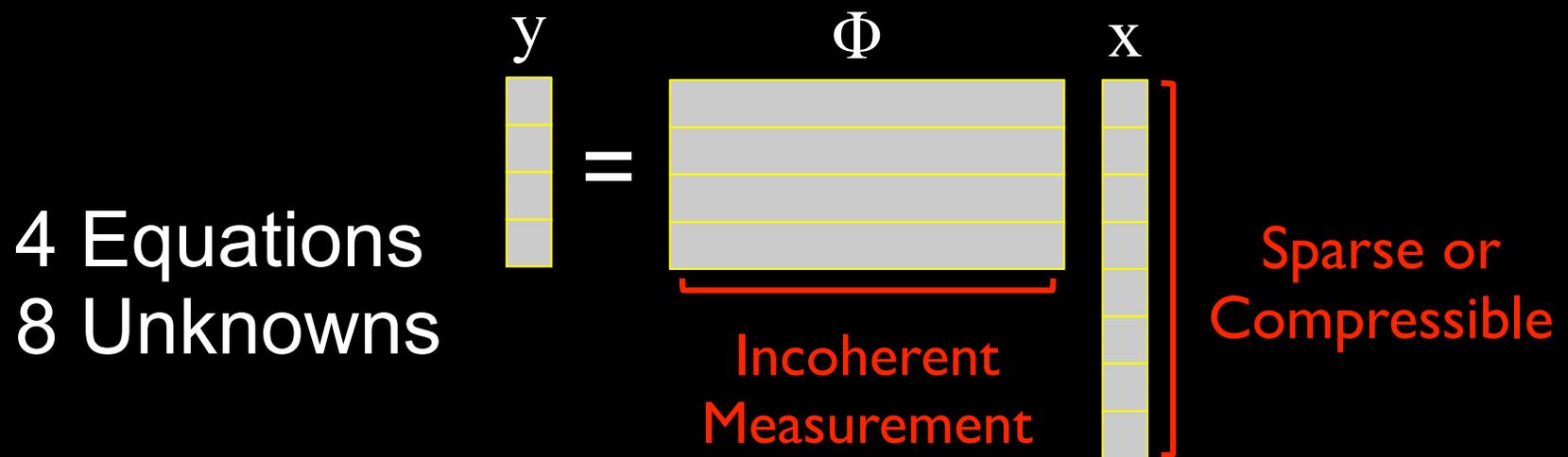
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4 Equations  
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# What is Compressed Sensing?

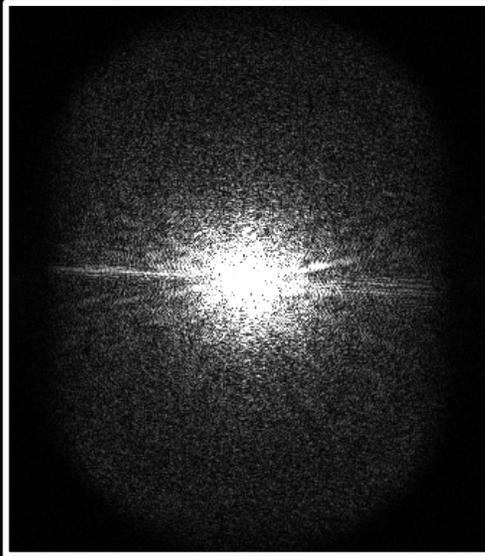
- CS is about acquiring a **sparse** signal in a most efficient way (subsampling) with the help of an **incoherent** projecting basis



We still can find 8 unknowns!

# Compressed Sensing MRI

k-space

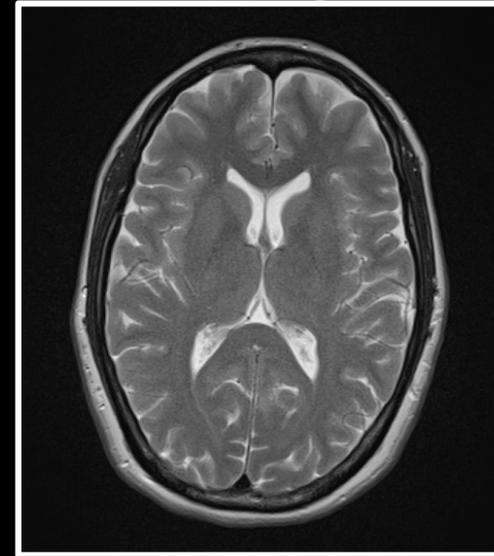


Inverse Fourier  
Transform  $\Phi^{-1}$



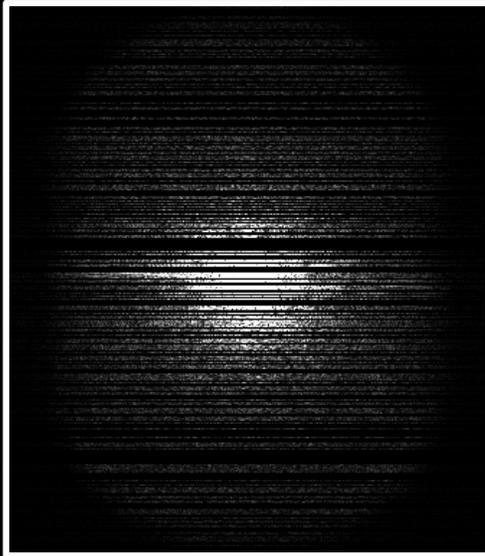
$$x = \Phi^{-1}y$$

Image



# Compressed Sensing MRI

k-space

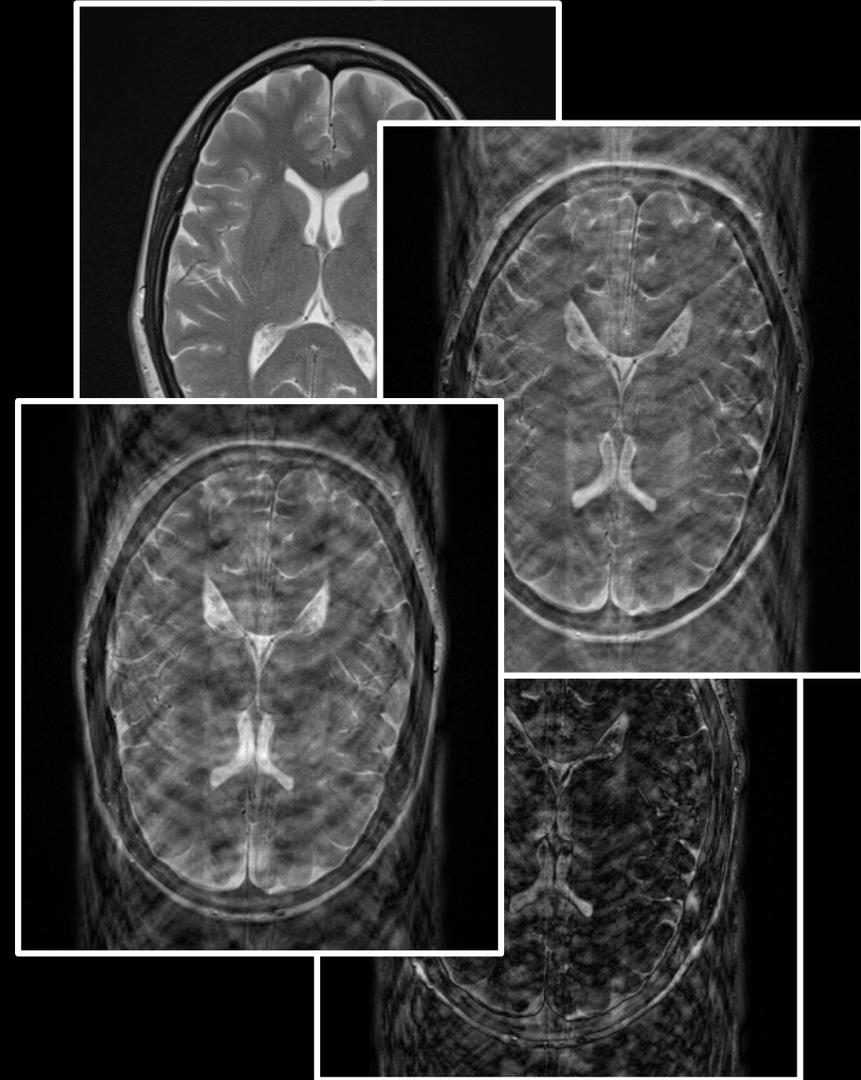


~~Inverse Fourier Transform  $\Phi^{-1}$~~



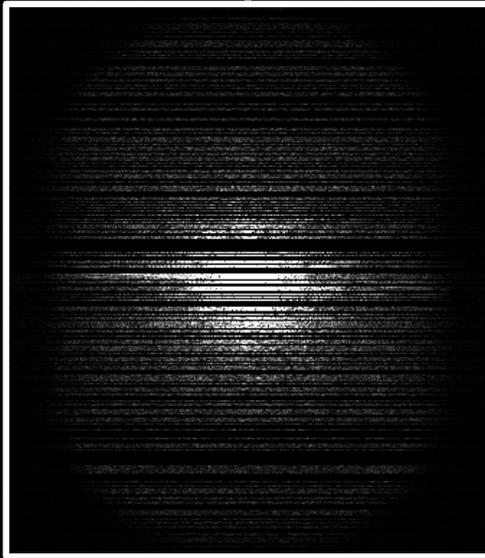
~~$x = \Phi^{-1}y$~~

Image



# Compressed Sensing MRI

k-space

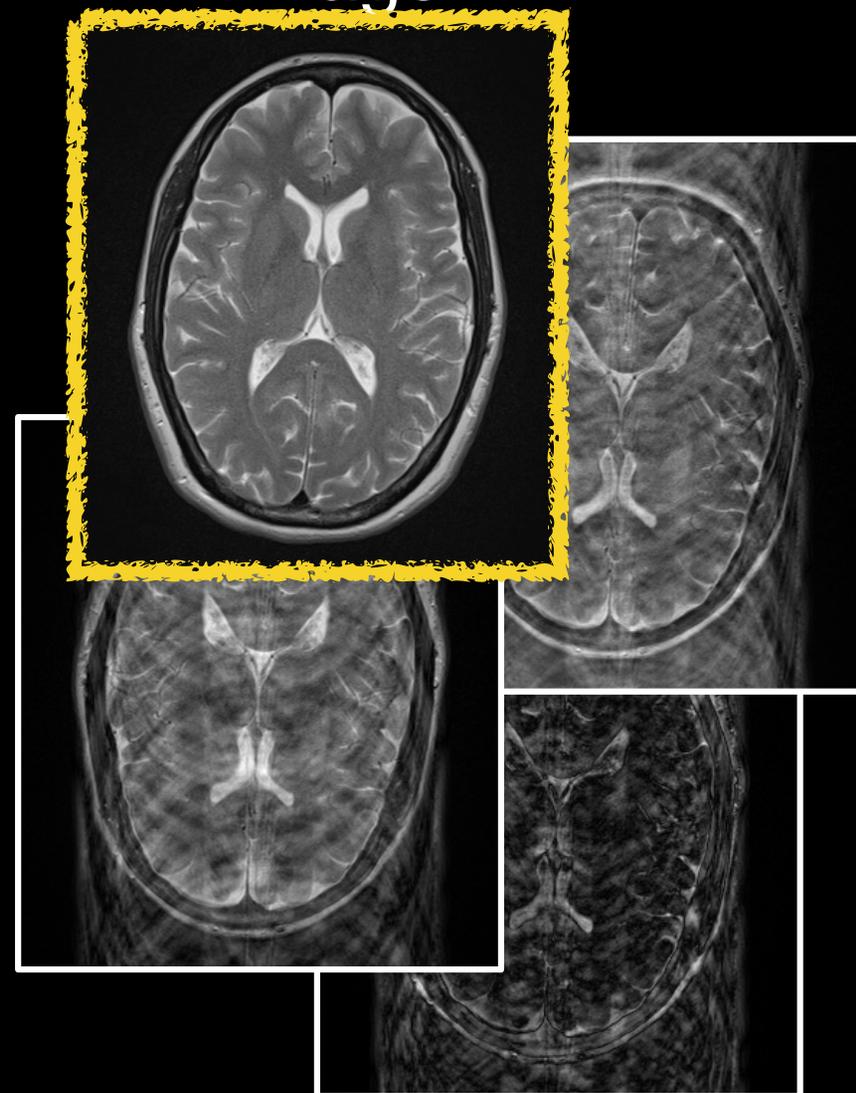


~~Inverse Fourier Transform  $\Phi^{-1}$~~



~~$x = \Phi^{-1}y$~~

Image



Choose the most compressible image matching data  
(systematic optimization)

# Math Background

L0-norm ( $|x|_0$ ): a number of non-zero coefficients

L1-norm ( $|x|_1$ ): a sum of absolute values of coefficients

L2-norm ( $|x|_2$ ): a sum of squared values of coefficients

$$\begin{array}{ccc} \mathbf{x} & \mathbf{x} & \mathbf{x} \\ \begin{pmatrix} 0 \\ 1 \\ 2 \\ 3 \end{pmatrix} & \begin{pmatrix} 0 \\ 1 \\ 0 \\ 0 \end{pmatrix} & \begin{pmatrix} 1 \\ 1 \\ -2 \\ 3 \end{pmatrix} \end{array}$$

# CS-MRI Reconstruction

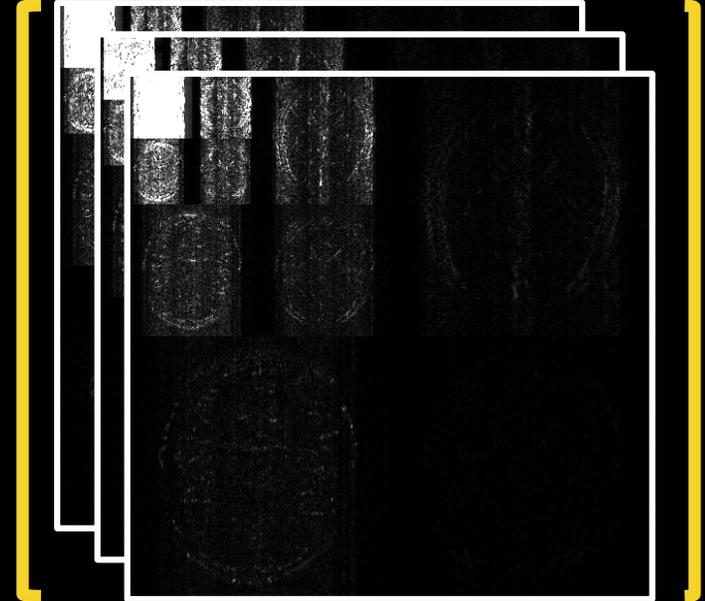
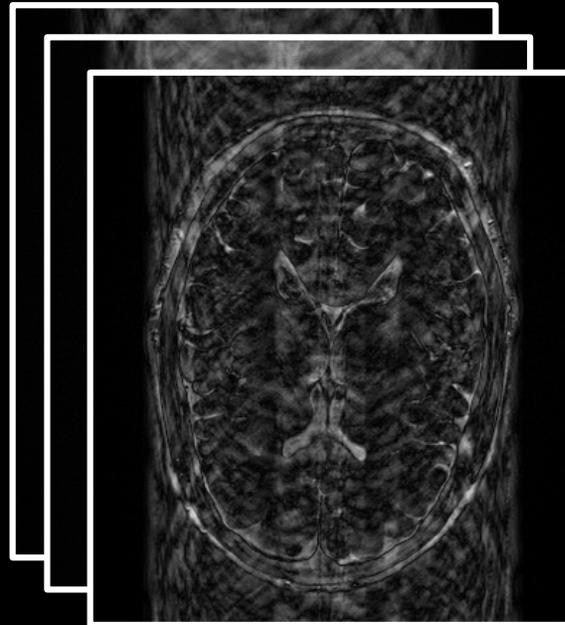
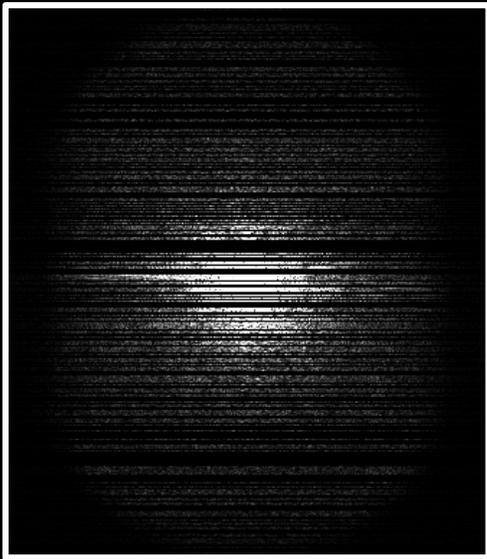
$$|y - \Phi x|^2 < \epsilon$$

$$w = \Psi x$$

y: k-space

x: Image

w: Wavelet



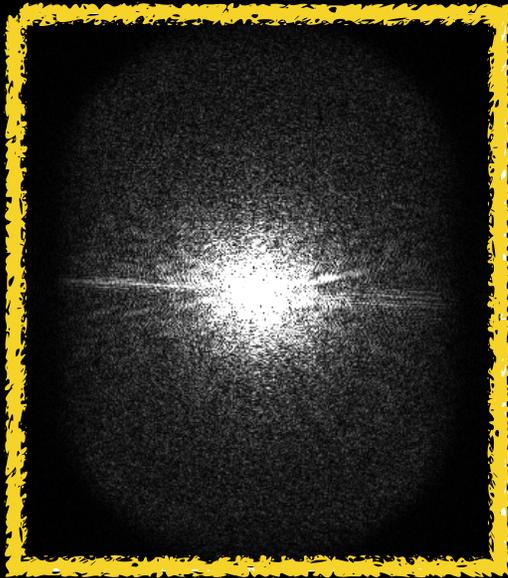
L1-norm

minimize  $|\Psi x|_1$

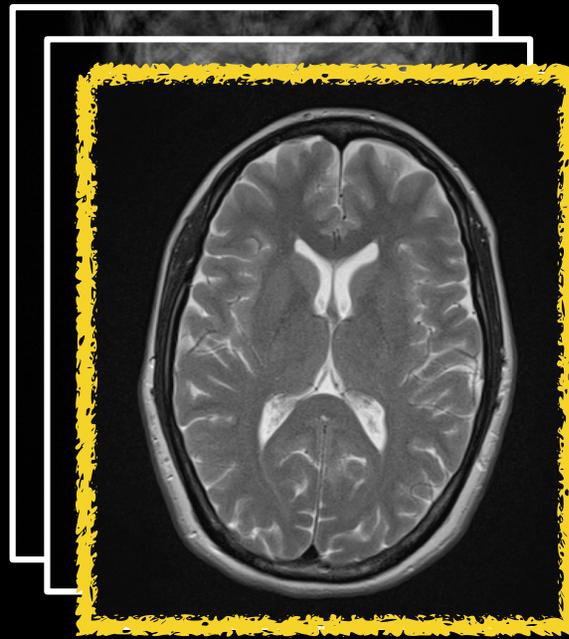
# CS-MRI Reconstruction

$$\text{minimize } F(\mathbf{x}): |\mathbf{y} - \Phi\mathbf{x}|^2 + R(\mathbf{x})$$

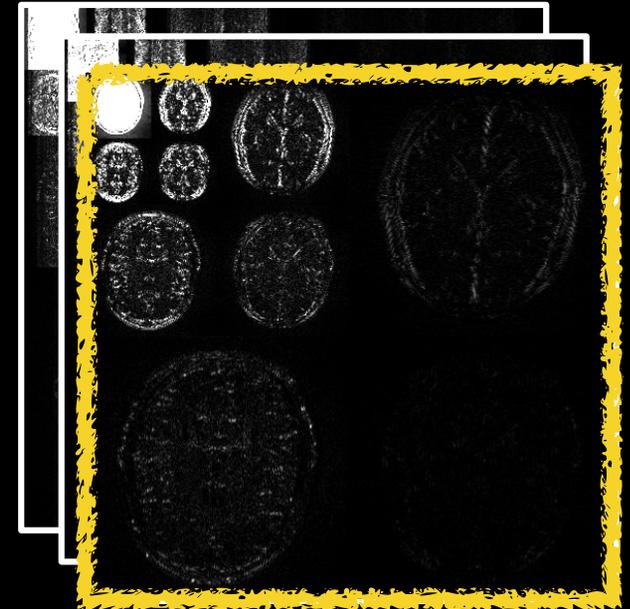
$\mathbf{y}$ : k-space



$\mathbf{x}$ : Image



$\mathbf{w}$ : Wavelet



$$\mathbf{y}' = \mathbf{FT}(\mathbf{x})$$

$$\mathbf{x} = \Psi^{-1}\mathbf{w}$$

# Three Tenets of CS

$$\text{minimize } F(\mathbf{x}): \underbrace{|\mathbf{y} - \Phi\mathbf{x}|_2^2}_{\text{Data Consistency}} + \underbrace{R(\mathbf{x})}_{\text{Compressibility Constraint}}$$

**Data Consistency**      **Compressibility Constraint**

- Three key elements of Compressed Sensing:

Compressibility

Incoherence

Nonlinear Reconstruction

# Compressibility Constraint

minimize  $F(\mathbf{x}): \|\mathbf{y} - \Phi\mathbf{x}\|_2^2 + \mathbf{R}(\mathbf{x})$

**Compressibility  
Constraint**

- $\mathbf{R}(\mathbf{x}) = \lambda\|\mathbf{x}\|_1$  (Identity Transform)
- $\mathbf{R}(\mathbf{x}) = \lambda\|\Psi\mathbf{x}\|_1$  (Wavelet Transform)
- $\mathbf{R}(\mathbf{x}) = \lambda\mathbf{H}(\mathbf{x})$  (Total Variation)
- $\mathbf{R}(\mathbf{x}) = \lambda\|\mathbf{x}\|_*$  (Rank or Nuclear Norm)
- Many more...

# Wavelet Transform

- Natural images are compressible using wavelet transforms

Image Compression Standard: JPEG2000



Uncompressed  
378 KiB  
1:1

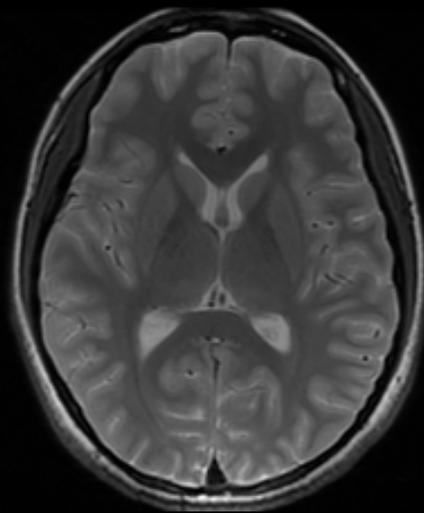
JPEG JFIF  
11.2 KiB  
1:33.65  
IJG q 30

JPEG 2000  
11.2 KiB  
1:33.65

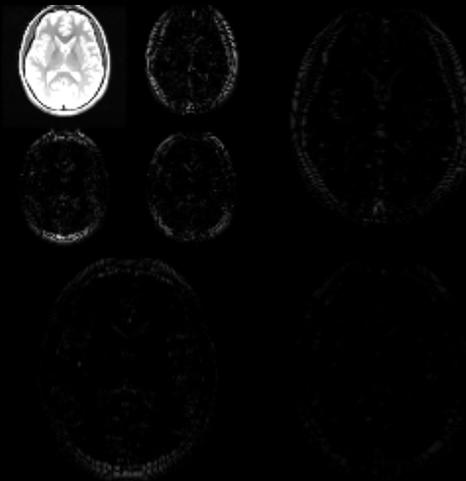
Images from Wikipedia

# Wavelet Transform

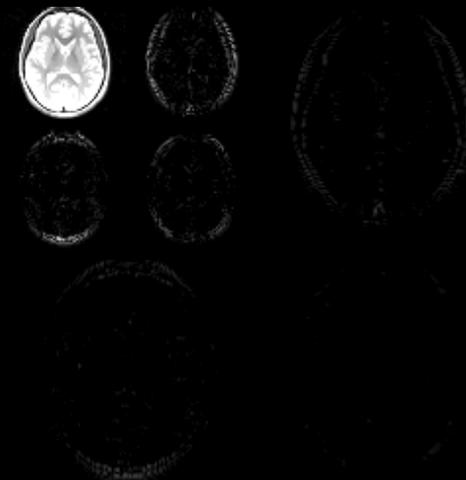
MR images are mostly compressible using wavelet transforms



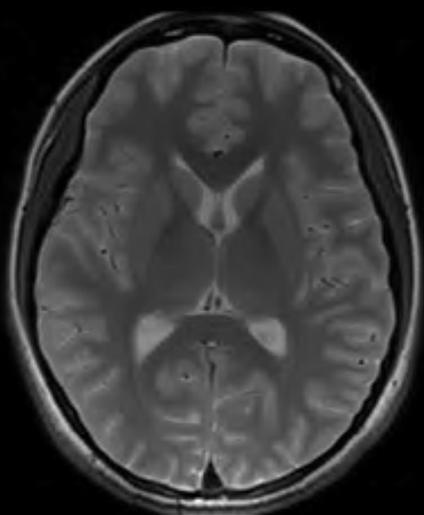
**Wavelet Transform**



**10% Largest Coefficients**

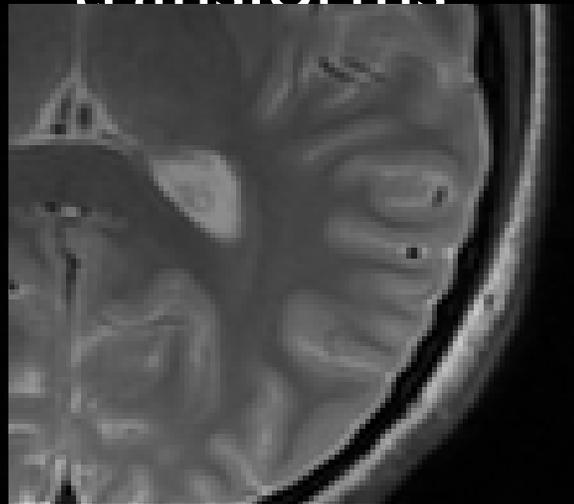
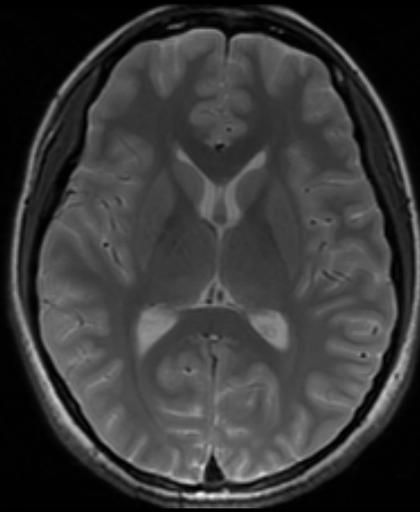


**Inverse Wavelet Transform**

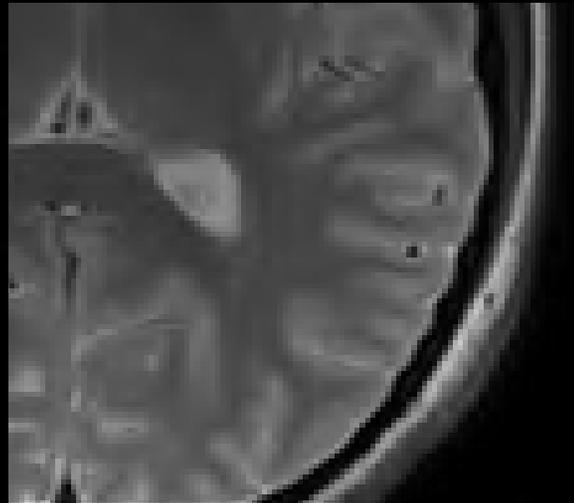
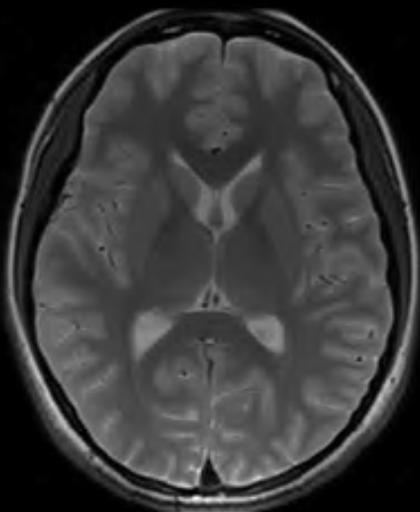


# Wavelet Transform

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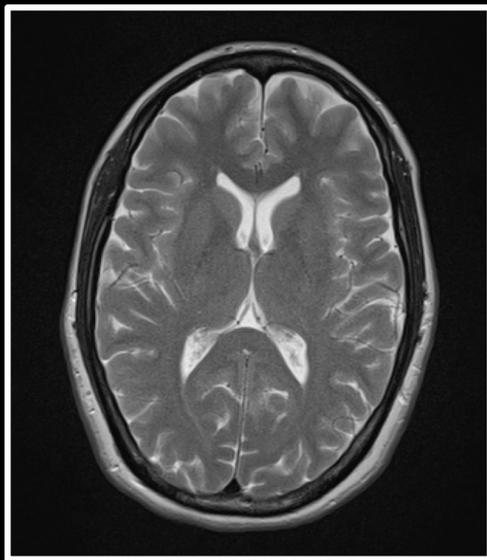


**10% Largest Coefficients**



# Total Variation

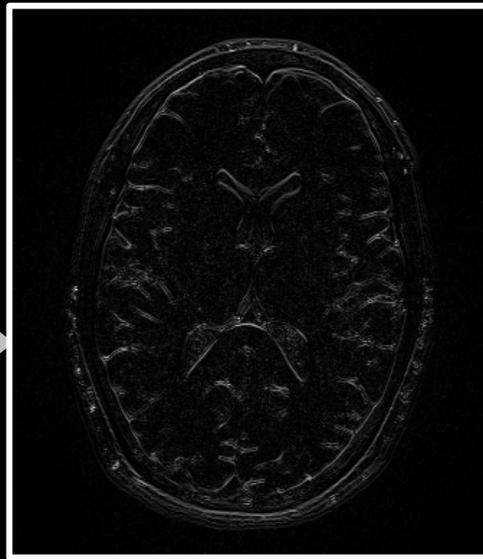
$$H(x) = \sum_{i,j} \sqrt{\underbrace{|x_{i+1,j} - x_{i,j}|^2}_{Dx} + \underbrace{|x_{i,j+1} - x_{i,j}|^2}_{Dy}}$$



**Total  
Variation**

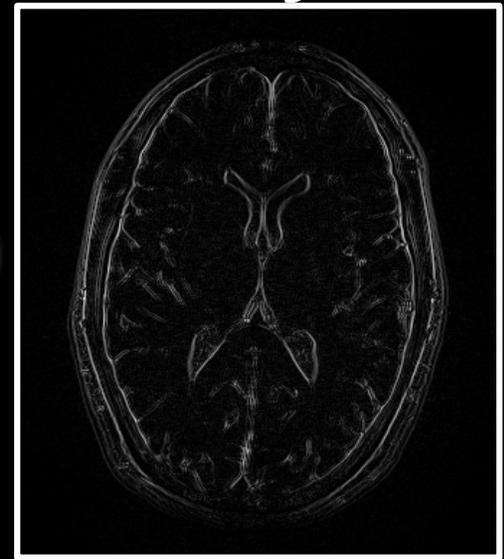


**Dx**



**+**

**Dy**



**Σ**

# CS-MRI Reconstruction

$$\text{minimize } F(\mathbf{x}): \underbrace{\|y - \Phi\mathbf{x}\|_2^2}_{\text{data fidelity}} + R(\mathbf{x})$$

- Minimizing  $F(\mathbf{x})$  is non-trivial since  $R(\mathbf{x})$  is not differentiable
  - Linear programming is challenging due to high computational complexity
- Simple gradient-based algorithms have been developed:
  - Re-weighted L1 / FOCUSS
  - IST / IHT / AMP / FISTA
  - Split Bregman / ADMM

*I.F. Gorodnitsky, et al., J. Electroencephalog. Clinical Neurophysiol. 1995 Daubechies I, et al. Commun. Pure Appl. Math. 2004  
Elad M, et al. in Proc. SPIE 2007  
T. Goldstein, S. Osher, SIAM J. Imaging Sci. 2009*

# State-of-the-Art CS-MRI

- Reducing possible reconstruction failure
  - Improve sparse transformations
  - Develop k-space undersampling schemes
- Integrating CS with DL/parallel imaging
  - Develop compatible undersampling patterns
  - Develop reconstruction methods

# State-of-the-Art CS-MRI

- Methods to evaluate CS reconstructed images
  - RMSE / SSIM / Mutual Information
- Reducing reconstruction time
  - Reduce computational complexity
  - Parallelize reconstruction problems
- Developing stable reconstruction algorithms
  - Minimize / avoid the number of regularization parameters

# Summary So Far...

$$\text{minimize } F(\mathbf{x}): \underbrace{|\mathbf{y} - \Phi\mathbf{x}|_2^2}_{\text{Data Consistency}} + \underbrace{R(\mathbf{x})}_{\text{Compressibility Constraint}}$$

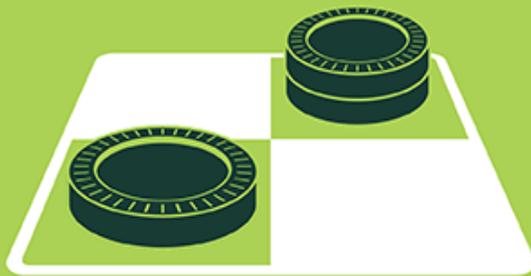
Data  
Consistency

Compressibility  
Constraint

Compressibility Constraint  
Incoherent Measurement  
Reconstruction

# ARTIFICIAL INTELLIGENCE

Early artificial intelligence stirs excitement.



# MACHINE LEARNING

Machine learning begins to flourish.



# DEEP LEARNING

Deep learning breakthroughs drive AI boom.



1950's

1960's

1970's

1980's

1990's

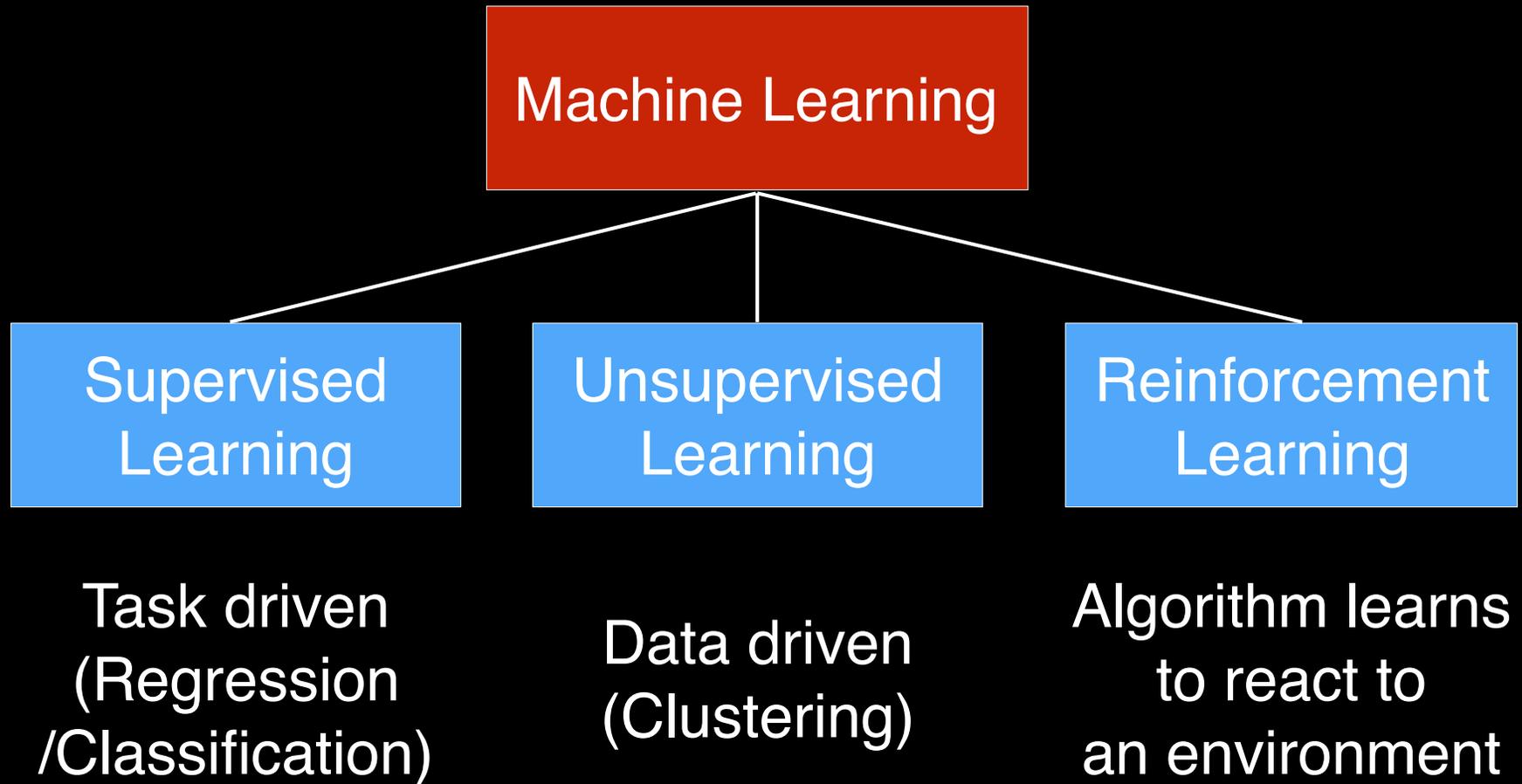
2000's

2010's

Since an early flush of optimism in the 1950s, smaller subsets of artificial intelligence – first machine learning, then deep learning, a subset of machine learning – have created ever larger disruptions.

*From nvidia.com*

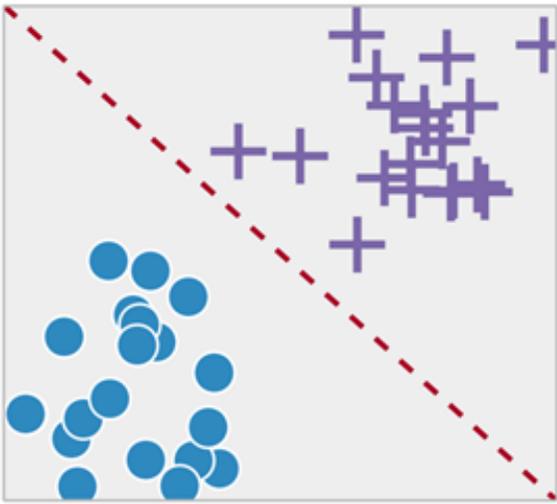
# Types of Machine Learning



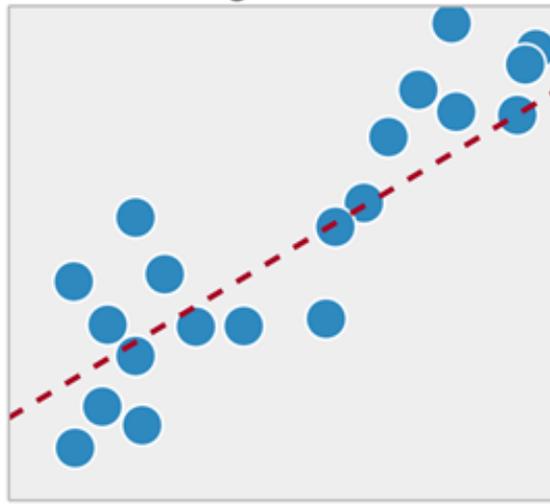
# Types of Machine Learning

## Supervised Learning

Classification

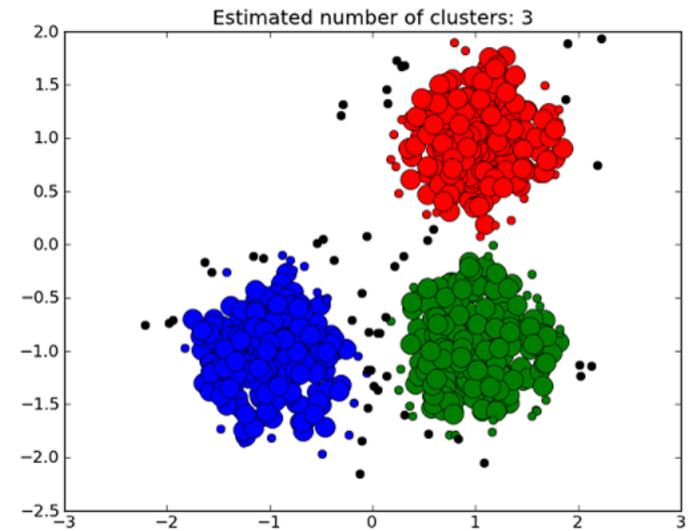


Regression



Discriminative  
Model

## Unsupervised Learning



Generative Model

# Common Datasets for Deep Learning

- MNIST: 60,000 images, hand writing digits (1998)

• CIFAR-10: 60,000 images, 10 classes of  
Not trivial to build medical imaging database with a high number of images and accurate labeling

- ImageNet: 1,300,000 high-res images, 1,000 classes of object (2012)

0 1 2 3 4 5 6 7 8 9  
0 1 2 3 4 5 6 7 8 9  
0 1 2 3 4 5 6 7 8 9  
0 1 2 3 4 5 6 7 8 9  
0 1 2 3 4 5 6 7 8 9  
0 1 2 3 4 5 6 7 8 9  
0 1 2 3 4 5 6 7 8 9



## ImageNet Challenge

IMAGENET

- 1,000 object classes (categories).
- Images:
  - 1.2 M train
  - 100k test.



# Key Design Considerations

1. Define clear clinical questions
2. Design deep learning models
  - Supervised vs. unsupervised learning
  - Descriptive vs. generative modeling
3. Consider potential limitations
  - Limited amount of training and testing data
  - Uncertainties in labeling

# Artificial Intelligence for MRI

Detection



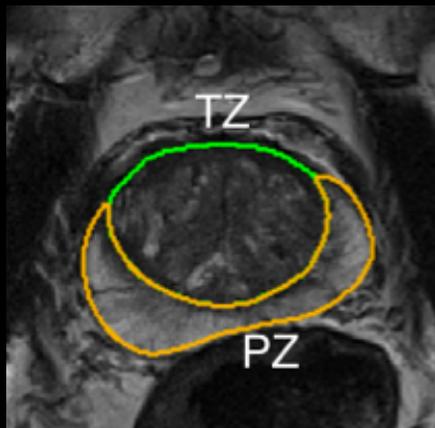
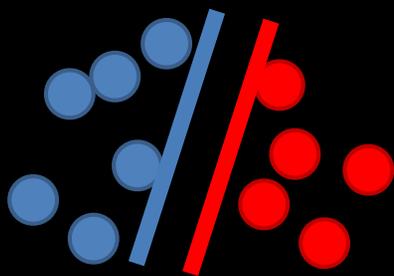
Segmentation



Classification



*Normal*      *Cancerous*



Histologic Findings



# Model Evaluation, Model Selection, and Algorithm Selection

- Target function is a specific, unknown model that we want to learn or approximate
- Model is a certain function that we believe is similar to the true function, the target function that we want to model
- Learning algorithm is a set of instructions that tried to model the target function using a training dataset
- Hyperparameters are the tuning parameters of a machine learning algorithm

# Target Function and Model



Model:  $y = ax + b$

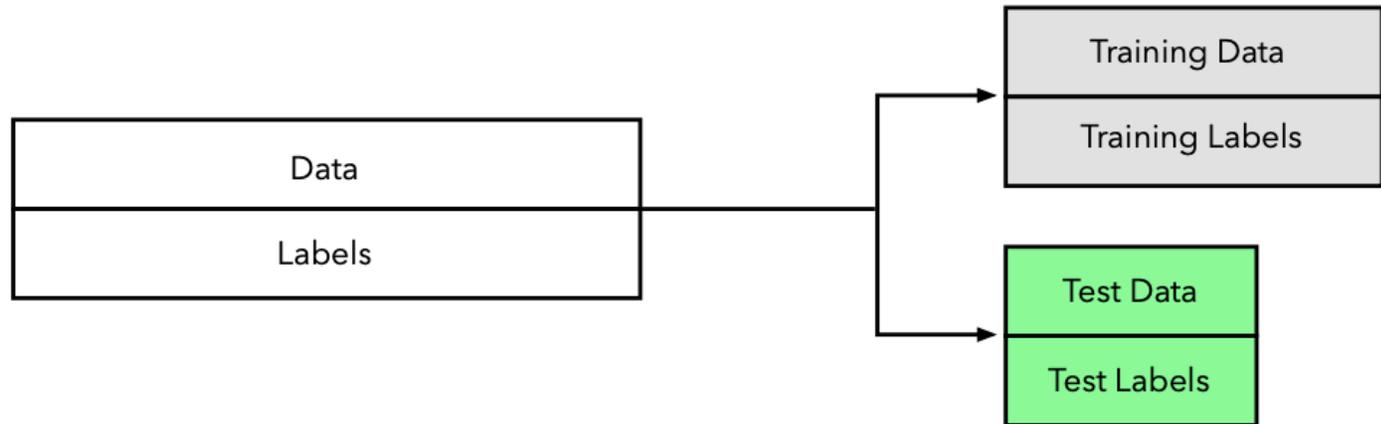
Model parameters: a and b

Learning  
Algorithm

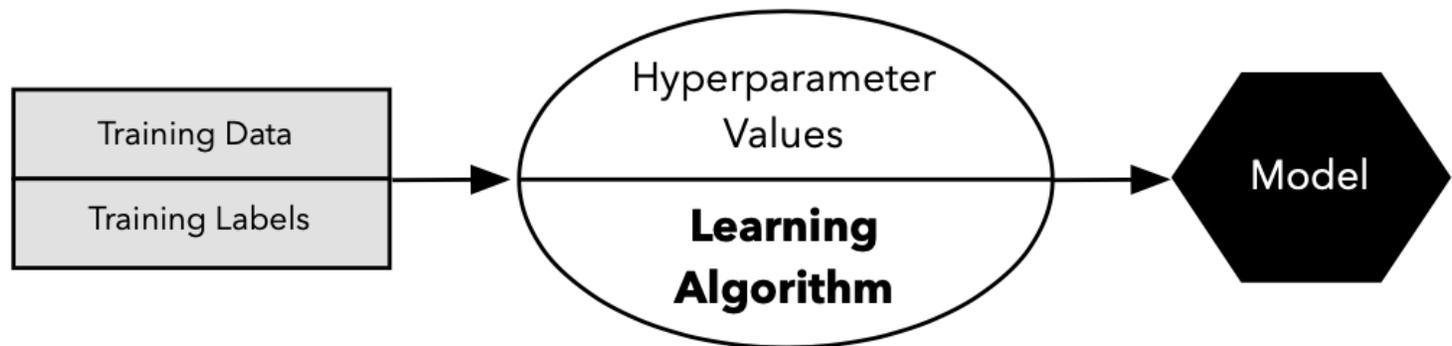
Hyperparameters

# Holdout Validation Method

1

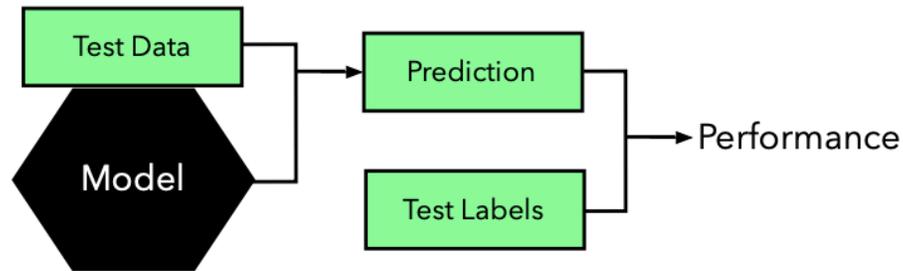


2

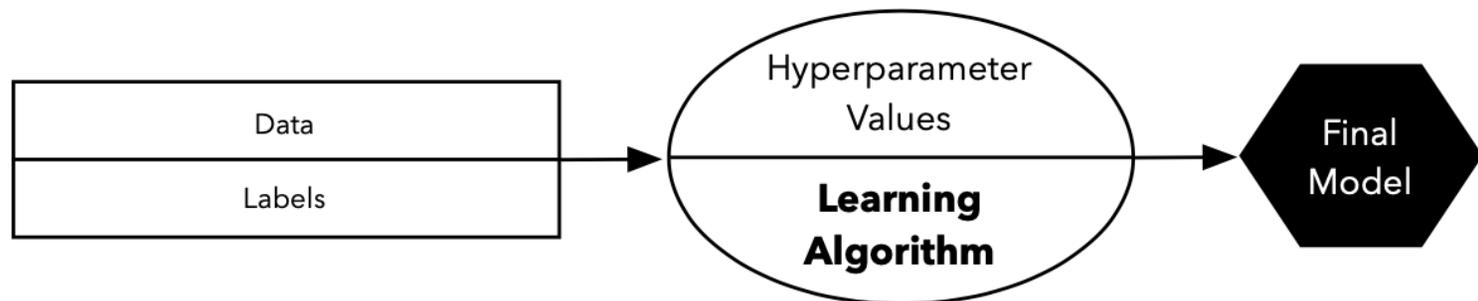


# Holdout Validation

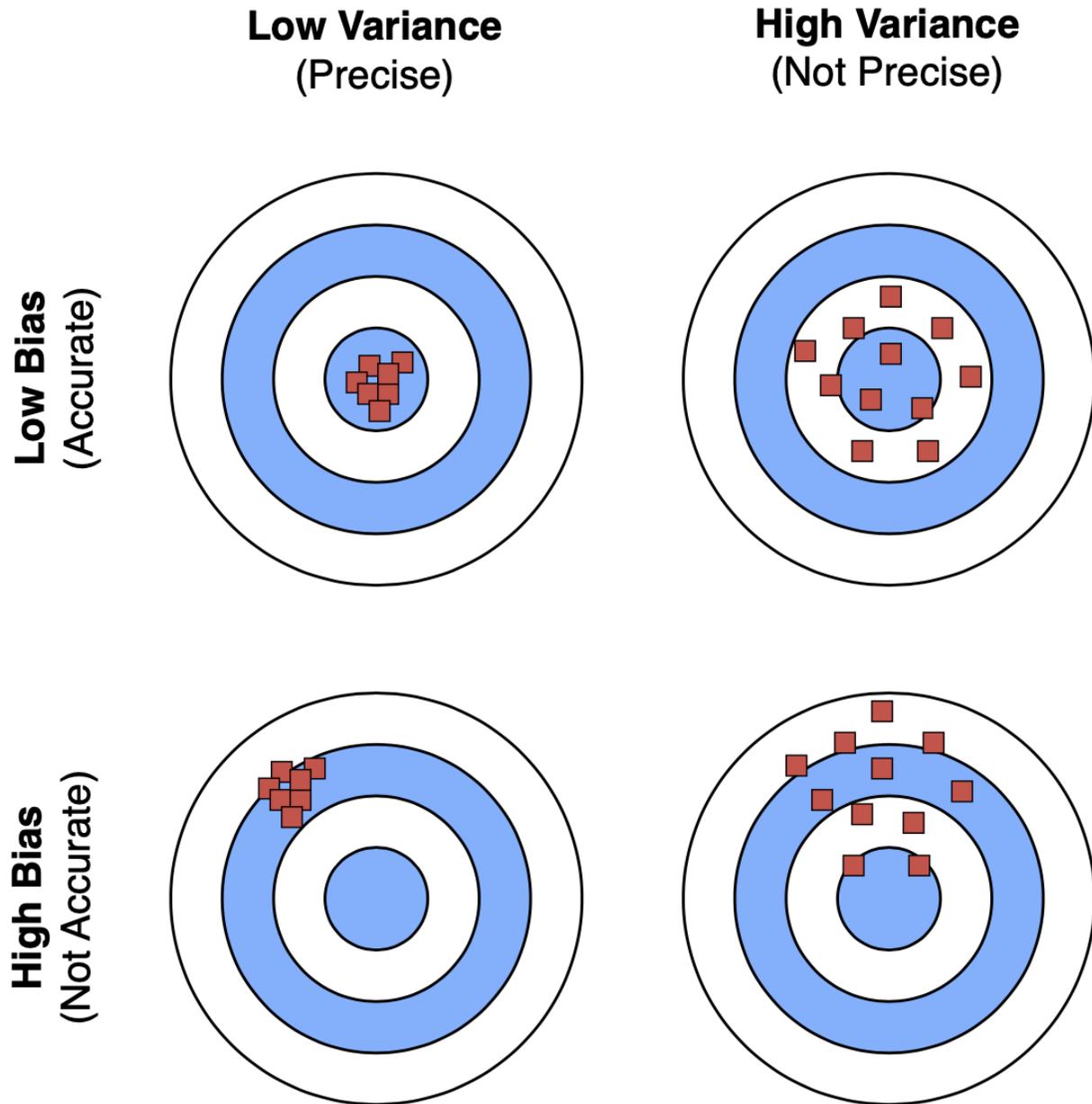
3



4

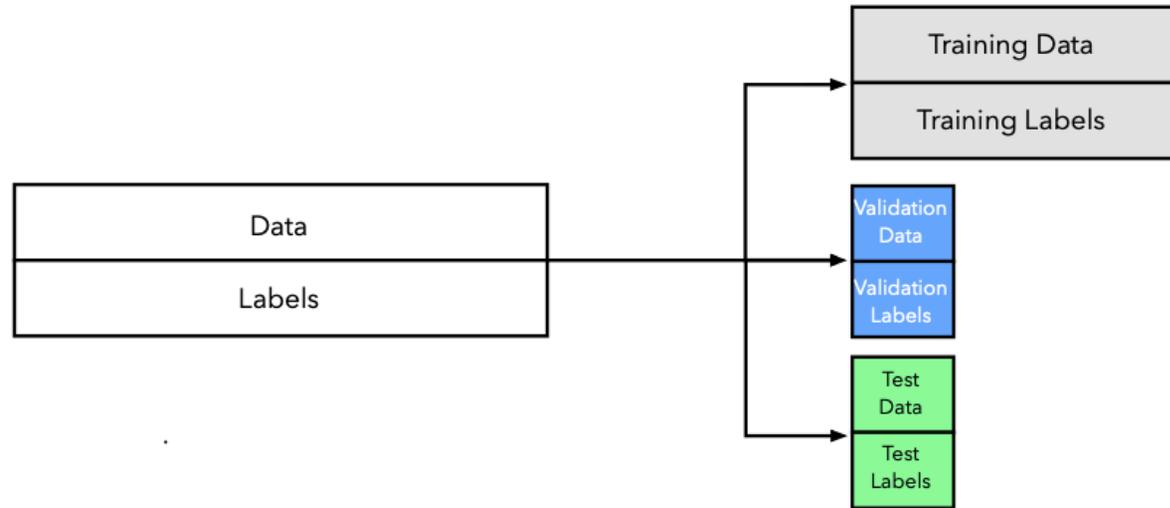


# Bias and Variance

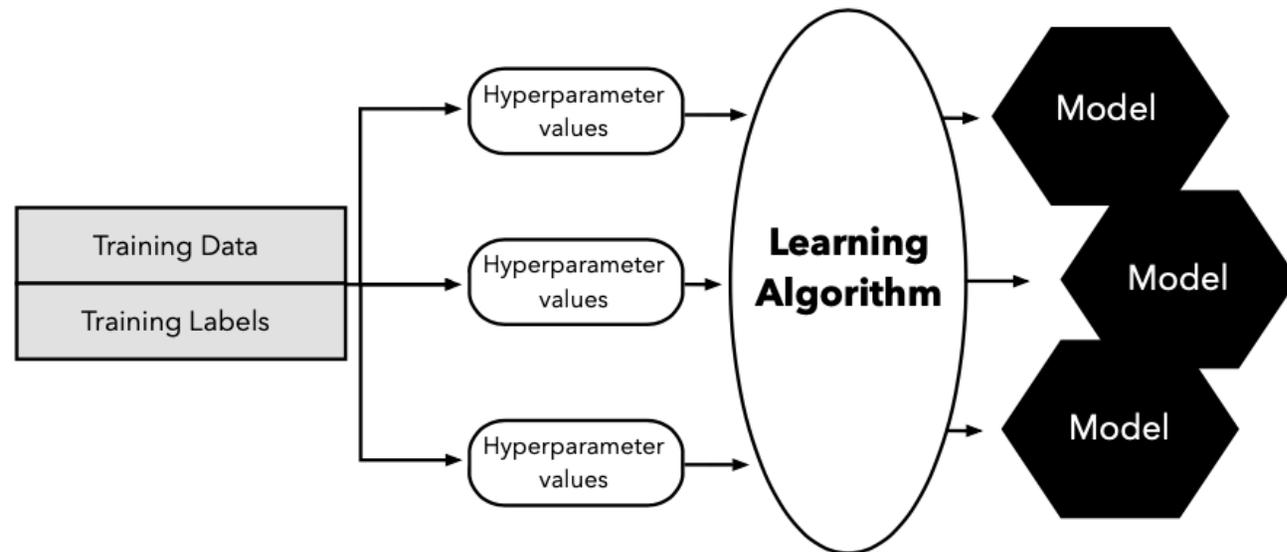


# Three-way Holdout Method

1

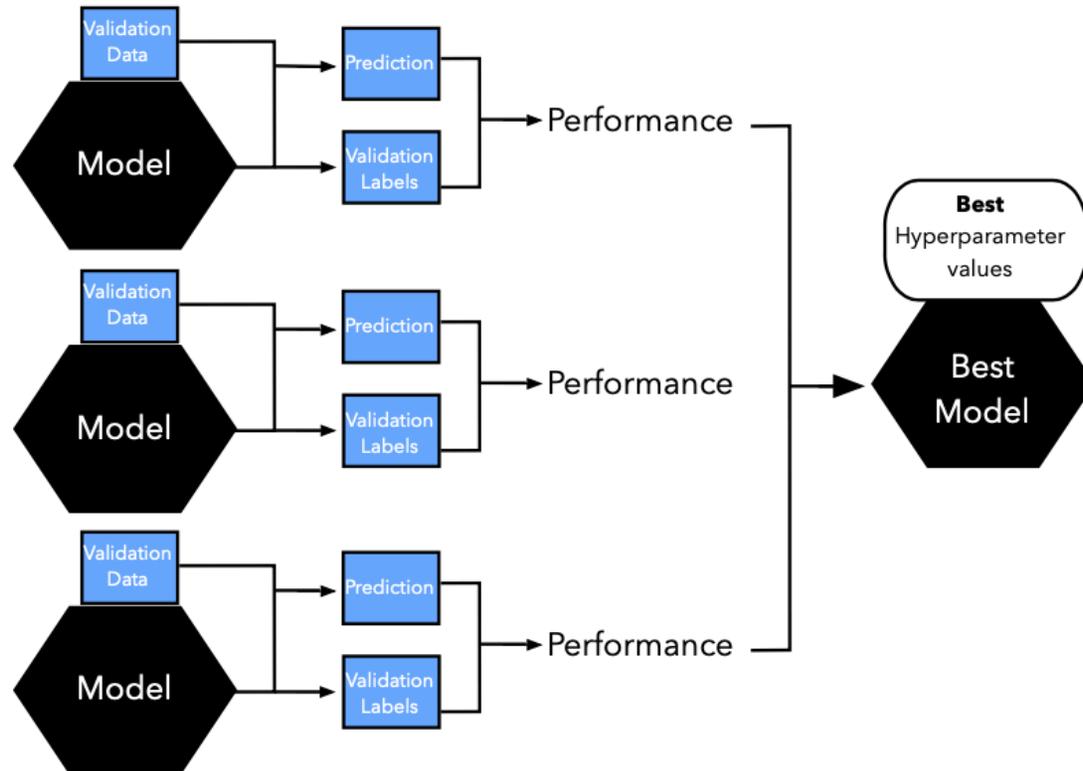


2

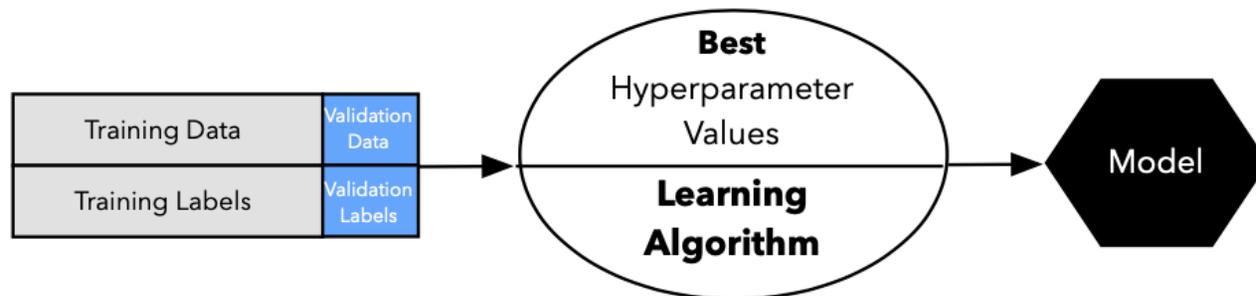


# Three-way Holdout Method

3

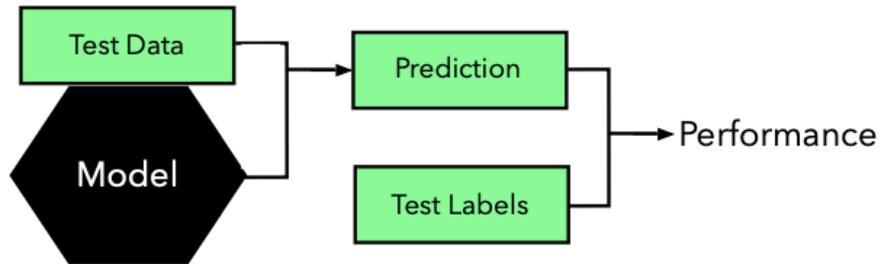


4

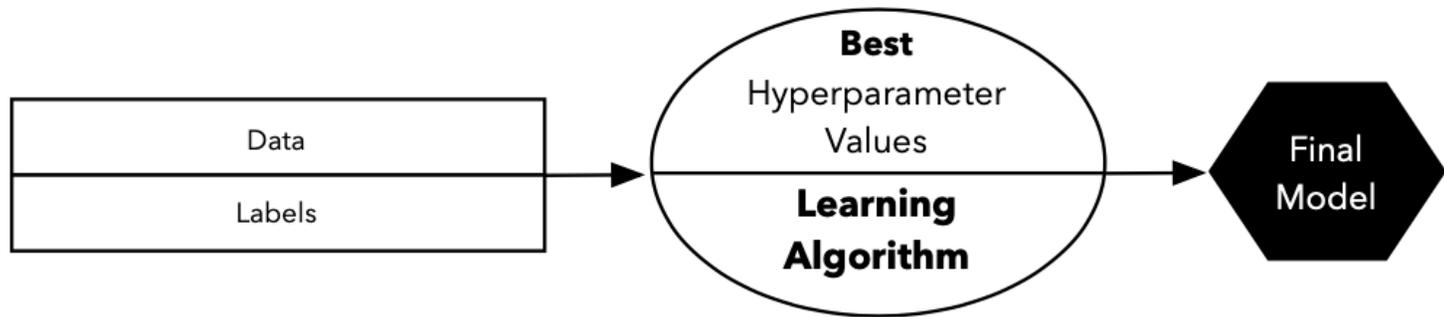


# Three-way Holdout Method

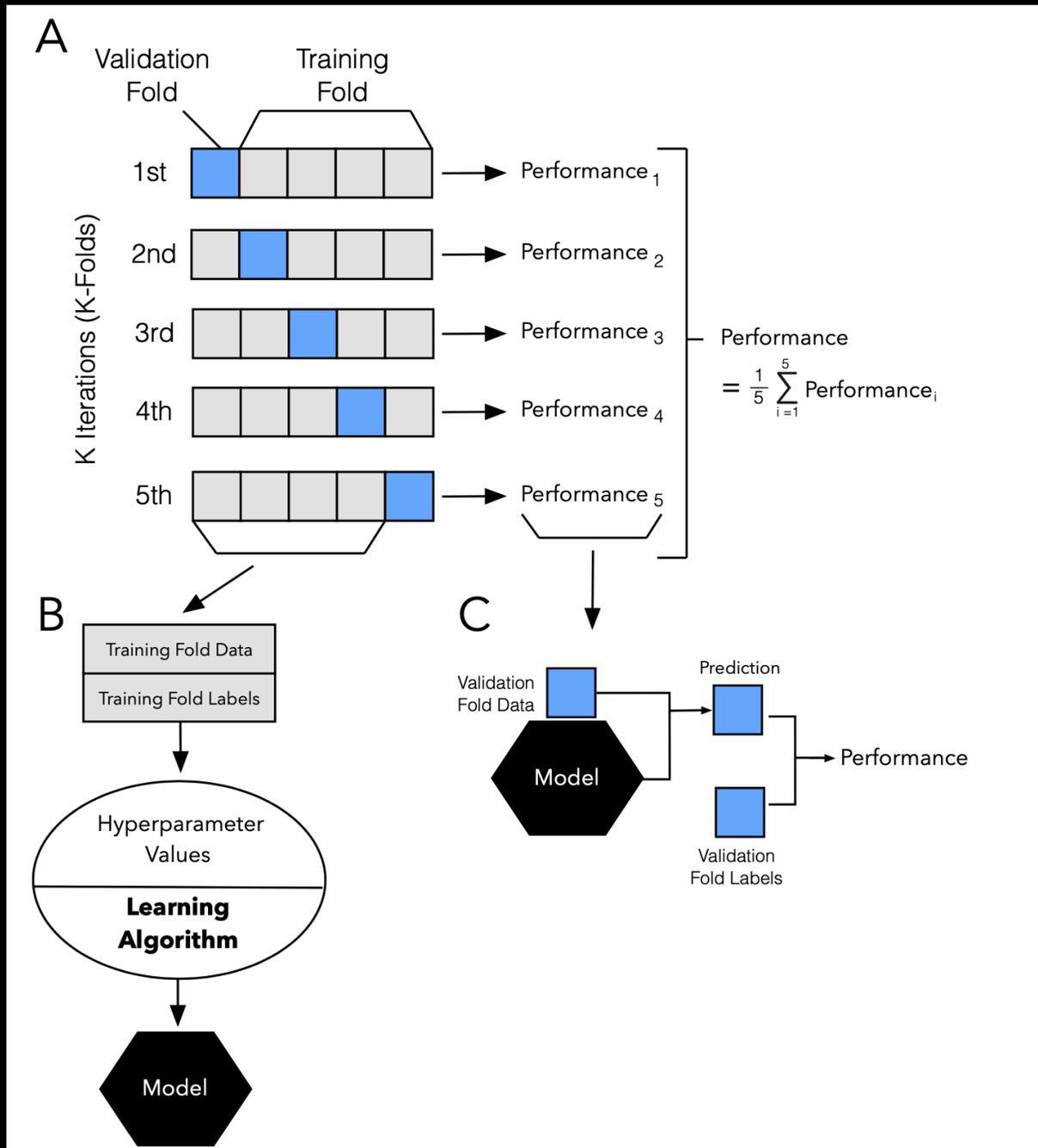
5



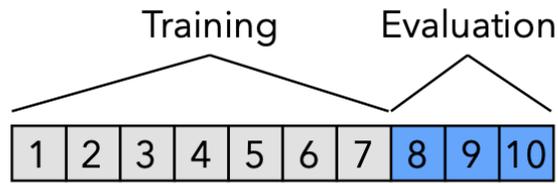
6



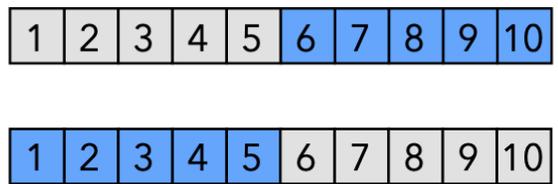
# k-fold Cross-Validation



# Holdout / CV / Repeated Holdout / LOOCV



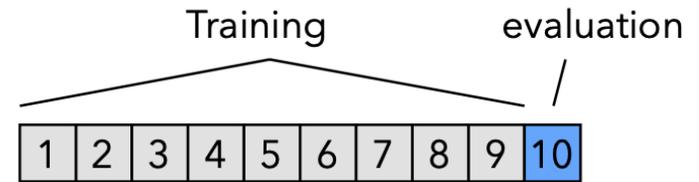
Holdout Method



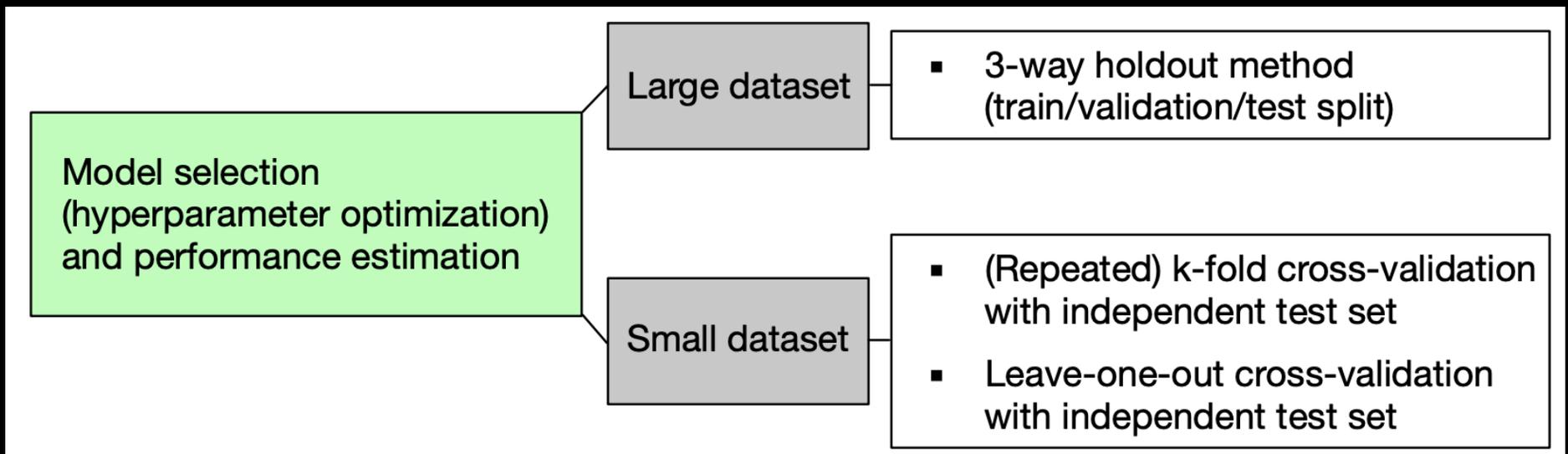
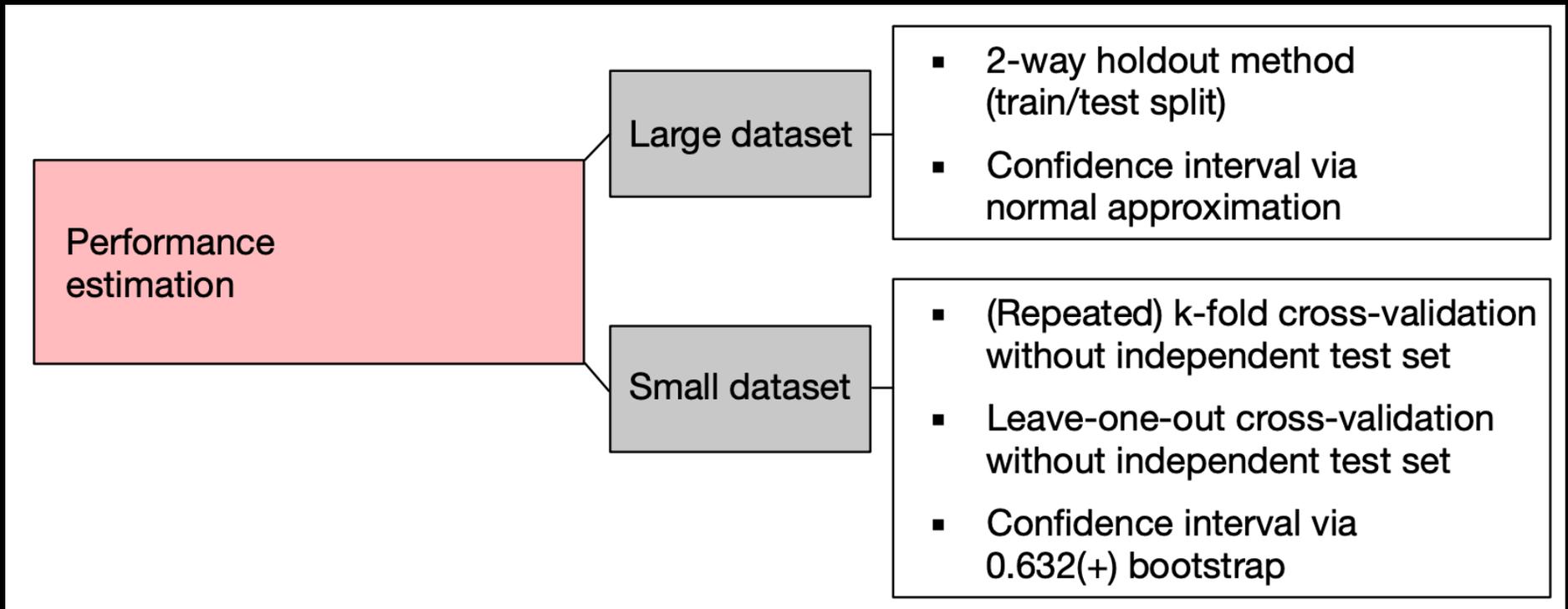
2-Fold Cross-Validatio

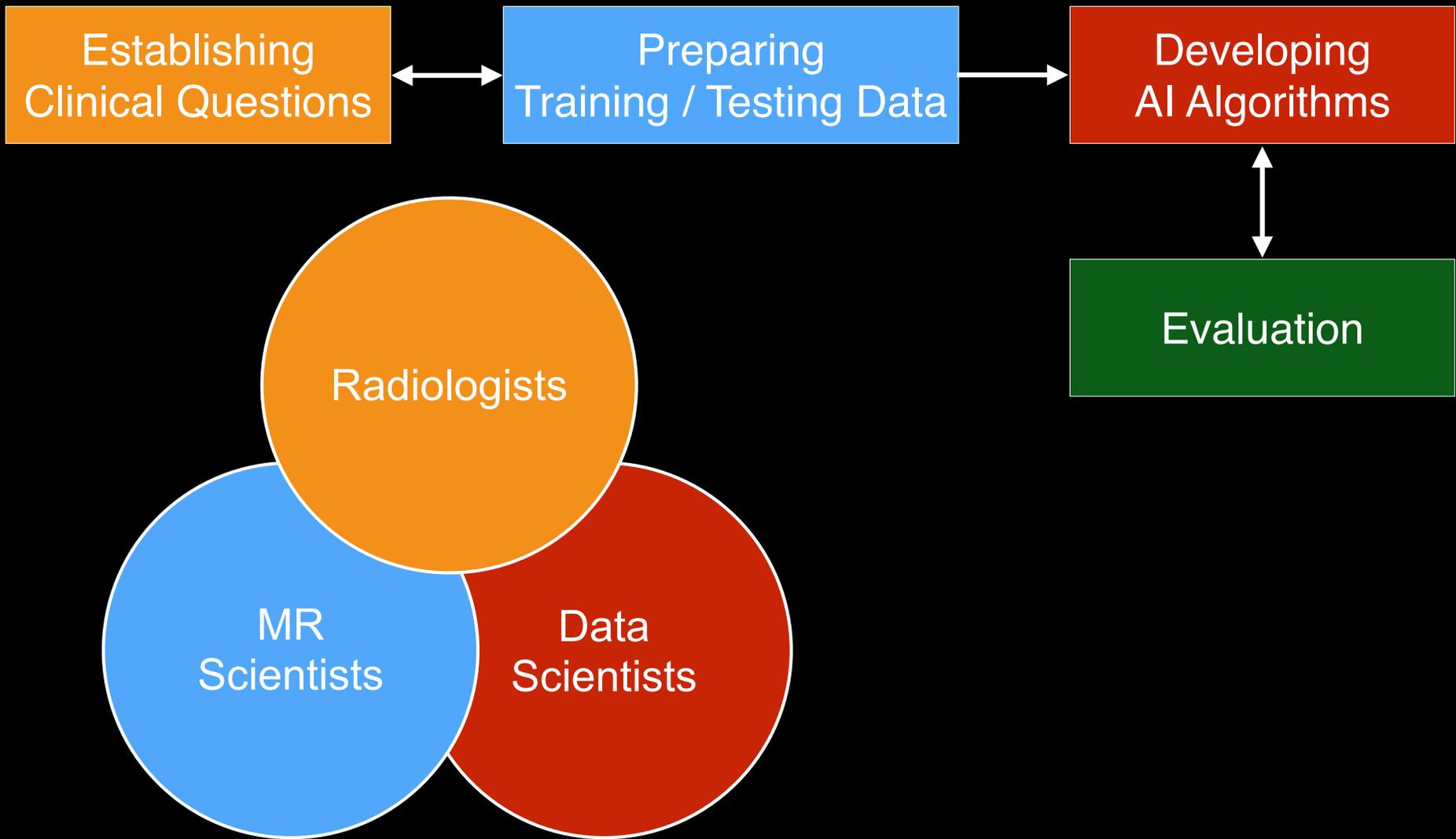


Repeated Holdout



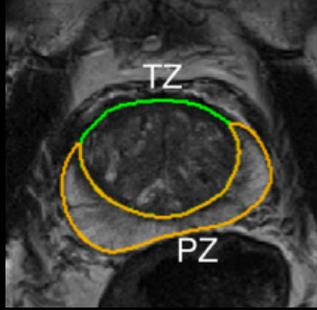
# Summary





# On-going AI Projects

Organ segmentation



Prostate  
Breast  
Placenta



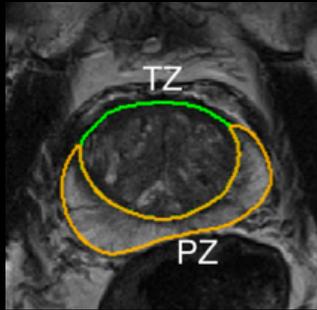
Tumor segmentation

*C Ruiming, et al. IEEE ISBI 2019  
(Runners-up for Best Paper Award)  
Y Liu, et al. IEEE Access 2019  
Y Liu, et al. ICCV 2019 Demo  
Y Liu, et al. IEEE Access 2020*



# On-going AI Projects

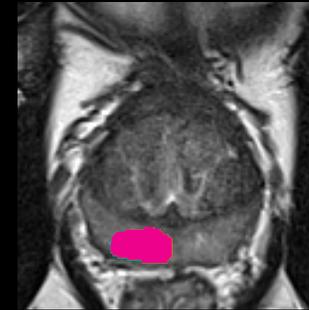
Organ segmentation



Cancer detection



Cancer classification

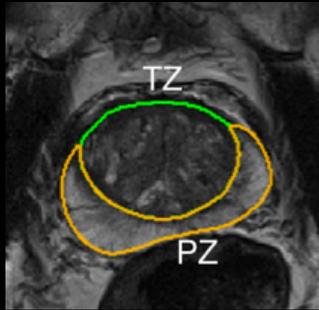


Tumor segmentation

*X Zhong, et al. Abdominal Radiology 2019*  
*C Ruiming, et al. IEEE TMI 2019*  
*K Sung and C Ruiming. Patent Pending*  
*(Serial Number 62/812,914)*  
*K Sung, et al. US Patent# 10,939,87*

# On-going AI Projects

Organ segmentation



Cancer detection

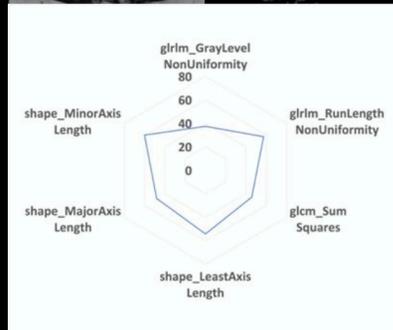
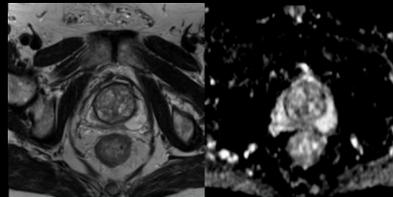


Cancer classification

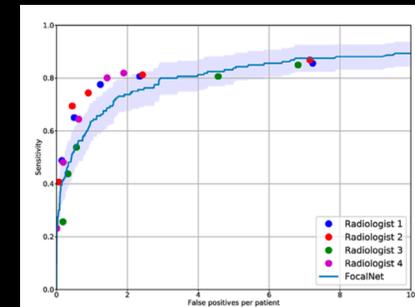


Tumor segmentation

Cancer risk stratification



Human-AI comparison



Cao, Ruiming, et al. JMRI 2021

H Zheng, et al. IEEE ISBI 2021

# On-going AI Projects

Prediction of adverse pregnancy outcome (APO)

Predicting negative MRI findings and anomaly detection

Integrative AI model with imaging and genomic information

Breast cancer risk assessment with BPE calculation

Predicting pathological outcome for non-mass enhancement Breast lesions

Super-resolution MRI via GAN



Qi Miao, M.D.



Melina Hosseiny, M.D.



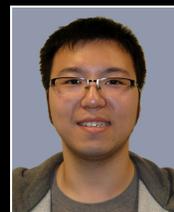
Wakana Murakami, M.D.



Brian Lee, M.D.



Arya Aliabadi, M.D. candidate



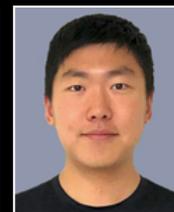
Jiahao Lin



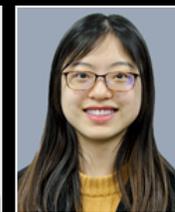
Alibek Danyalov



Yongkai Liu



Haoxin Zheng



Ran Yan

# Future of Prostate MRI: What is Next?

- Human-AI interaction
  - Integration of the models in the clinical workflow
  - Accessibility for non-developers
- Interpretable / explainable AI
  - ROC curves are not everything. Critical to understand which problem matters, what matters is how it is going to affect clinical practice and help save lives
- Multi-institutional validation

# Further Reading

- Original Compressed Sensing
  - <https://ieeexplore.ieee.org/document/1580791>
  - <https://ieeexplore.ieee.org/document/1614066>
- Compressed Sensing MRI
  - <https://ieeexplore.ieee.org/abstract/document/4472246>
- ML model selection and evaluation
  - <https://arxiv.org/abs/1811.12808>

# Thanks!

- Next time
  - Dr. Kim-Lien Nguyen (6/1)
  - Dr. Ai-Chi Chen (6/3)

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